

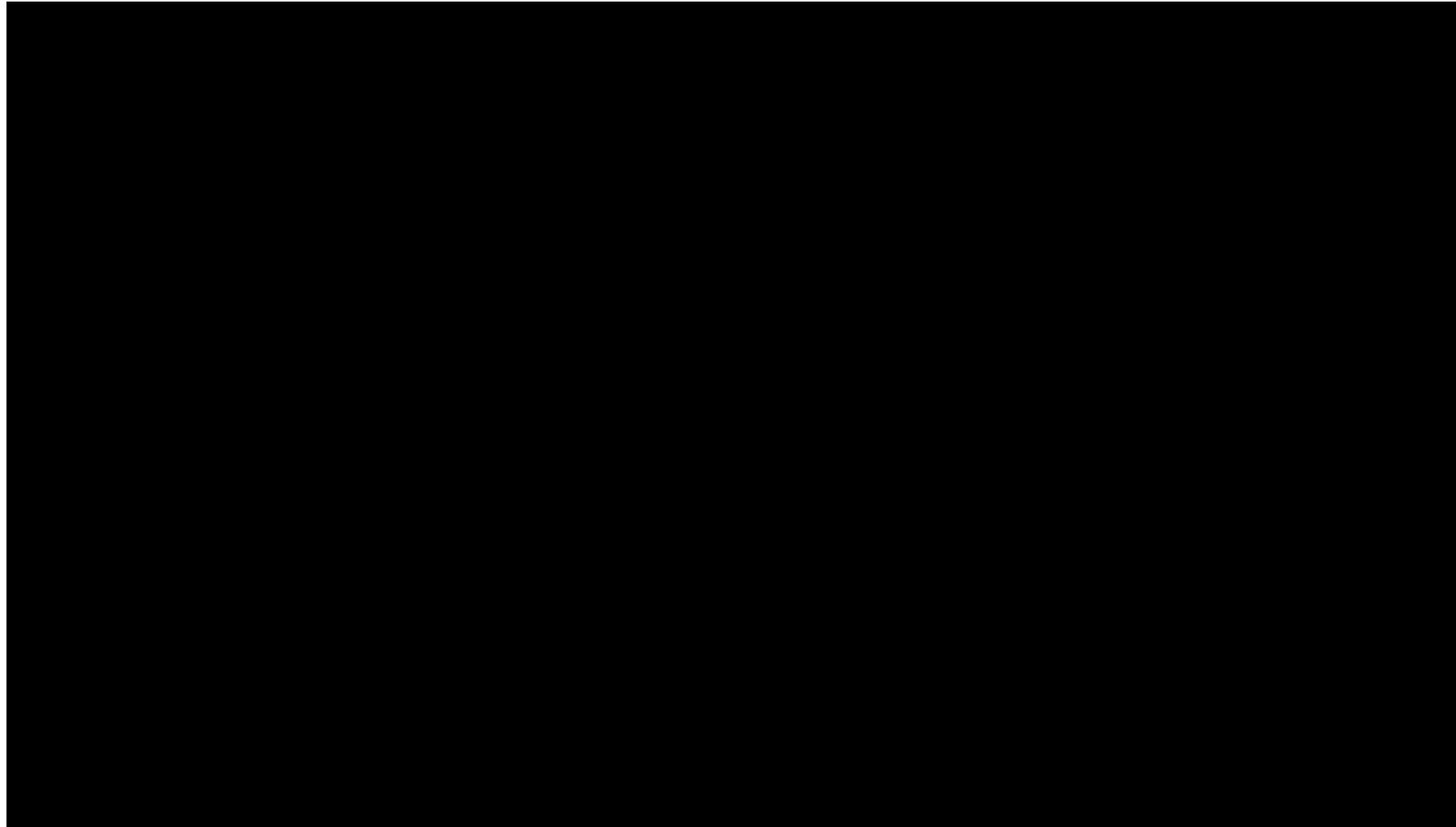
# Novel applications II: Magnetic nanostructures

**Samir Lounis**

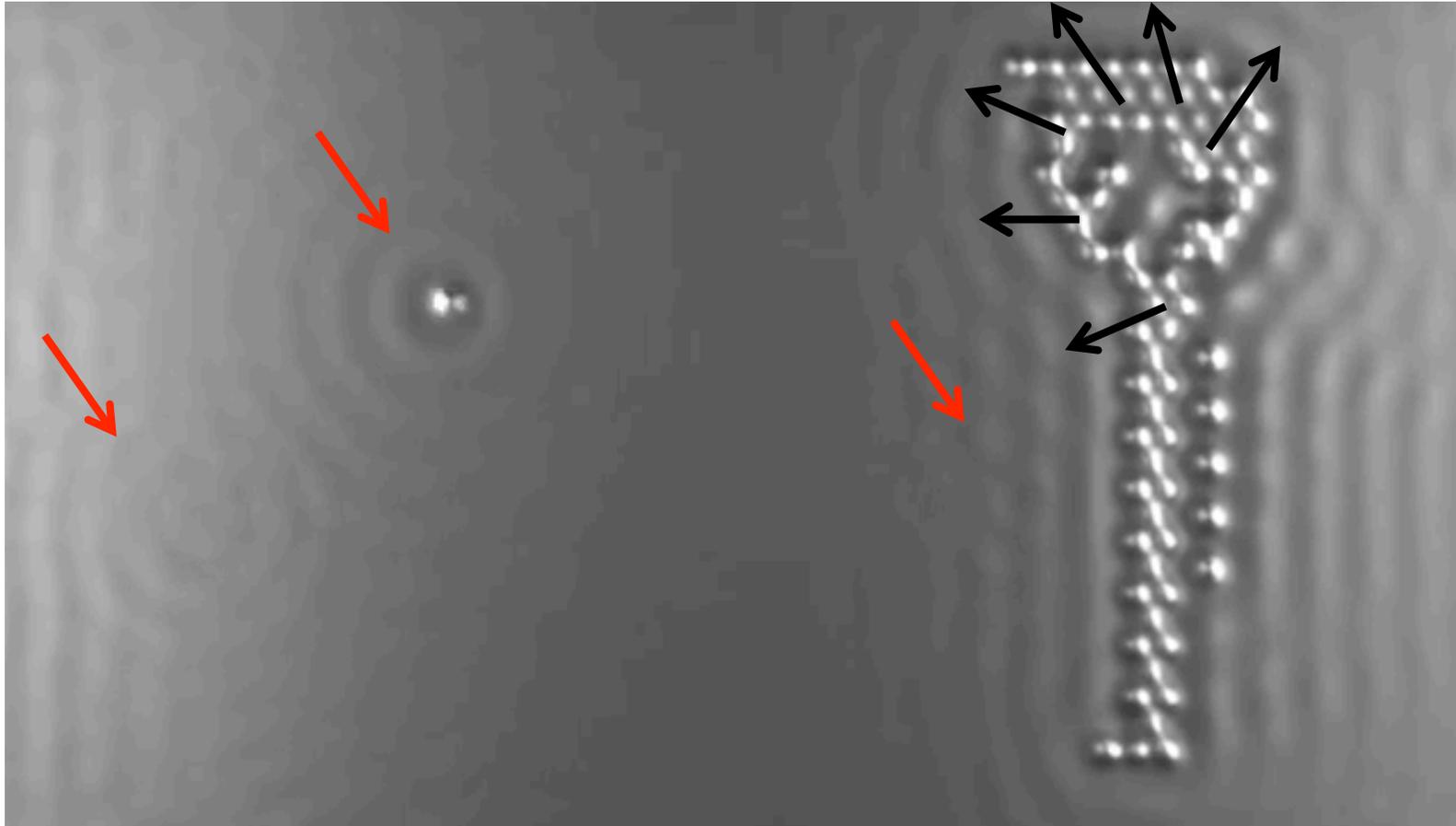
July 10, 2013

Peter Grünberg Institut & Institute for Advanced Simulation

# World's smallest movie



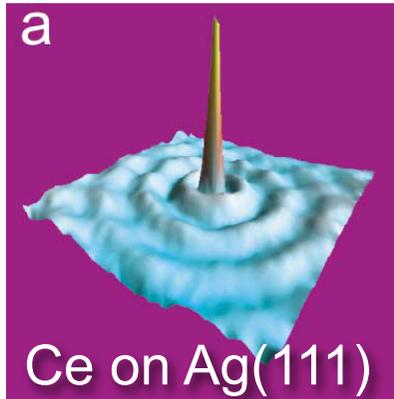
 Heinrich et al. IBM Almaden



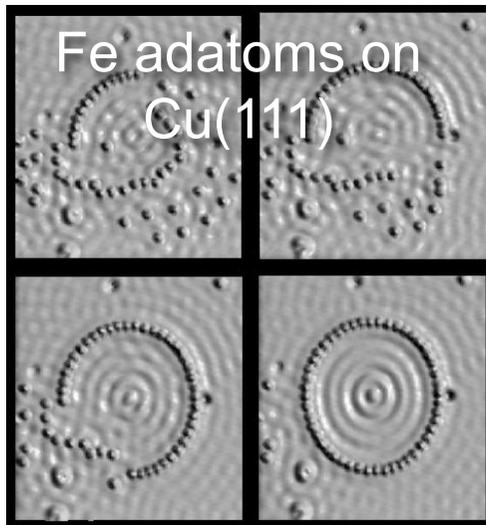
▣ Heinrich et al. IBM Almaden

$$H = -\frac{1}{2} \sum_{i \neq j} J_{ij} \vec{e}_i \cdot \vec{e}_j - \frac{1}{2} \sum_{i \neq j} D_{ij} \vec{e}_i \times \vec{e}_j - \sum_i K_i (\vec{e}_i \cdot \vec{e}_j^z)^2 - \dots$$

