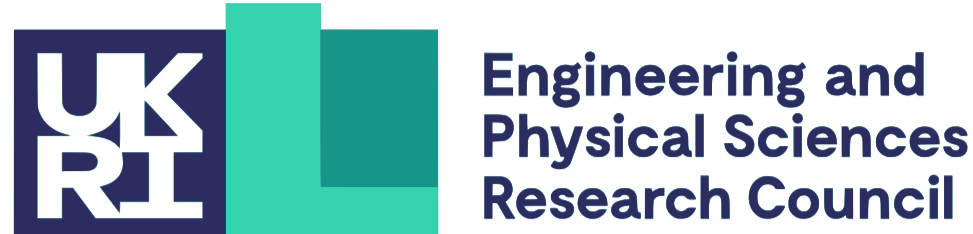


# Predicting the Impact of Childhood Vaccines: Health & Economics

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## Biological Background<sup>1,2</sup>

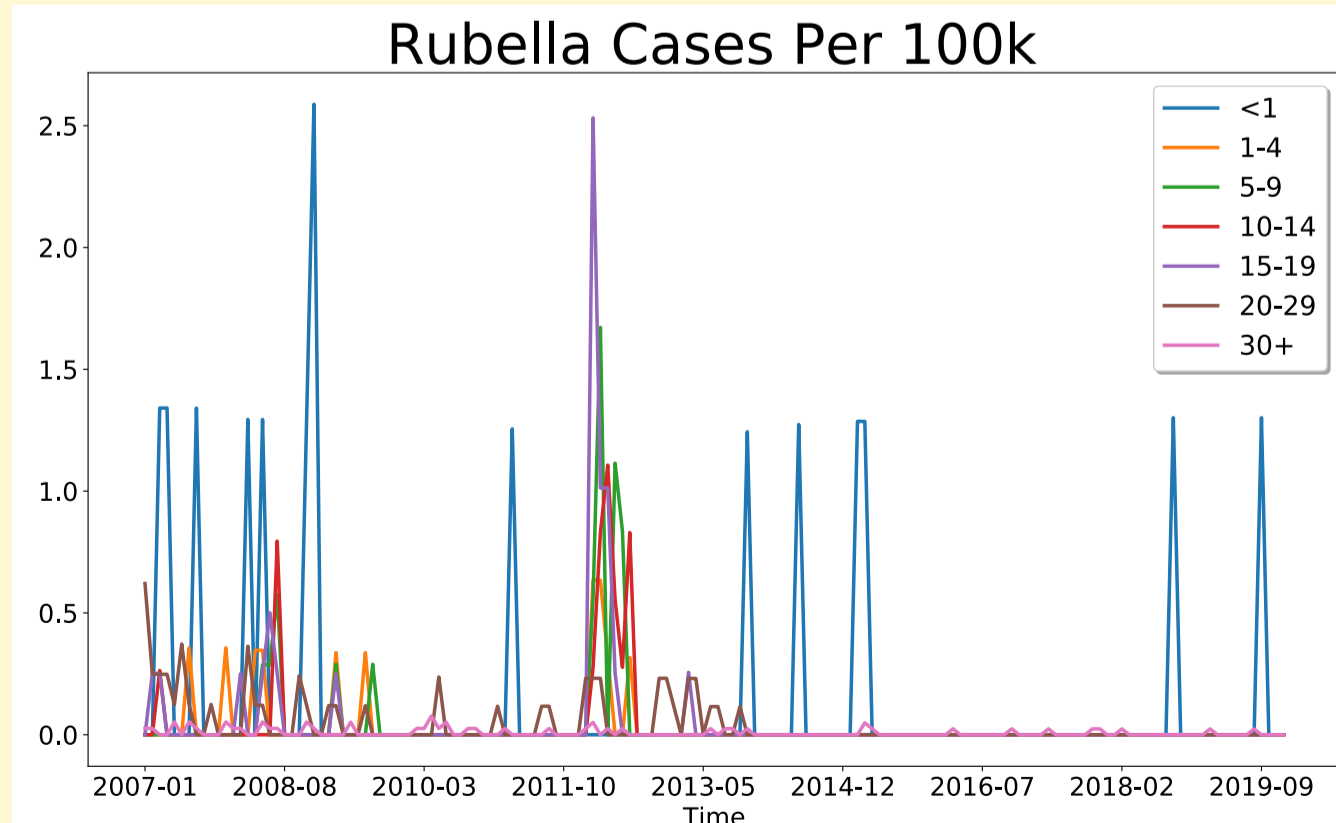
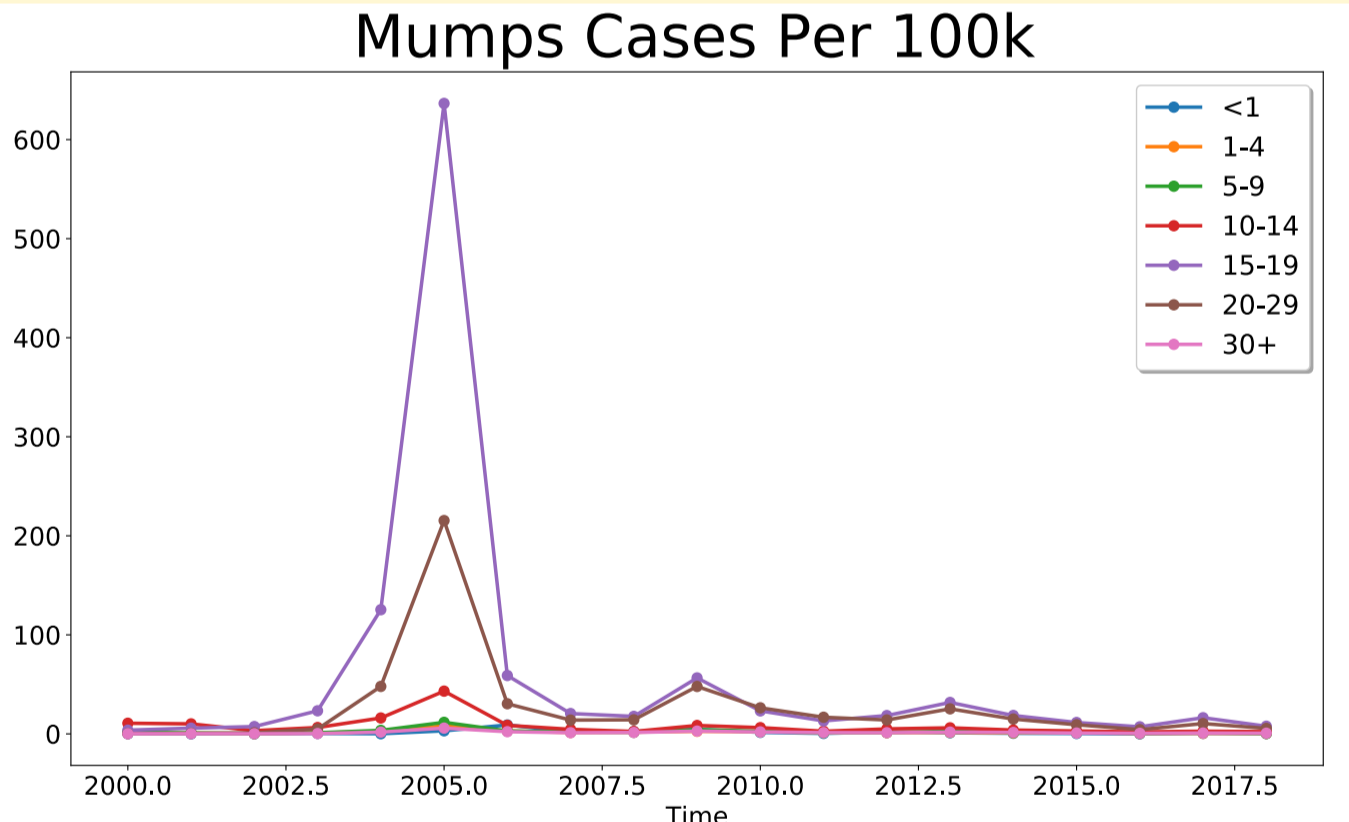
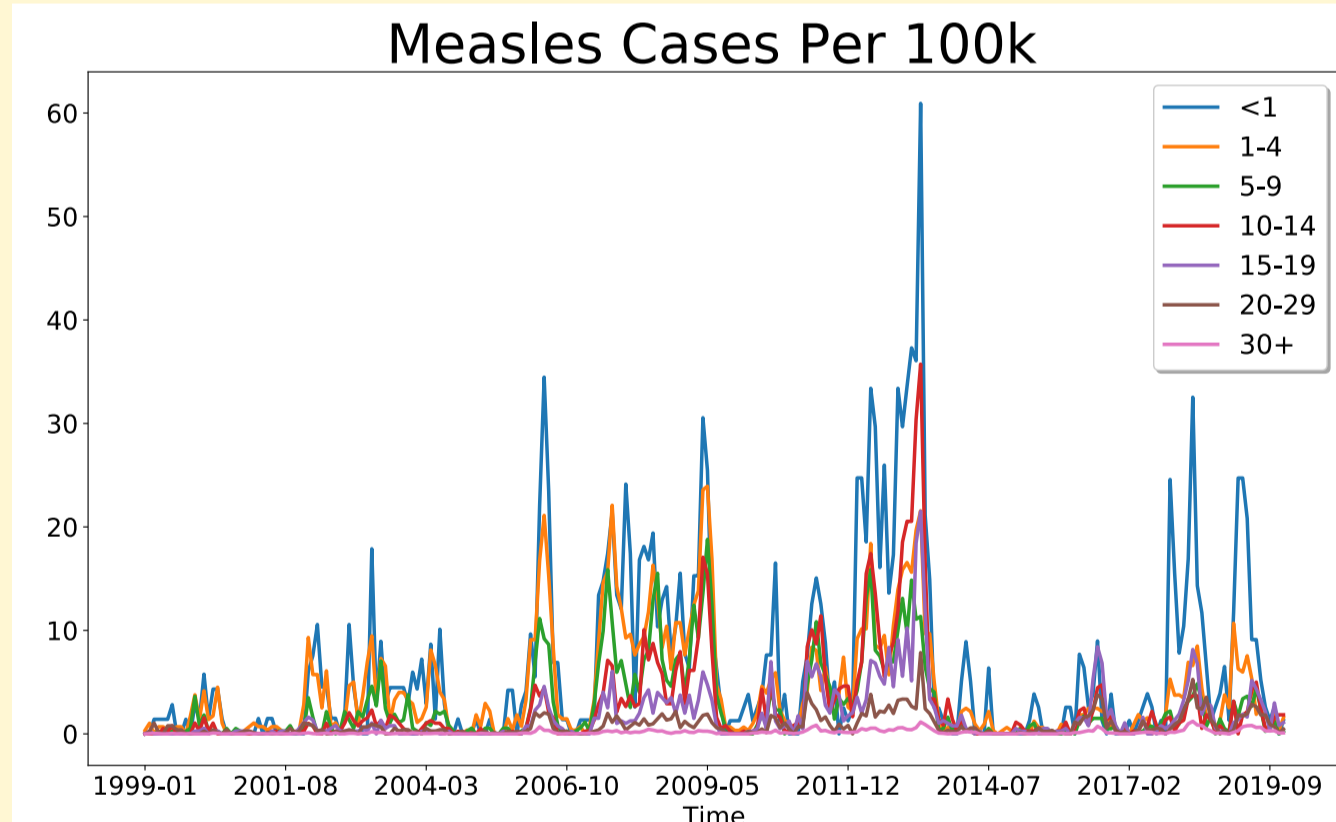
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| <p><b>Measles</b></p> <ul style="list-style-type: none"> <li>• Infectious period lasts 6-7 days and recovery takes 7-10 days</li> <li>• Airborne: contained in droplets (survives on surfaces for hours)</li> <li>• Severe cold-like symptoms, red