- p.14, Fig. 1.4: Replace 2r (on left) by 2R.
- p.24, l.10: For weak metrizability also boundedness of X is needed (but this also follows later from the coercivity).
- p.32, l.-8 (Example 2.12): Replace  $\mathbb{R}^m$  by  $\mathbb{R}^3$ .
- p.39, l.5: Replace f by F.
- p.40, l.1: Add the condition dim  $X < \infty$ .
- p.42, l.1 (Example 2.26): Also assume that  $\varphi \ge 0$  and  $\varphi(0) = \inf \varphi = 0$ .
- p.54, l.-10 (Proposition 3.9): It should additionally be assumed here that  $|D_Z D_A f(x, u, A)| \le C(1+|u|+|A|)$  for  $Z \in \{x, u, A\}$  in order for div $[D_A f(x, u(x), \nabla u(x))]$  to be well-defined (in fact, in (3.6) this existence is assumed).
- p.57, l.2 (Theorem 3.11): This result also holds, with the same proof, for any weak solution  $u_* \in W^{1,2}_{loc}(\Omega; \mathbb{R}^m)$  of the corresponding Euler–Lagrange equation (this is used in the bootstrapping argument on p.61).
- p.58, l.-4:  $k \in \{1, ..., d\}$  (braces missing).
- p.63, l.-4: Replace  $f: \mathbb{R}^{d \times d} \to \mathbb{R}$  by  $f: \mathbb{R}^d \to \mathbb{R}$ .
- p.65, l.-3 (Theorem 3.21): One also needs to assume  $|D_v f(x, v, A)|, |D_A f(x, v, A)| \le C(1+|v|^{p-1}+|A|^{p-1})$ for some C > 0 and  $p \in [1, \infty)$  (see Remark 3.2).
- p.69, l.15: f needs to be *twice* continuously differentiable and we also need to require that  $H(\cdot, \tau) \in W^{1,2}(\Omega; \mathbb{R}^m)$  for every  $\tau \in \mathbb{R}$ .
- p.70, l.7 (Theorem 3.23): The growth bound should read (no *p*):  $|D_v f(x, v, A)|, |D_A f(x, v, A)| \le C(1 + |v| + |A|).$
- p.76, l.11 (Example 3.31): Replace  $\leq$  by  $\geq$ .
- p.78, l.6 (Exercise 3.2): Delete point (iii).
- p.84, l.13 (Lemma 4.3): Replace  $K \subset \mathbb{R}^{m \times d}$  by  $K \subset \mathbb{R}^N$ .
- p.84, l.15 (Lemma 4.3): Replace  $(\nu_j)$  by  $(\nu^{(j)})$ .
- p.85, l.-7 (Theorem 4.4): The family  $(\nu_x)_{x\in\Omega} \subset \mathcal{M}^1(\mathbb{R}^N)$  is weakly\* measurable with respect to  $\kappa$ .
- p.92, l.2 (Lemma 4.7): Replace  $C_0(\Omega) \times C_0(\mathbb{R}^N)$  by  $C_0(\Omega \times \mathbb{R}^N)$ .
- p.93, l.-6 (Example 4.10):  $\Omega$  is  $(0,1)^2$  everywhere.
- p.97, l.4 (proof of Lemma 4.13): Replace  $|\tau_k V_{i(k)}|$  by  $|\tau_k V_{i(k)}|^p$ .
- p.97, l.10 & l.-10 (proof of Lemma 4.13): Replace  $v_k$  by  $v_{i(k)}$ .
- p.97, l.-12 (proof of Lemma 4.13): Replace  $V_k$  by  $V_{j(k)}$ .
- p.97, l.-11 & p.98, l.3 (proof of Lemma 4.13): Replace  $h \in C_0(\mathbb{R}^m)$  by  $h \in C_0(\mathbb{R}^{m \times d})$ .
- p.103, l.9 (Problem 4.8): Also require  $\nu_x(\partial E) = 0$ .
- p.111, l.4 (proof of Proposition 5.3): The display should read (lim sup added):  $\lim \sup_{k \to \infty} \|\nabla v_{j,k}\|_{\mathrm{L}^{\infty}} \leq \lim \sup_{k \to \infty} \|\nabla u_k\|_{\mathrm{L}^{\infty}} + |F| < \infty.$