# Manipulation of surface states

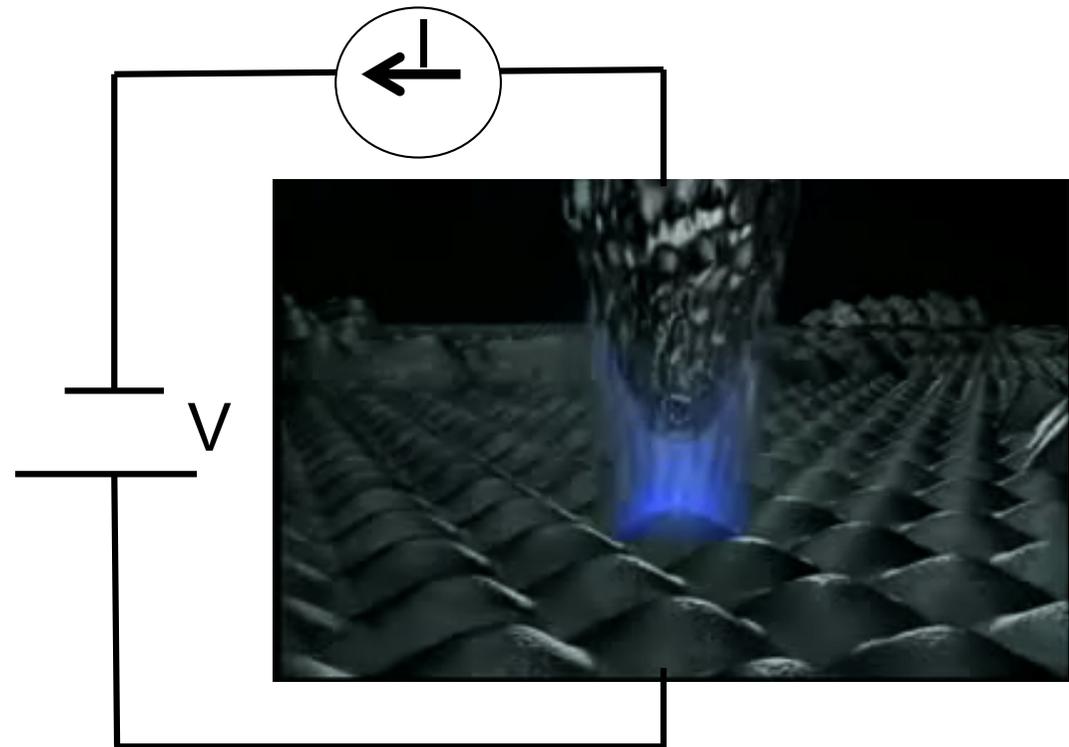


- Silly, Pivetta, Ternes, Patthey, Pelz, Schneider, PRL (2004)



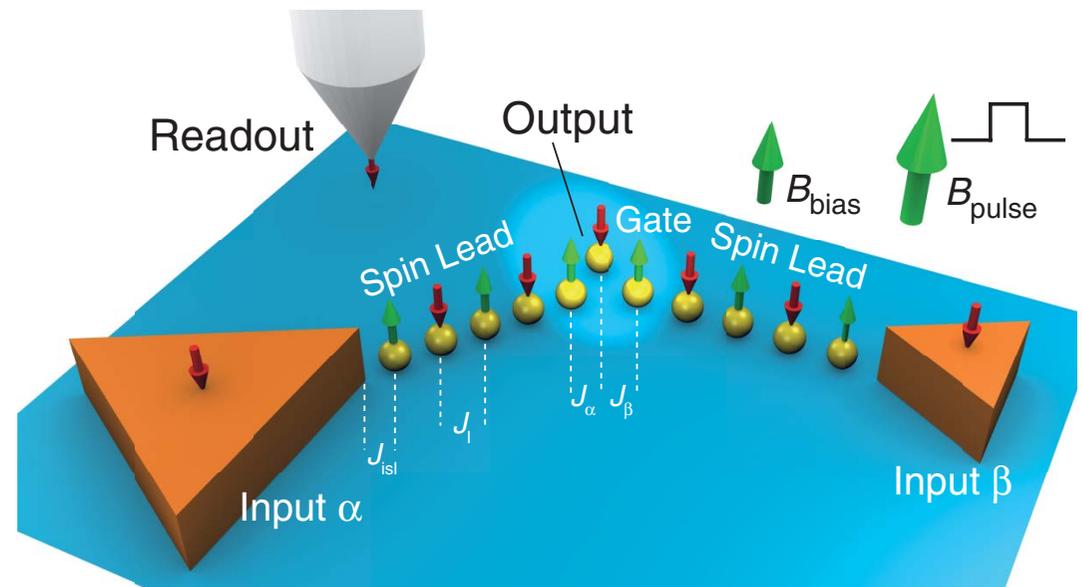
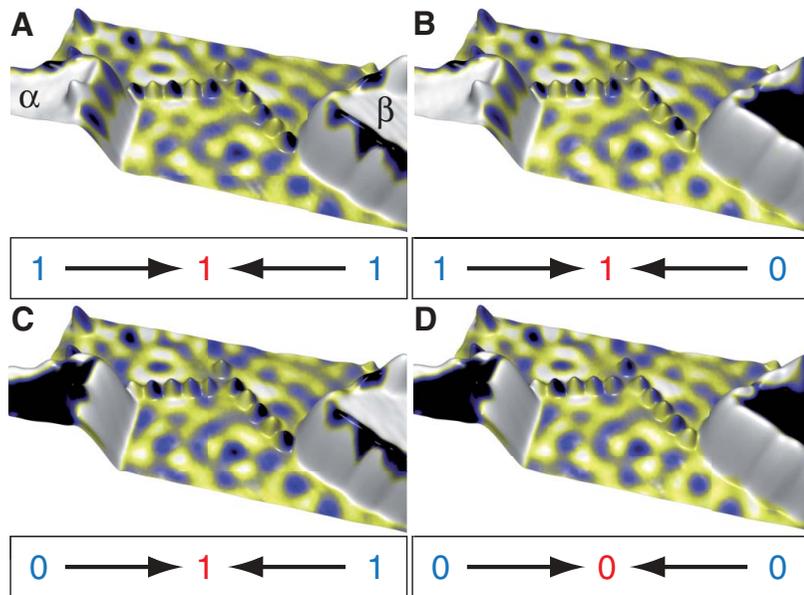
- Crommie, Lutz, Eigler, Science (1993)

