FLAIM: AIM-based Synthetic Data Generation in the Federated Setting

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Synthetic Data Generation (SDG)

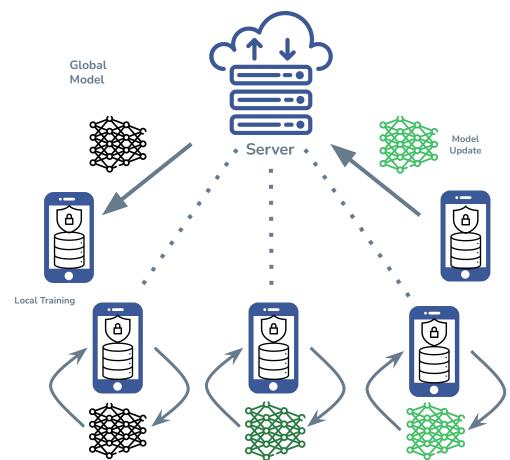
- **Goal:** Produce "fake" data with the properties of real data
- Synthetic data attractive for many reasons
 - Key reason: Privacy
 - Allow general release for downstream tasks e.g., training models, analytics
- Lots of solutions when data is centralised in one place
 GANs, LLMs, Statistical models, etc.
- Methods prone to "memorisation"
 - Can produce verbatim copies of real data
 - Prevention via **Differential Privacy (DP)**



Federated Learning (FL)

• Federated Setting

- Millions of clients, holding local data
- Wish to participate in model training
- Perform local work and send to server
- "Realistic" scenario for large organisations
- Synthetic data not well studied in FL
 - Generic image/language generation (e.g. GANs)
- Our focus: Federated Synthetic Tabular Data





Differential Privacy (DP)

- Parameterized by (${m arepsilon}$, ${m \delta}$):
 - $\circ~arepsilon$ Privacy budget, larger implies less privacy (noise)
 - $\circ~\delta~$ Small probability of failure, set "cryptographically" small
- To guarantee $DP \rightarrow add$ noise into training process
- Smaller the privacy budget = more noise needed
- Has many useful properties
 - Post-processing
 - Composition



Differentially Private Synthetic Data Generators (DP-SDG)

- Define workload of queries **Q**
- Goal: Produce synthetic data with accurate answers over workload Q
- **Example:** Marginal Query e.g., "How many rows have Sex="M" and Employed=True?"
- Want to learn: Model producing synthetic data with low error over **Q**
- Data can still be used for any number of downstream tasks
 - e.g., training ML models
 - No guarantees outside defined workload Q



DP-SDG: "Select-Measure-Generate"

- Private tabular SDG methods follow "Select-Measure-Generate"
- For t = 1, ... ,T
 - 1. Select: query $q \in Q$ with highest error (privately)
 - a. Exponential mechanism with utility scores u(q)
 - 2. Measure: Measure chosen marginal q under calibrated noise
 - a. Gaussian mechanism
 - 3. Generate: Update model to learn noisy marginal



Adaptive Iterative Mechanism (AIM) McKenna et al. (VLDB 24)

- Follows "Select-Measure-Generate" paradigm
 - \circ ("Generate") uses Private-PGM \rightarrow Markov Random Field (MRF)
- Modifications to improve utility:
 - Augmented utility scores "Select" step performed in smarter way
 - Budget annealing Rounds (T) do not need to be set in advance
 - **zCDP accounting** Add less noise for same privacy guarantees
- Translating AIM to the federated setting is the core focus of our work



Federated DP-SDG

- Key Question: How do we federate AIM?
 - = how to federate "Select-Measure-Generate" paradigm

• Distributed setting

- All clients participate over a single (or few) rounds
- Typically assume all participants are available

• Federated setting

- Client participation is subset of true population (e.g., dropout, availability)
- Client data exhibits strong heterogeneity (e.g., distribution skew)



Prior Work: Pereira et al. 2022

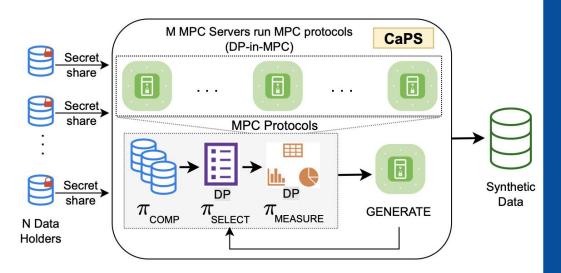
• Distributed setting

- Secure Multi-party Computation (MPC)
- 2/3-party settings, all clients available
- All clients secret-share workload answers to computing server(s)
- Servers work to emulate central algorithm
 - Distributed **Select** + **Measure** steps

• Drawbacks

- Focus on MWEM poor data representation
- "Fully-MPC" solution has overheads





Our Work: Distributed AIM

- Pereira et al., 2022 distribute MWEM using MPC
- Our Work: DistAIM
 - Plug AIM into their framework replacing MWEM
 - Gain utility boost due to AIM over prior work
- **Problem:** not designed with FL in mind inherits issues of Pereira et al.
 - 1. Assumes all clients available to secret-share answers
 - 2. Overhead for clients sharing all workload answers
 - 3. Overhead for server due to MPC operations for exponential mechanism