- p.115, l.10 (proof of Lemma 5.8): Replace  $u \mapsto M(\nabla u)$  by  $u \mapsto \int_{\Omega} M(\nabla u) \, \mathrm{d}x$ .
  - p.115, l.15 (proof of Lemma 5.8): Replace "." by " $\otimes$ ".
  - p.116, l.4 (proof of Lemma 5.8): Replace  $M_{\neg l}^{\neg k}(\nabla u) = \cdots$  by  $(-1)^{k+l}M_{\neg l}^{\neg k}(\nabla u) = \cdots$ .
  - p.117, l.11 (Lemma 5.10): Replace  $L^{\infty}$  by  $W^{1,\infty}$ .
  - p.117, l.-11 (proof of Lemma 5.10): Replace  $\int_{\Omega} M_{\neg l}^{\neg k}(\nabla u_j)\psi \, dx$  by  $(-1)^{k+l} \int_{\Omega} M_{\neg l}^{\neg k}(\nabla u_j)\psi \, dx$ ; same for the following display.
  - p.117, l.10 (proof of Lemma 5.10): The density argument needs to be applied only after the displays  $\int_{\Omega} M_{-l}^{-k}(\nabla u)\psi \, dx$  and  $-\sum_{l=1}^{3} \int_{\Omega} \left[ u^1(\operatorname{cof} \nabla u)_l^1 \right] \partial_l \psi \, dx = \int_{\Omega} \det \nabla u \, \psi \, dx$ , respectively.
  - p.118, l.-6 & l.-2 (proof of Lemma 5.11): Replace  $\Omega$  by B(0, 1).
  - p.120, l.-2 (proof of Theorem 5.13): Replace  $v \in \mathbb{R}^n$  by  $v \in \mathbb{R}^d$ .
  - p.120, l.10 (Theorem 5.13 (ii)): Replace dist( $\nabla u_i(x), \{A, B\}$  by dist( $\nabla u_i(x), \{A, B\}$ ).
  - p.123, l.11 (proof of Proposition 5.14):  $(u_i) \subset W^{1,p}(\Omega; \mathbb{R}^m)$  is a generating sequence for  $\nu$ .
  - p.123, l.-3 (proof of Proposition 5.14): Replace dx by dy.
  - p.128, l.2 (Lemma 5.19): The convergence in (5.15) only holds if the sequence  $(f(x, u_j, V_j))_j$  additionally is assumed to be uniformly L<sup>1</sup>-bounded and equiintegrable (like in Theorem 4.1 (iii)). However (and this is what we use later in the proof of Theorem 5.20), for Carathéodory integrands  $f: \Omega \times \mathbb{R}^M \times \mathbb{R}^N \to \mathbb{R}$  satisfying the *p*-growth bound (5.14), it holds that

$$\liminf_{j \to \infty} \int_{\Omega} f(x, u_j(x), V_j(x)) \, \mathrm{d}x \ge \int_{\Omega} \left\langle f(x, u(x), \cdot), \nu_x \right\rangle \, \mathrm{d}x.$$

- p.128, l.-11 (Theorem 5.20): Replace  $f: \Omega \times \mathbb{R}^m \times \mathbb{R}^{m \times d} \to \mathbb{R}$  by  $f: \Omega \times \mathbb{R}^m \times \mathbb{R}^{m \times d} \to [0, \infty)$ .
- p.129, l.1 (Remark 5.21): Replace  $q \in [1, p/(d-p))$  by  $q \in [1, dp/(d-p))$ .
- p.140, l.-3 (proof of Lemma 6.6): Replace  $C^1$  by  $C^{\infty}$  (or  $C^2$ ); also several other occurrences throughout this proof.
- p.140, l.-2 (proof of Lemma 6.6): Delete  $(-1)^{k+l}$ .
- p.141, l.2 (proof of Lemma 6.6): Delete  $(-1)^{k+l}$ .
- p.147, l.-9 (proof of Theorem 6.9): Replace  $x' \in u(\Omega)$  by  $x' \in u_*(\Omega)$ .
- p.156, 1.6/7 (proof of Lemma 7.2): Replace D by B(0, 1).
- p.159, l.-10 (proof of Theorem 7.5): A more complete proof is as follows: The functional  $\mathcal{F}_*$  is weakly lower semicontinuous as the supremum of weakly lower semicontinuous functionals. Indeed, if  $u_j \rightharpoonup u$  in X, then for all weakly lower semicontinuous  $\mathcal{H} \colon X \to \mathbb{R}$  with  $\mathcal{H} \leq \mathcal{F}$ ,