July 10, 2013



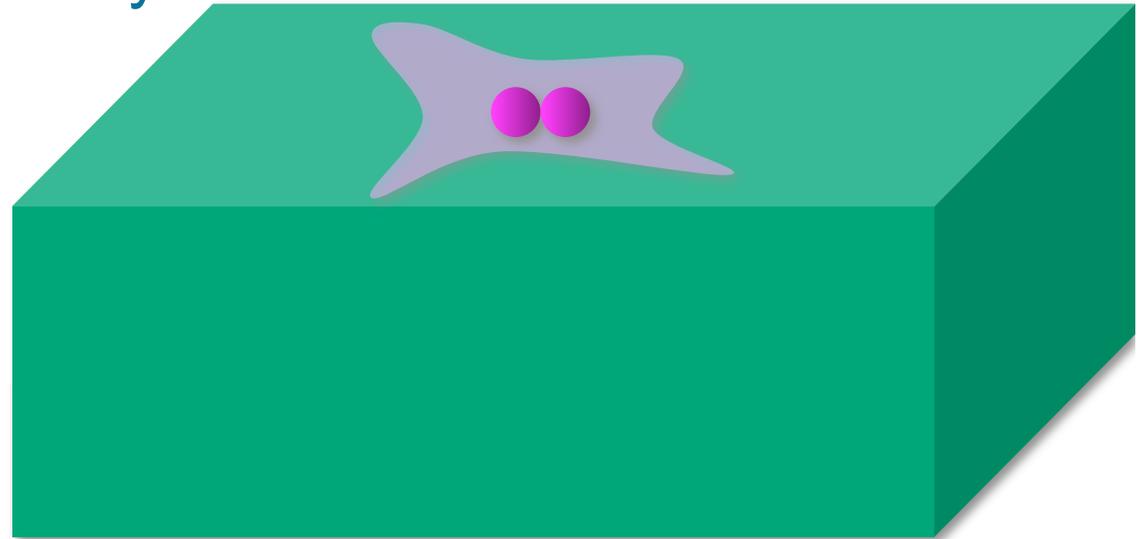
*From youtube.com: look at STM!*

# Magnetic logic gates



# KKR Green-function method within density-functional theory

Embedding the clusters  
is a non-trivial task

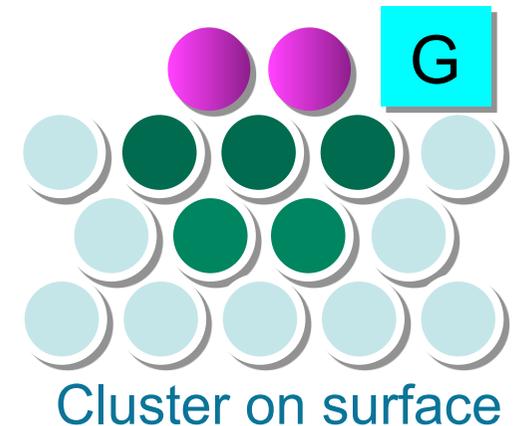
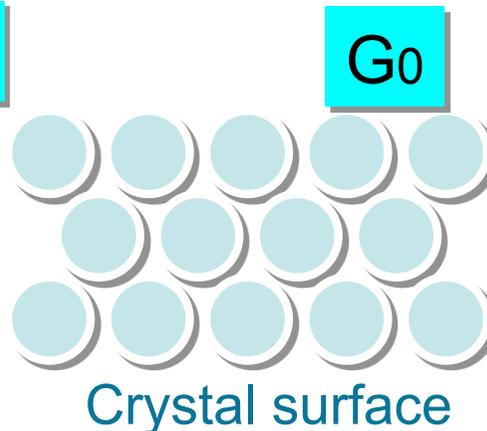


Dyson eq.: Reference system  $\rightarrow$  New system

$$G(E) = G_0(E) + G_0(E)V G(E)$$

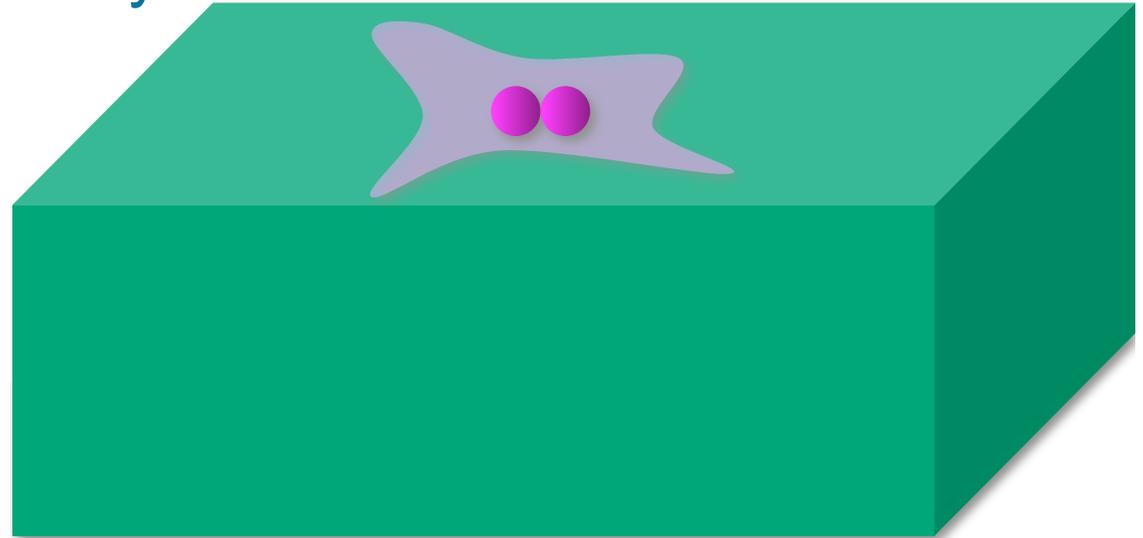
No periodic supercell needed  
Takes into account the infinite system

$$n(E) = -1/\pi \text{Im}G(E)$$



# KKR Green-function method within density-functional theory

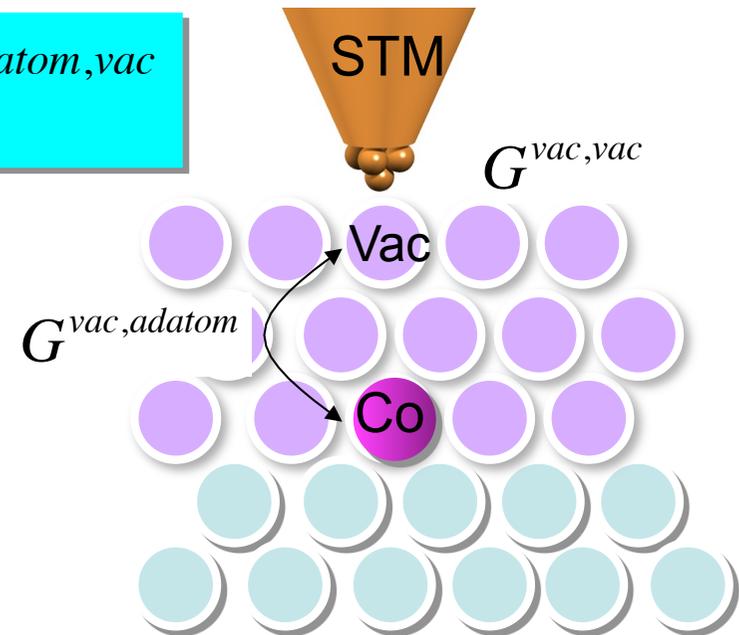
Embedding the clusters  
is a non-trivial task



$$G^{vac,vac} = G_0^{vac,vac} + G_0^{vac,adatom} V^{adatom} G^{adatom,vac}$$

Tersoff-Hammann approximation:

$$\frac{dI}{dV} \propto -\frac{1}{\pi} \text{Im} G^{vac,vac}$$



# Magnetism of single adatoms

# Appetizer: Adatoms and small clusters

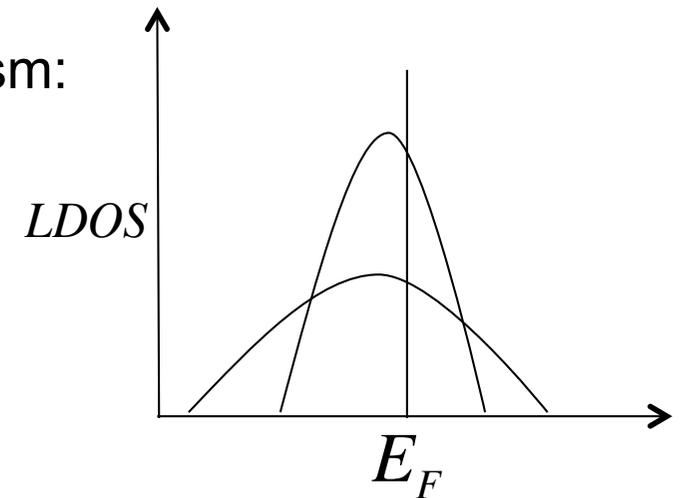
## Transition from atomic to monolayer & bulk behaviour

Stoner model & Stoner criterion for ferromagnetism:

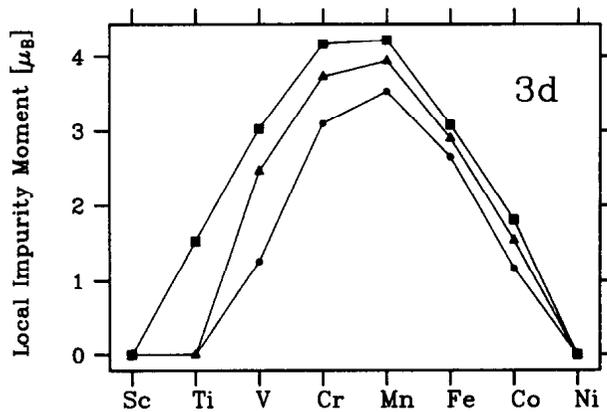
$$\delta M = \chi \delta B$$

$$In^0(E_F) > 1$$

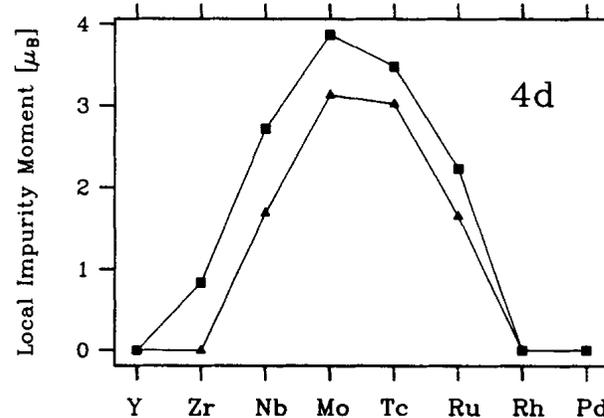
$$\chi = \frac{1}{1 - In^0(E_F)} n^0(E_F)$$



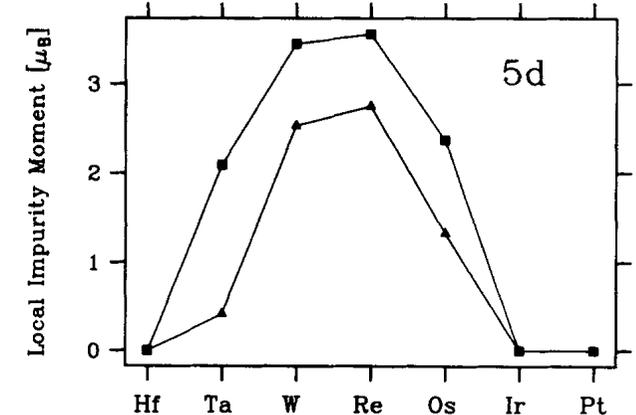
3d atoms/Cu(001)



4d atoms/Ag(001)



5d atoms/Ag(001)

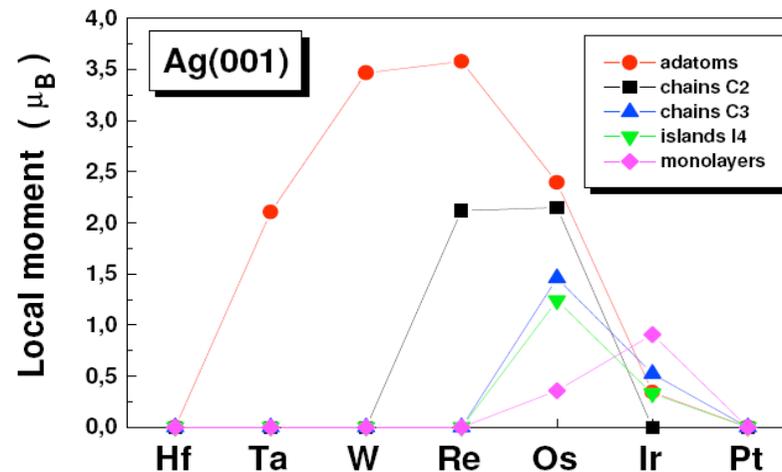
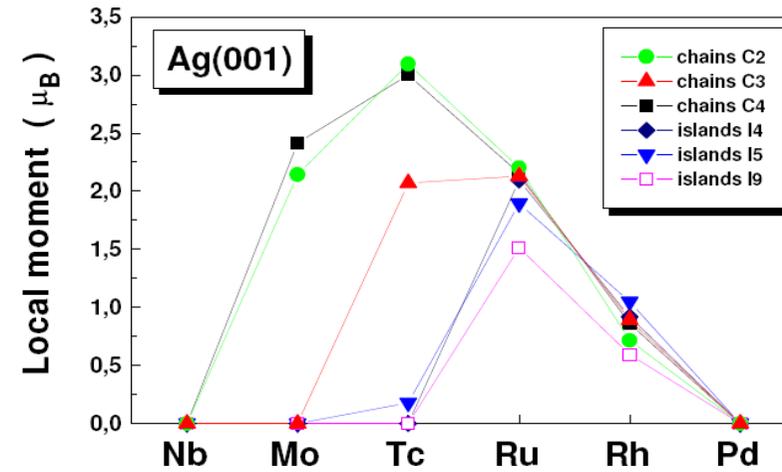
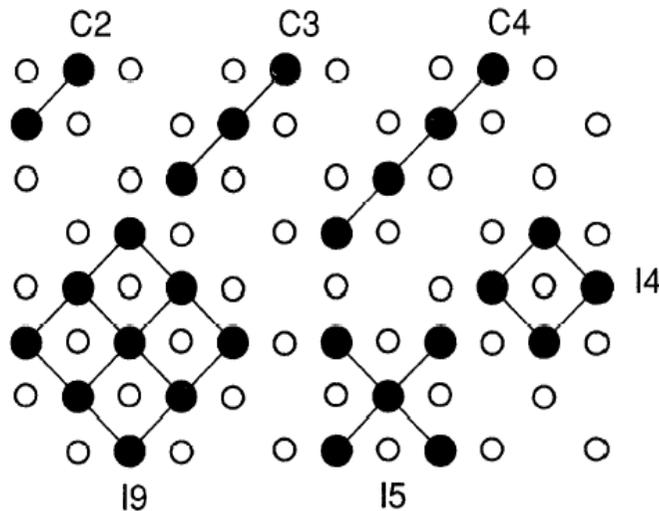


# Transition from atomic to monolayer & bulk behaviour

Spin moments: 4d & 5d on Ag(001), shape & size dependence

Dependence on:

- Size
- Shape
- Interactions:
  - Intra-cluster
  - Cluster-substrate





# Nanowires & magnetic frustration

# Non-collinear magnetism

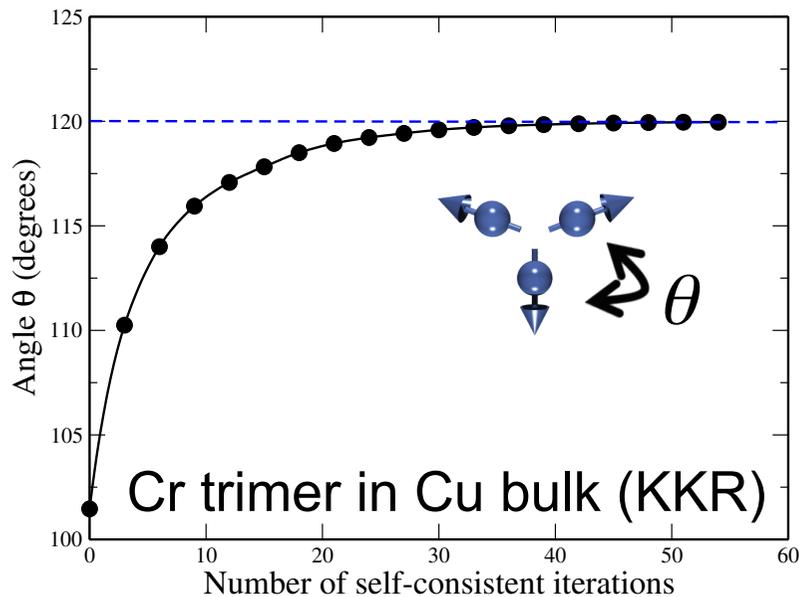
Classical Heisenberg Hamiltonian:

$$H = -\frac{1}{2} \sum_{i \neq j} J_{ij} \vec{e}_i \cdot \vec{e}_j$$

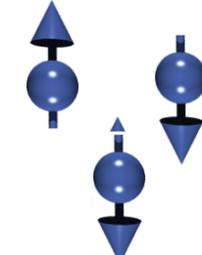
Driving mechanism:

Competing interactions:

Ferromagnetism or antiferromagnetism

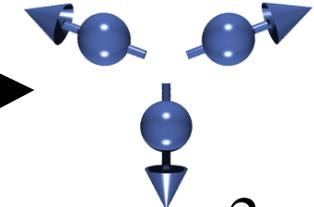


**Competing AF interactions**



$H_{col} = -|J|$

**Non-collinear compromise!**



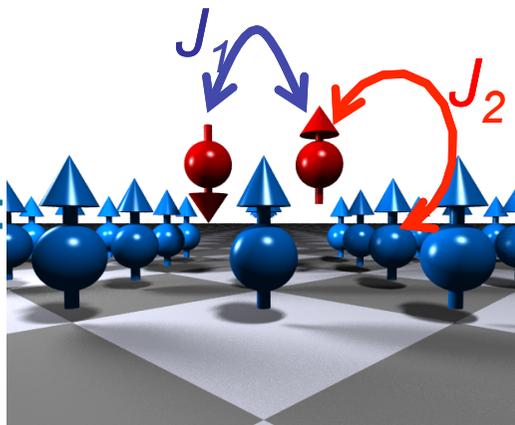
$H_{ncol} = -\frac{3}{2}|J|$

Mn or Cr atoms couple AF

# Non-collinear magnetism:

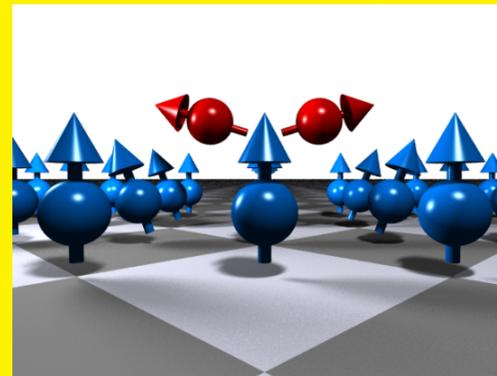
Mn on Ni(001)

collinear result:  
frustrated



$$H(\text{ferri}) = J_1$$

Total  $E$  minimum ( $-13\text{meV}$ )