eyes, sensitivity to light, fever, rash</li> <li>• Serious complications: pneumonia, encephalitis (babies &lt; 1 year old, children with weakened immune system)</li> <li>• Risks during pregnancy include miscarriage, stillbirth, premature birth</li> </ul> | <p><b>Mumps</b></p> <ul style="list-style-type: none"> <li>• Infectious period lasts 4-8 days (airborne) and recovery takes 1 to 2 weeks.</li> <li>• Most common symptom is swelling of the parotid glands</li> <li>• Headaches, joint pain, high temperature</li> <li>• Can be passed on by infected people who have no obvious symptoms</li> <li>• Serious complications: viral meningitis, swelling of testicles/ovaries if gone through puberty, encephalitis</li> </ul> | <p><b>Rubella</b></p> <ul style="list-style-type: none"> <li>• Infectious period lasts 11-12 days (airborne) and recovery takes about 3 days</li> <li>• Symptoms include a red/pink spotty rash, joint pain, and flu-like symptoms</li> <li>• Serious complications: encephalitis, low platelet count, ear infection</li> <li>• If caught early during pregnancy can lead to miscarriage or baby born with Congenital Rubella Syndrome (CRS)</li> <li>• Babies with CRS may spread the virus for more than a year</li> </ul> |
|---|--|--|