$$\mathcal{H}[u] \leq \liminf_{j \to \infty} \mathcal{H}[u_j] \leq \liminf_{j \to \infty} \mathcal{F}_*[u_j].$$

Taking the supremum over all such  $\mathcal{H}$ , we see that  $\mathcal{F}_*[u] \leq \liminf_{j \to \infty} \mathcal{F}_*[u_j]$ .

Let  $(u_j) \subset X$  be a minimizing sequence for  $\mathcal{F}$ . By the weak coercivity, we may assume that  $u_j \rightharpoonup u_*$  in X. Then,

$$\inf_{X} \mathcal{F} \leq \mathcal{F}[u_*] \leq \liminf_{j \to \infty} \mathcal{F}_*[u_j] \leq \liminf_{j \to \infty} \mathcal{F}[u_j] = \inf_{X} \mathcal{F}.$$

Hence,  $\mathcal{F}_*$  attains its minimum, which is equal to the infimum of  $\mathcal{F}$  over X.

• p.166, l.7 (Example 7.10): The sentence should read: "However, since rank B = 1, we have that  $g(\mathbf{P}(A + tB)) = 0$  is affine in  $t \in \mathbb{R}$ .".

• p.172 ff. (Theorem 7.15): The functional-analytic setup in the proof needs to be changed as follows: Let  $\mathcal{M}_p(\mathbb{R}^{m \times d})$  for  $p \in (1, \infty)$  denote the class of finite signed measures on  $\mathbb{R}^{m \times d}$  with bounded p'th-order absolute moment, that is,  $\mathcal{M}_p(\mathbb{R}^{m \times d}) := \{ \mu \in \mathcal{M}(\mathbb{R}^{m \times d}; \mathbb{R}) : \int 1 + |A| \, d\mu(A) < \infty \}$ . Then, an integrand  $h \in \mathbf{I}^p(\mathbb{R}^{m \times d})$  can be viewed as a linear functional on  $\mathcal{M}_p(\mathbb{R}^{m \times d})$  via the duality pairing  $\langle \mu, h \rangle := \int h \, d\mu$  (where  $\mu \in \mathcal{M}_p(\mathbb{R}^{m \times d})$ ). The functionals  $h \mapsto \langle \cdot, h \rangle$  (where  $h \in \mathbf{I}^p(\mathbb{R}^{m \times d})$ ) separate the points of  $\mathcal{M}_p(\mathbb{R}^{m \times d})$ , that is, for  $\mu_1, \mu_2 \in \mathcal{M}_p(\mathbb{R}^{m \times d})$  with  $\mu_1 \neq \mu_2$  there is an integrand  $h \in \mathbf{I}^p(\mathbb{R}^{m \times d})$  such that  $\langle \mu_1, h \rangle \neq \langle \mu_2, h \rangle$ .

Let  $\tau_p$  be the weakest topology on  $\mathcal{M}_p(\mathbb{R}^{m \times d})$  that makes all the functionals  $h \mapsto \langle \cdot, h \rangle$  continuous. It is a general result of topology (see, e.g., Theorem 3.10 of [W. Rudin: Functional Analysis, McGraw-Hill, 1991]) that the topological space  $(\mathcal{M}_p(\mathbb{R}^{m \times d}), \tau_p)$  is a locally convex topological vector space and its dual space  $(\mathcal{M}_p(\mathbb{R}^{m \times d}), \tau_p)^*$  is given as  $\mathbf{I}^p(\mathbb{R}^{m \times d})$  (via the above duality pairing).