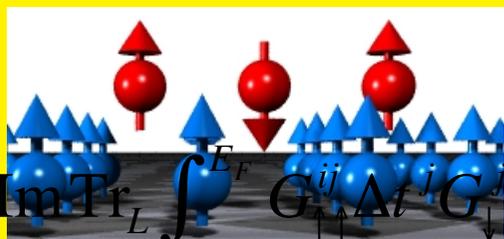


$\theta = 72.5^\circ$

$$H(\text{ncol}) = -J_1 \cos(2\theta) - J_2 \cos(\theta)$$

Total  $E$  minimum ( $-9\text{meV}$ )

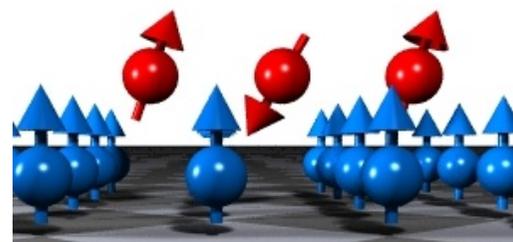
col



$$J_{ij} = \frac{1}{4\pi} \text{Im Tr}_L \int^{E_F} G_{\uparrow\uparrow}^{ij} \Delta t^i G_{\downarrow\downarrow}^{ji} \Delta t^j$$