Our Work: Naive FLAIM

- DistAIM obtains good utility but w/ overheads not compatible with typical FL
- Can we design an analog to traditional FL training?
 - Offload work to clients (make local steps)
 - Client(s) distill work into update => server aggregates and updates global model

• FLAIM

- **"Select":** have each (available) client perform a number of local steps
 - Under LDP
- "Measure": server performs under lightweight cryptography i.e., secure-aggregation
 - Distributed DP
- **"Generate":** update graphical model => post-processing
- Avoids (heavy) MPC \rightarrow secure exponential mechanism



Our Work: AugFLAIM (Non-private)

• **Problem:** clients w/ strong heterogeneity more likely to choose skewed marginals

$$u(q; D_k) \propto ||M_q(D_k) - M_q(\hat{D}^{(t)})||_1$$

- **Solution:** correct local skew by penalising q with strong heterogeneity
- How to define heterogeneity? Deviation of clients marginal from global

$$\tau_k(q) := ||M_q(D_k) - M_q(D)||_1$$

• **Problem:** M_a(D) is exactly what we are trying to learn (privately) via AIM !



Our Work: AugFLAIM (Private)

- **Problem:** Can't ever learn "true" heterogeneity of clients local marginals
- **Private Proxy:** have clients submit 1-way marginals every round
 - Pay privacy cost in the number of features
 - Obtain subsequently more accurate 1-way answers

$$\tilde{\tau}_k(q) := \frac{1}{|q|} \sum_{j \in q} \|M_{\{j\}}(D_k) - \tilde{M}_{\{j\}}(D)\|_1$$



Methods

1. Naive FLAIM

- Translation of AIM to FL with no modifications
- "SecAgg + noise"

2. AugFLAIM (Oracle)

- Assumes knowledge of heterogeneity skew
- Modify select step for local clients taking this into account

3. AugFLAIM (Private)

- Private proxy of heterogeneity
- Estimates all 1-way marginals and query from "select" step at each round



Experiment: Comparison with Baselines

- Popular deep learning alternative
 OP-CTGAN
- FLAIM baselines
 - NaiveBayes 1-way marginals only
 - **FLAIM (Random)** random decisions
 - NaiveFLAIM no modification to utility score
- Our proposal: AugFLAIM (Private)
- Table shows NLL compared to test set

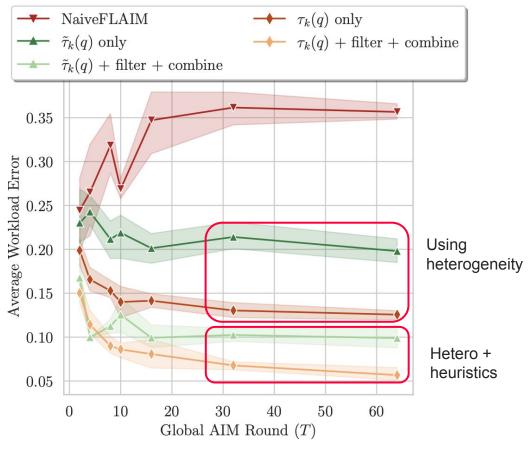
Table 1: Comparison of FLAIM approaches against baselines for negative log-likelihood (NLL), $\varepsilon = 5$. Smaller NLL is better.

Method / Dataset	Adult	Credit	Covtype
Fed DP-CTGAN	37.1	83.8	62.7
FedNaiveBayes	25.33	18.02	44.9
FLAIM (Random)	83.9	47.7	58.4
NaiveFLAIM	29.4	18	45.4
AugFLAIM (Private)	20.87	16.2	41.6
DP-CTGAN	28.6	27.6	45.9
AIM	19.2	15.57	40.92



Experiment: Ablation

- Why does AugFLAIM (Private) perform so well?
- NaiveFLAIM
 - No utility score modification
- AugFLAIM (Oracle)
 - Access to true heterogeneity
- AugFLAIM (Private)
 - Private proxy for heterogeneity



(b) Credit



Experiment: Overheads

- If T is small
 - Utility of AugFLAIM >= DistAIM
- If T is large
 - DistAIM favorable performance
- **Bandwidth** = Average client sent & received
- On Adult, DistAIM requires
 - 2x more rounds
 - 1300x increase in bandwidth
 - \circ to reduce workload error by ~¹/₂



Table 2: Overhead of DistAIM vs. FLAIM at optimal T

	$T(\uparrow)$	Bandwidth (†)	$\operatorname{Err}(\downarrow)$	NLL (\downarrow)
Adult	$2 \times$	1300×	$0.58 \times$	0.1×
Magic	$3.2 \times$	$1643 \times$	$0.19 \times$	0.15 imes
Mushroom	$7 \times$	7.5 imes	0.79x	0.4 imes
Nursery	$20 \times$	3.4 imes	$0.89 \times$	0.17 imes

Conclusion

- FLAIM provides a way to
 - obtain comparable utility to DistAIM in practical FL
 - whilst reducing client overheads via lightweight MPC

• Limitations

- Example-level DP
- Inherits limitations of "select-measure-generate"
 - Continuous features
 - Specifying a workload Q
 - High-dimensional datasets

Poster Number 91 Today, 6:30pm



arXiv:2310.03447