### MMR Vaccine

**2 doses**  
 1 year old (*Newborn babies have antibodies passed on from their mother at birth which make the MMR vaccine less effective. Antibodies are almost gone by the age of 1.*)  
 3 years and 4 months old (*before child goes to school*)  
 99% of people protected against measles and rubella and 88% against mumps

**Side Effects**  
 Area around needle injection might get red, swollen, and sore.  
 7 to 11 days after injection babies or young children may feel unwell for about 2-3 days.

## Data Sources



- **New reported cases:** epidemiological data for MMR diseases are available as age standardised rates from the ECDC Surveillance Atlas of Infectious Diseases dataset  
*Measles:* monthly data, 1999-2019    *Mumps:* annual data, 2000-2017  
*Rubella:* monthly data, 2007-2019
- **Demographics:** collected from the Office for National Statistics  
*Birth rate:* per million, from 1888    *Death rate:* by single age, from 1974 to 2018  
*Annual mid-population:* from 1971
- **Vaccination rate:** from Public Health England  
*MMR vaccine coverage:* 1985-2013



**References**  
 1. NHS. www.nhs.uk. 2. Anderson, Roy M., B. Anderson, and Robert M. May. *Infectious diseases of humans: dynamics and control*. Oxford university press, 1992. 3. Bolker, Ben M., and Grenfell, Bryan T. "Chaos and biological complexity in measles dynamics." *Proceedings of the Royal Society of London. Series B: Biological Sciences* 251.1330 (1993): 75-81. 4. Bolker, B., and Grenfell, Bryan T. "Space, persistence and dynamics of measles epidemics." *Philosophical Transactions of the Royal Society of London. Series B: Biological Sciences* 348.1325 (1995): 309-320. 5. Zhou, Fangjun, et al. "Economic evaluation of the routine childhood immunization program in the United States, 2009." *Pediatrics* 133.4 (2014): 577-585.

## ODE Model for Diseases<sup>3,4</sup>

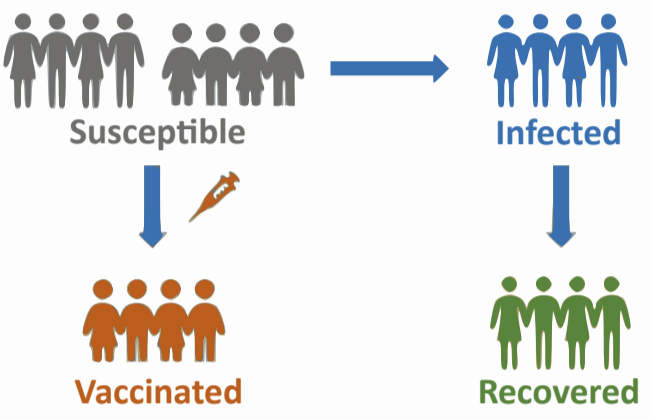
Let us define a  $k$ -age group compartmental SIRV model for the infection dynamics of the diseases covered by the MMR vaccine:

$$\frac{dS_i}{dt} = \delta_{i1}B - \sum_{j=1}^k \beta_i c_{ij} S_i I_j - v_i S_i - d_i S_i + \delta(t - t_{\text{end}}) a_{i-1} S_{i-1} - \delta(t - t_{\text{end}}) a_i S_i$$

$$\frac{dI_i}{dt} = \sum_{j=1}^k \beta_i c_{ij} S_i I_j - \gamma_i I_i - d_i I_i + \delta(t - t_{\text{end}}) a_{i-1} I_{i-1} - \delta(t - t_{\text{end}}) a_i I_i$$

$$\frac{dR_i}{dt} = \gamma_i I_i - d_i R_i + \delta(t - t_{\text{end}}) a_{i-1} R_{i-1} - \delta(t - t_{\text{end}}) a_i R_i$$

$$\frac{dV_i}{dt} = v_i S_i - d_i V_i + \delta(t - t_{\text{end}}) a_{i-1} V_{i-1} - \delta(t - t_{\text{end}}) a_i V_i$$



where  $i = 1, \dots, k$  and  $S_i, I_i, R_i, V_i$  are an  $i$ -age group of the proportion of Susceptible, Infected, Recovered, and Vaccinated people.

- $B$  = Birth rate
  - $\beta_i$  = Age-based force of Infection
  - $v_i$  = Age-based Vaccination rate
  - $d_i$  = Age-based (natural) death rate
  - $\gamma_i$  = Age-based Recovery rate
  - $a_i$  = Aging rate ( $a_0 = a_k = 0$ )
  - $c_{ij}$  = Average number of contacts from  $j$ -age group to  $i$ -age group (*Who Interacts With Who*)
- $$\delta(t-x) = \begin{cases} 0 & \text{if } t \neq x \\ \infty & \text{if } t = x \end{cases}$$
- and  $\int_{x-\epsilon}^{x+\epsilon} \delta(t-x) dt = 1$
- $$\delta_{ij} = \begin{cases} 0 & \text{if } i \neq j \\ 1 & \text{if } i = j \end{cases}$$

## Economic Evaluation<sup>5</sup>

- **Cost-effectiveness analysis:** Compares costs with natural biomedical units of outcomes i.e. number of cases, life years gained or quality-adjusted life years (QALY). Current threshold for treatments, suggested by NICE, is £20,000 to £30,000 per QALY.
- **Cost-benefit analysis:** Attaches monetary values to the measure of effect.
- **Cost-utility analysis:** Focuses more on the financial aspect, applied to pharmacoeconomics.

- We look at compendia and NHS reference costs for:
- Direct costs (direct labour, materials, medicines, facilities etc.)
  - Indirect/societal costs (volunteer services, cost of work loss etc.)
  - Costs associated to immunisation
  - Benefits of vaccination

**Calculation:**  
*Net Present Value (NPV):*  
 to analyse profitability of a project;  
 considers time value of money.

$$NPV = \sum_{t=0}^T \frac{R_t}{(1+r)^t}$$

$R_t$  = Net cash inflow-outflows during a single time period,  $t$   
 $r$  = Discount rate (rate of inflation)  
 $t$  = Time period in years  
 $T$  = Number of time periods under consideration

## Future Work

- **Modelling**
  - Having defined the model and identified suitable data sources, the next step is to attempt to fit the model and evaluate how well it fits the data.
  - Addition of temporal forcing.
- **Health Economics of MMR Vaccinations**
  - Modelling impact of alternative vaccination policies
  - Pricing of MMR vaccination policies.
- **Parameter Estimation**
  - Using different *Who Interacts With Who* matrices (e.g. BBC pandemic) instead of the current POLYMOD (see heatmap)