$$J_1 = J(\text{Mn-Mn}) = 136 \text{ meV}$$

$$J_2 = J(\text{Mn-Ni}) = 4 \times 13 \text{ meV}$$

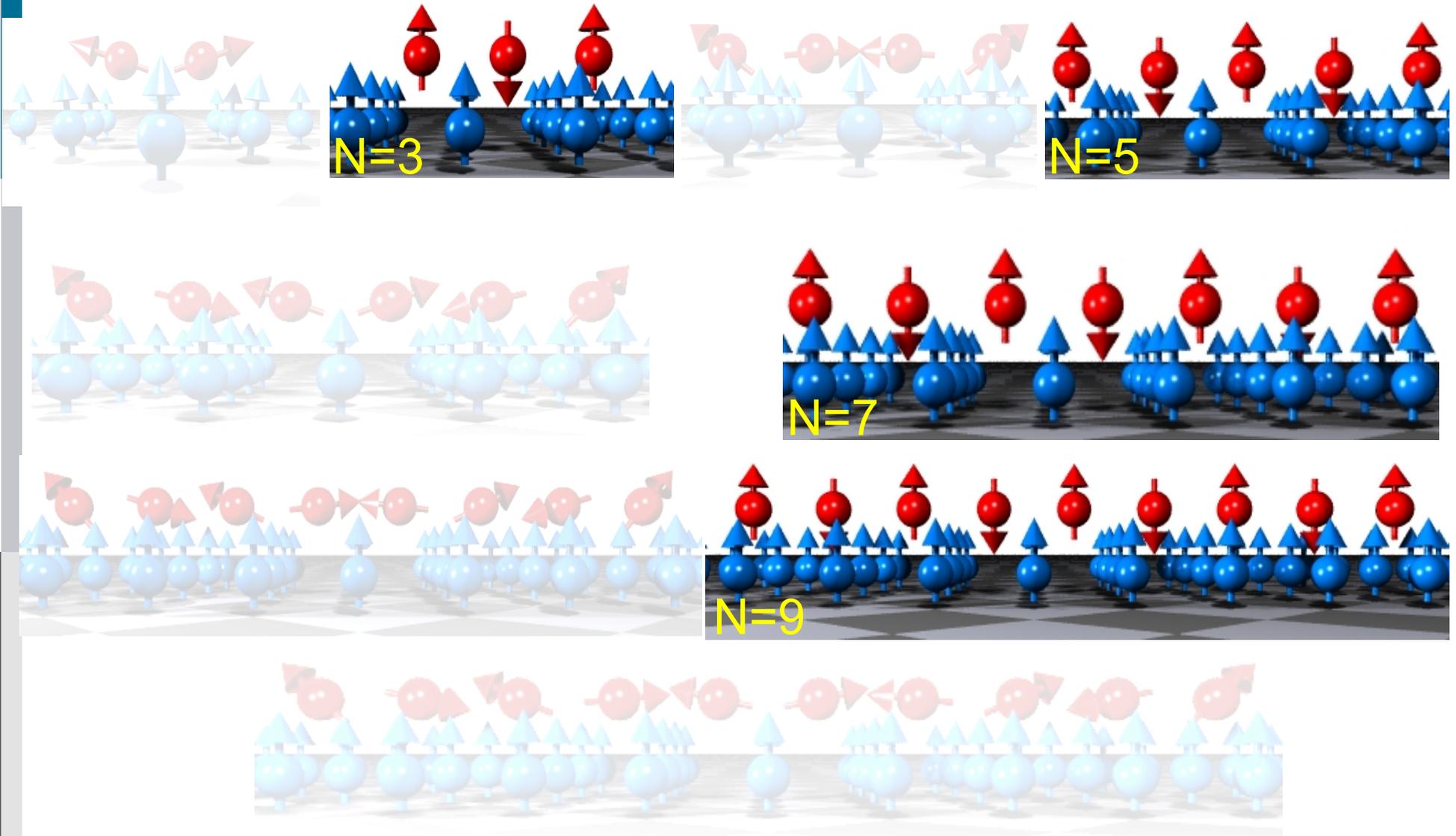


ncol

$$H(\text{ncol}) = -2J_1 \cos(\alpha) - J_2 \cos(\theta)$$

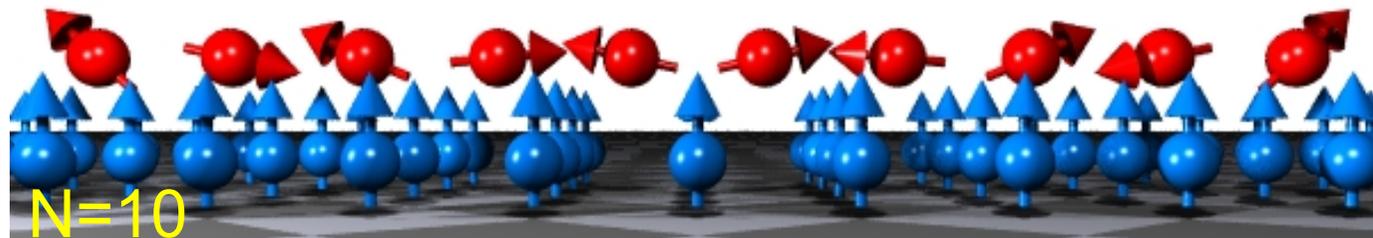
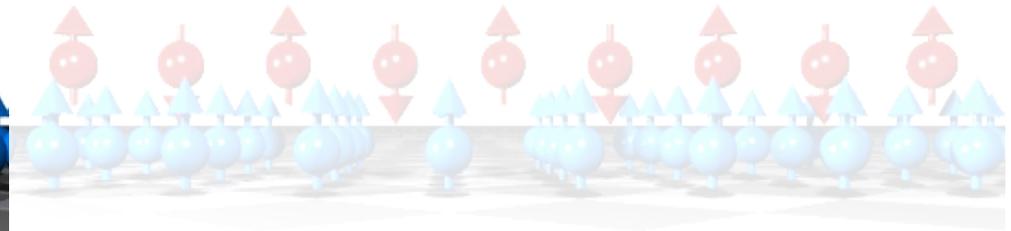
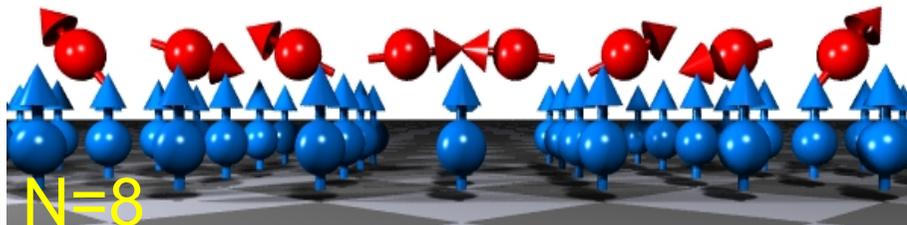
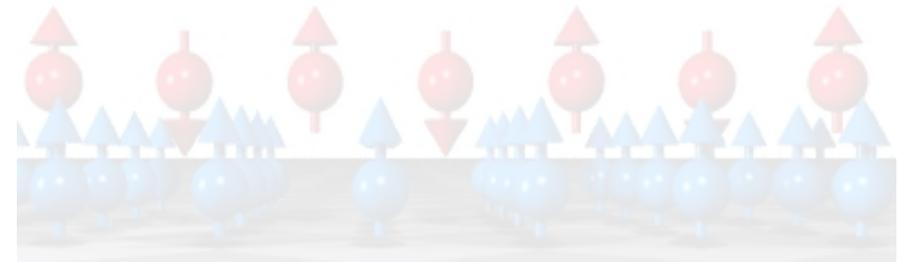
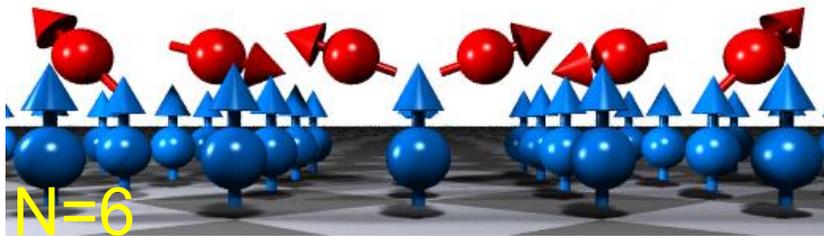
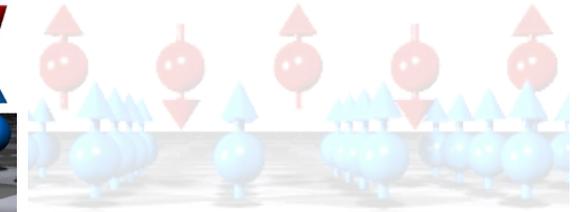
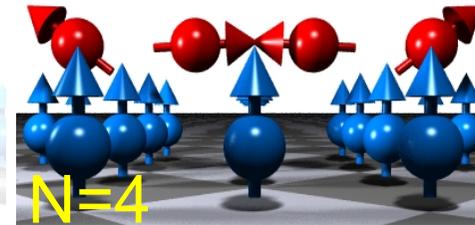
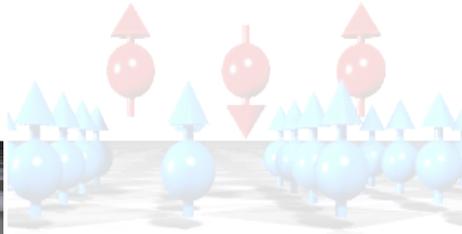
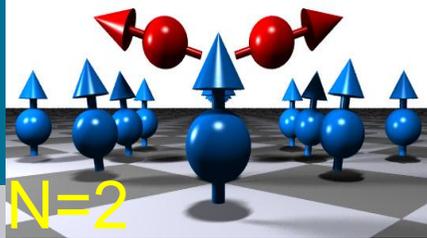
# Odd numbered wires

odd = anti-parallel



# Even-numbered wires: Frustration

even = non-collinear

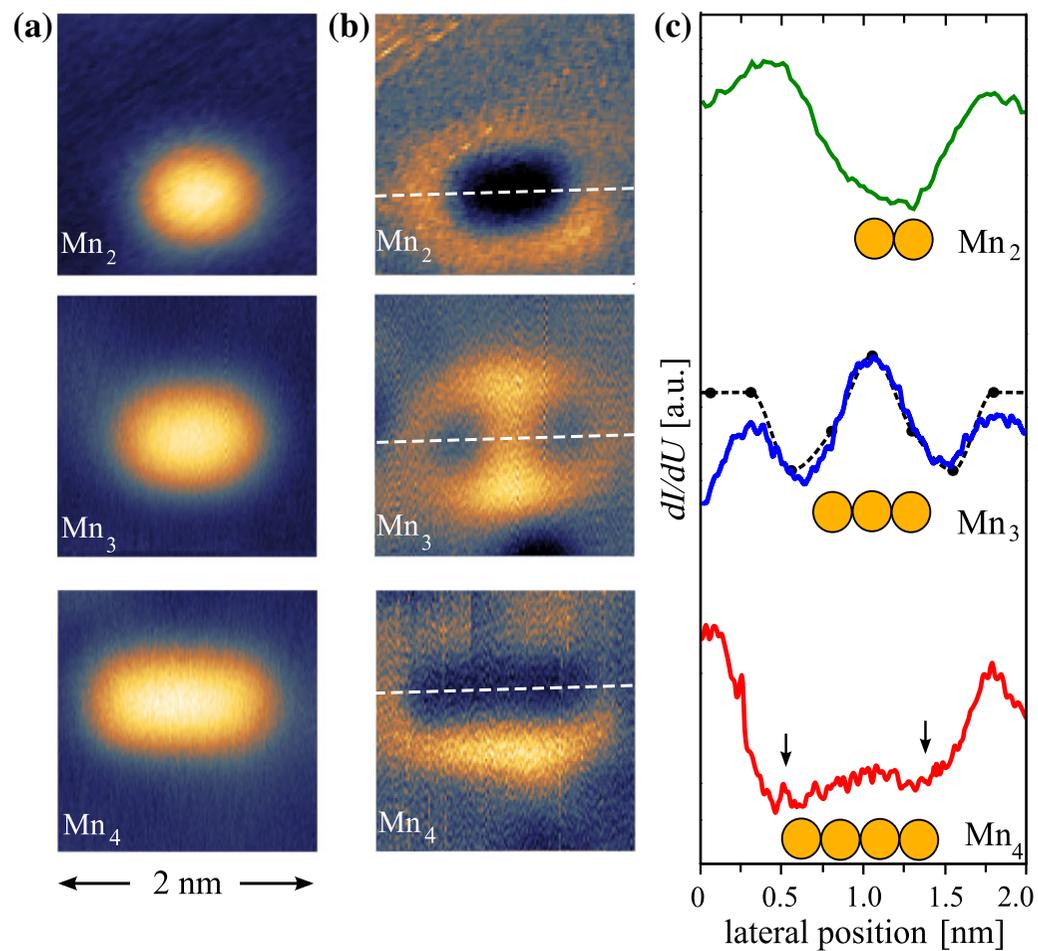


# Domino effect in nanowires



*From youtube.com: look at Domino*

# Experiment: Mn wires/Ni(110)





# **Magnetic crystalline anisotropy energy (MAE)**

# XMCD measurements on MAE of Co adatoms/Pt(111)

$$H = -\frac{1}{2} \sum_{i \neq j} J_{ij} \vec{e}_i \cdot \vec{e}_j - \sum_i K_i (\vec{e}_i \cdot \vec{e}_j^z)^2$$

$$\sum_i K_i = H_x - H_z$$

A	n	S	L	$\Delta L_{x-z}$	$K_{x-z}$
	1	2.14	0.60 (1.50)	-0.25	+18.45
	2	2.11	0.38 (0.74)	-0.11	+4.11
	3 chain	2.08	0.34 (0.67)	-0.06	+3.69
	3 triangle	2.10	0.25 (0.43)	-0.05	+2.22
	4	2.08	0.22 (0.33)	-0.01	+0.75
	5	2.08	0.27 (0.45)	-0.09	+1.81