The set  $\mathbf{GY}_{\text{hom}}^{p}(F)$  then needs to be viewed as a subset of the space  $\mathcal{M}_{p}(\mathbb{R}^{m\times d})$  (and not of  $\mathbf{I}^{p}(\mathbb{R}^{m\times d})^{*}$  as before), where it is convex and  $\tau_{p}$ -closed (it is not weakly\*-closed in  $\mathbf{I}^{p}(\mathbb{R}^{m\times d})^{*}$  because there is no tightness of the masses, e.g., for  $\nu_{j} = (1-j^{-p})\delta_{0} + (j^{-p}\delta_{-jA}+j^{-p}\delta_{jA})/2$  as  $j \to \infty$ , where A is a rank-one matrix). In Lemma 7.17 and the proof of Theorem 7.15 one thus needs to replace every occurrence of  $\mathbf{I}^{p}(\mathbb{R}^{m\times d})^{*}$  by  $\mathcal{M}_{p}(\mathbb{R}^{m\times d})$  (effectively moving from a dual to a pre-dual) and use the  $\tau_{p}$ -topology instead of the weak\* topology everywhere; the arguments are otherwise the same. As a result, Lemma 7.17 then needs to read as follows: "For any  $F \in \mathbb{R}^{m\times d}$  the set  $\mathbf{GY}_{\text{hom}}^{p}(F)$  is convex and  $\tau_{p}$ -closed in  $\mathcal{M}_{p}(\mathbb{R}^{m\times d})$ ." The application of the Hahn–Banach separation theorem (for locally convex topological vector spaces; see Theorem 3.10 in *loc. cit.*) is then also with respect to the space  $(\mathcal{M}_{p}(\mathbb{R}^{m\times d}), \tau_{p})$  and its dual  $\mathbf{I}^{p}(\mathbb{R}^{m\times d})$ . [This corrected setup is due to Stefan Müller.]

- p.174, l.13 (proof of Lemma 7.17): Replace  $u_j \in W^{1,p}(\Omega; \mathbb{R}^m)$  by  $u_j \in W^{1,p}(B(0,1); \mathbb{R}^m)$ .
- p.178, l.16 (Theorem 7.18): Delete the second "convex".
- p.175, l.1 (proof of Theorem 7.15): The necessity proof also needs to explicitly invoke Proposition 5.14 to localize.
- p.222, l.5 (Lemma 8.32): Replace  $\rightarrow$  by  $\stackrel{*}{\rightarrow}$  (in  $\mathcal{M}_{loc}$ ).
- p.260, l.-3: Replace  $K \subset \mathbb{R}^{3 \times 12}$  by  $K \subset \mathbb{R}^{3 \times 2}$ .
- p.278, l.-12 (Lemma 10.6): Replace  $\mu_0$  by  $\mu$ .
- p.298, l.4 (Problem 10.4): Replace  $y \in Q_n(x_0, r)$  by  $y \in Q_n(0, 1)$ .
- p.326, l.16 (proof of Theorem 11.21): Replace  $\geq \mu \|\nabla u_j\|_{L^1}$  by  $\geq \mu \cdot \limsup_{j \to \infty} \|\nabla u_j\|_{L^1}$ .
- p.372, l.-4: Replace  $\liminf_{k\to\infty} \mathcal{F}_k[u_k] = \liminf_{k\to\infty} \inf_X \mathcal{F}_k$  by  $\lim_{k\to\infty} \mathcal{F}_k[u_k] = \liminf_{k\to\infty} \inf_X \mathcal{F}_k$ .
- p.423, l.-7: Replace  $\eta_{\delta}(x) := \frac{1}{\delta^d} \eta\left(\frac{x}{\delta^d}\right)$  by  $\eta_{\delta}(x) := \frac{1}{\delta^d} \eta\left(\frac{x}{\delta}\right)$ .
- p.426, l.-2 (Theorem A.36): f (not Mf) is Lipschitz on the set  $\{M(|f| + |\nabla f|) < K\}$ .