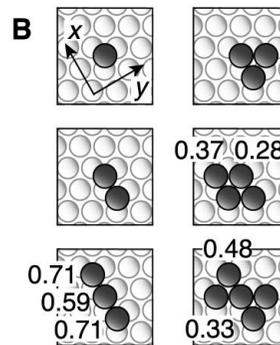
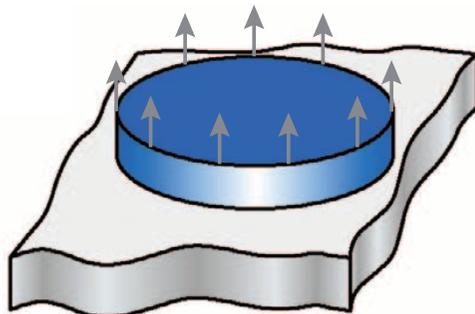
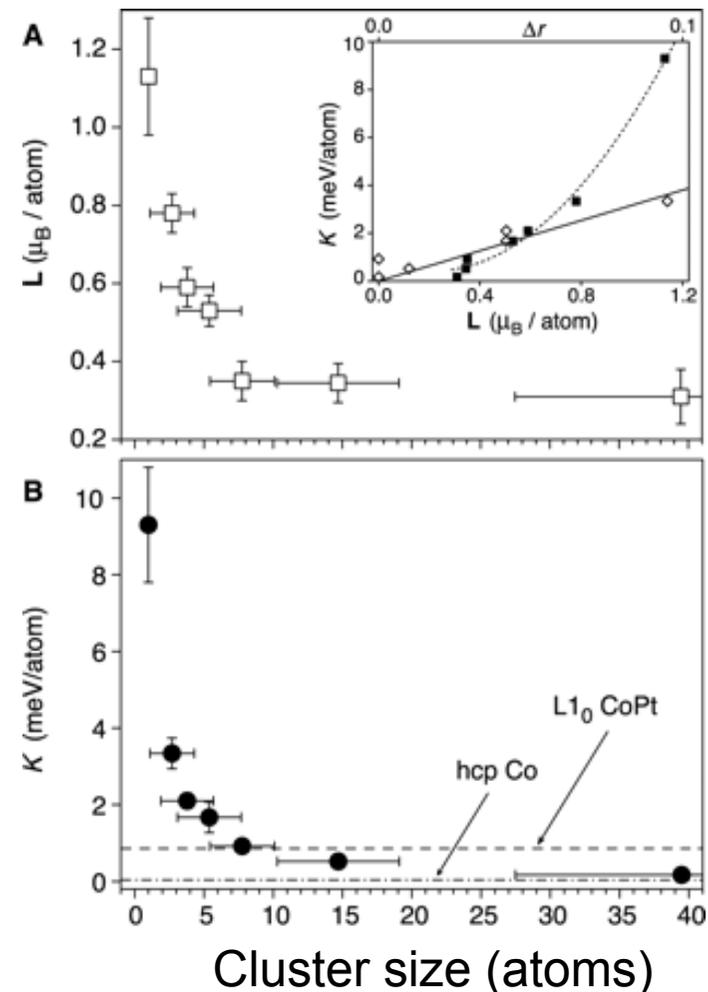
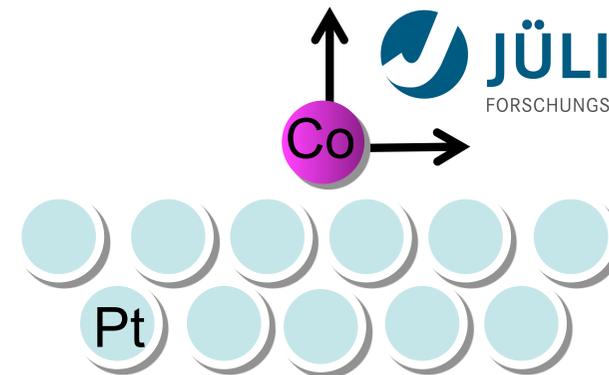


Fig. 4. (A) Values of S, L,  $\Delta L$  ( $\mu_B$ ), and K (meV) per Co atom calculated by the SPR-KKR method for Co particles on Pt(111) as shown in (B). The values of L in parentheses have been computed within the OP scheme with a 50% reduced Racah parameter. (B) Hard-sphere representation of the Co particles considered in the theoretical calculations. The labels indicate the OP values of L for nonequivalent Co sites. S, L,  $\Delta L$ , and K in (A) are averaged over all Co sites.

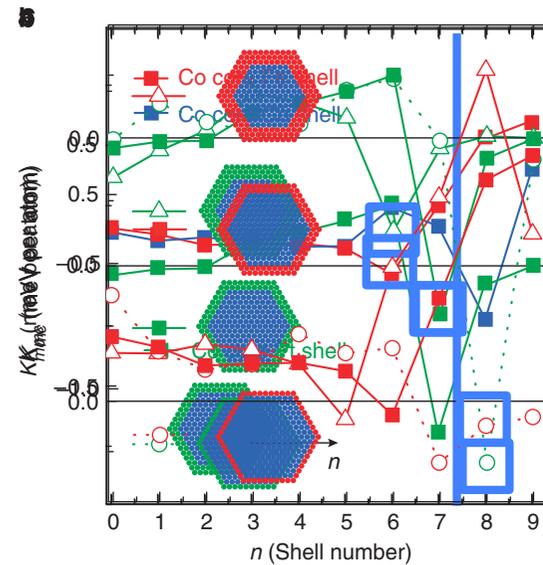
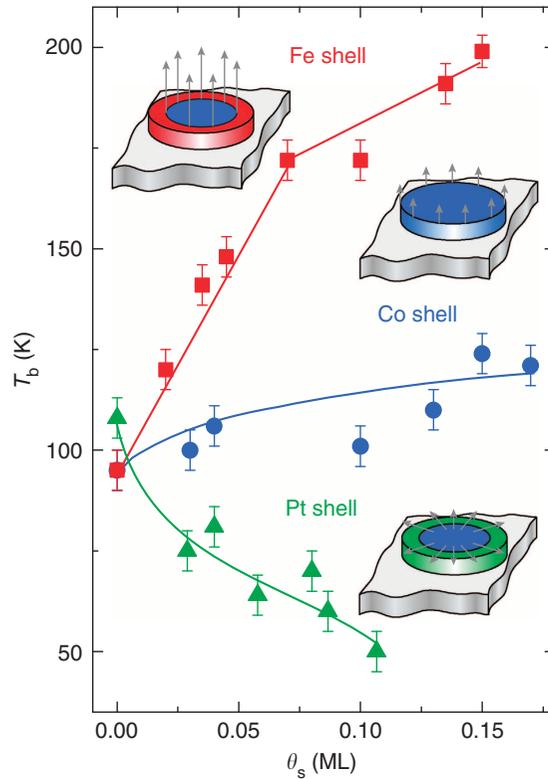


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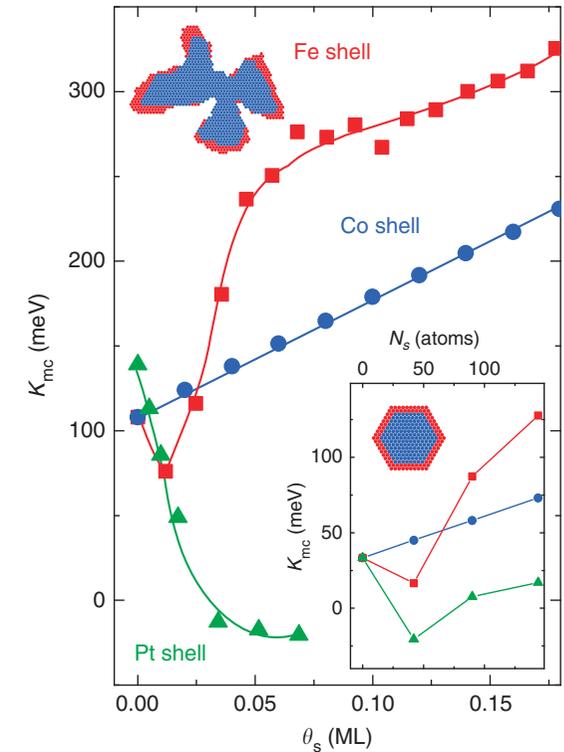


# Engineering of MAE of nanostructures

Blocking temperature is related to MAE



Calculated MAE for experimental island sizes and shapes.

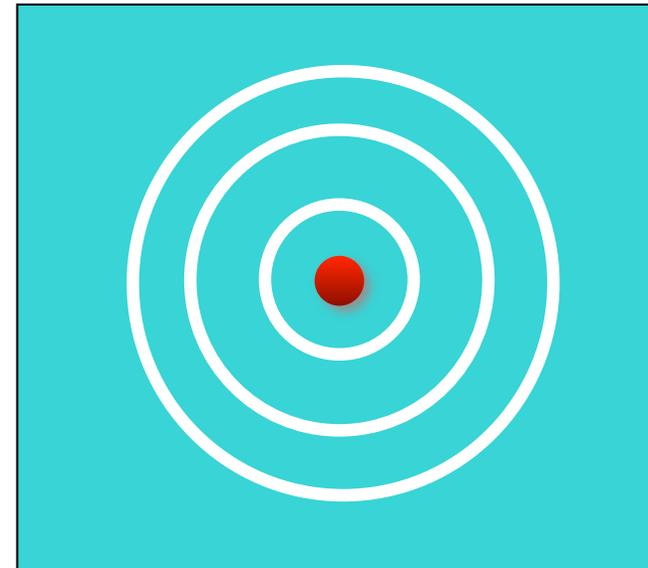




# Friedel oscillations & confinement



Stone in water



$$\text{3D jellium } \Delta n(r) \propto \frac{\cos(2k_F r)}{r^3}$$

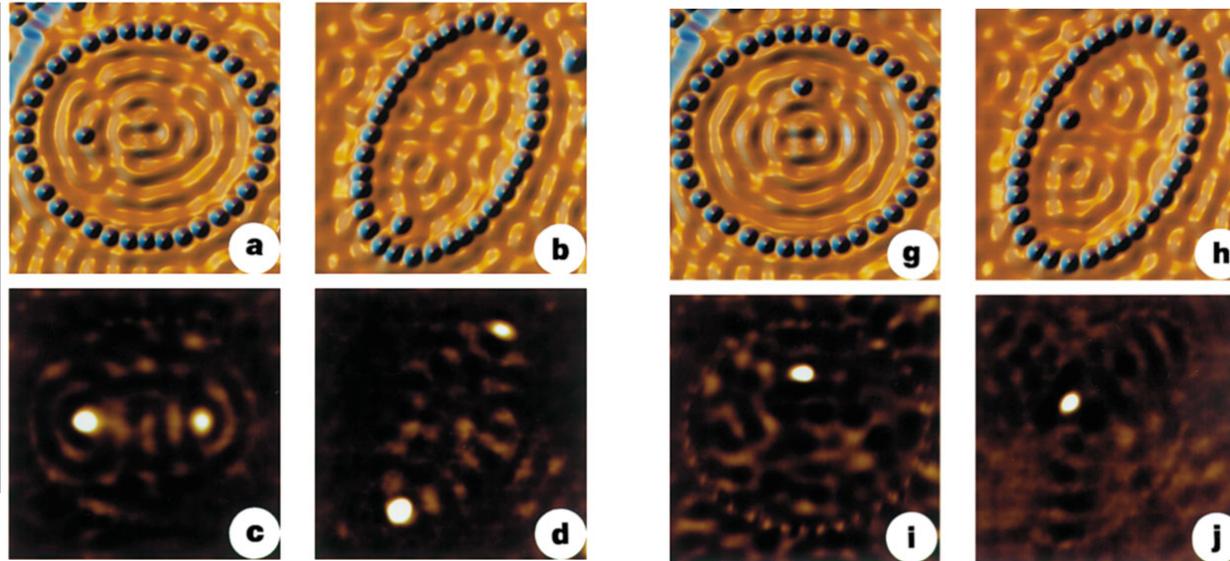
$$\text{2D jellium } \Delta n(r) \propto \frac{\cos(2k_F r)}{r^2}$$

# Quantum Corals & Quantum Mirage

Atom at focal point; mirage at second focal point!

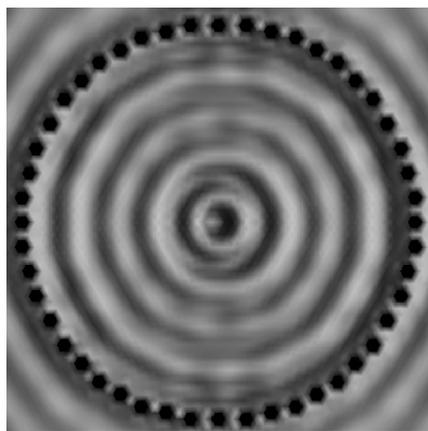
STM image:  
Co corral  
on Cu(111)

Significant  
role of  
surface state



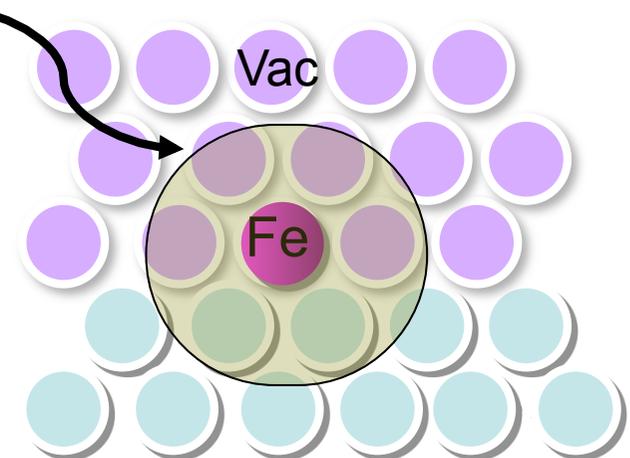
Manoharan, Lutz, and Eigler, Nature (2000)

Related *ab-initio* calculations:



1-Self-consistent calculations

Side view



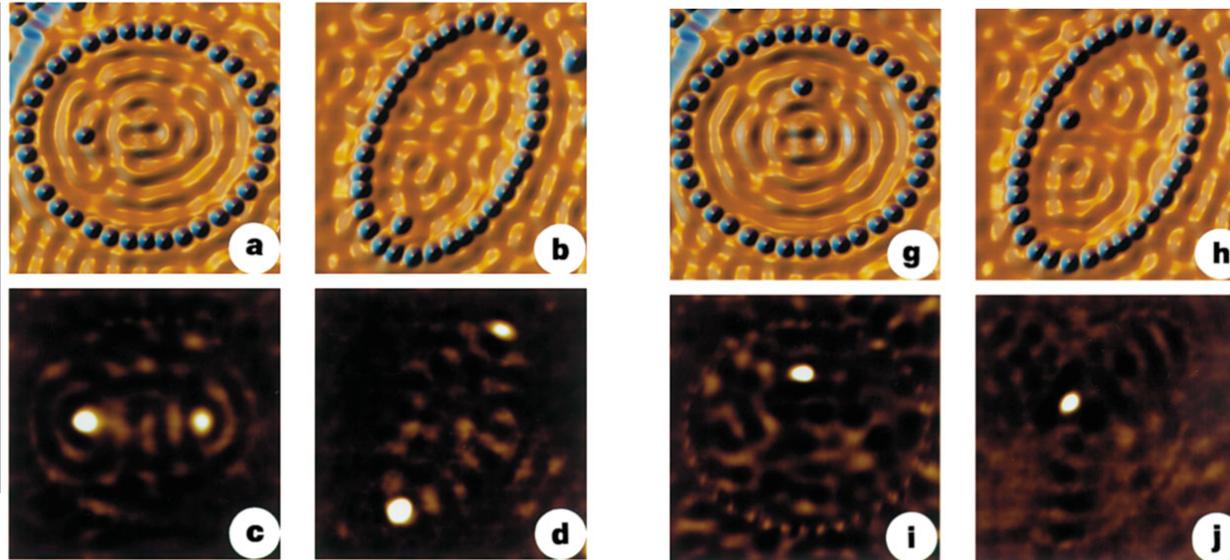
Lazarovits, Ujfalussy, Szunyogh,  
Gyorffy, Weinberger, J.Phys. Cond. Matt. (2005)

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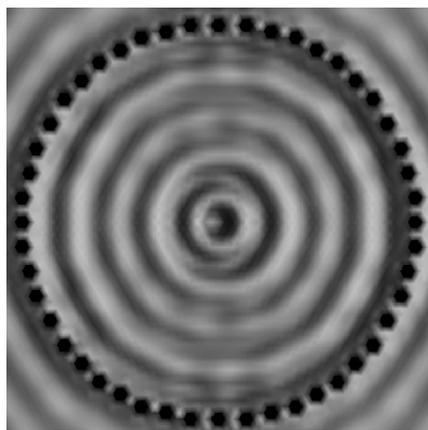
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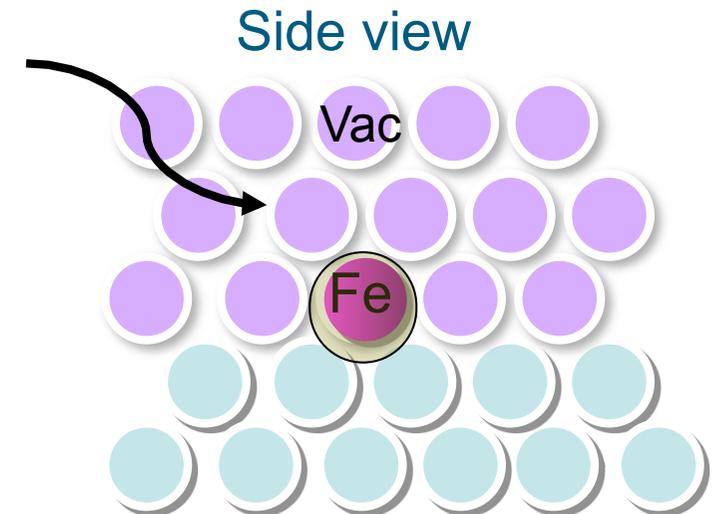


Manoharan, Lutz, and Eigler, Nature (2000)

Related *ab-initio* calculations:



2-Use of potential of  
single Fe atoms



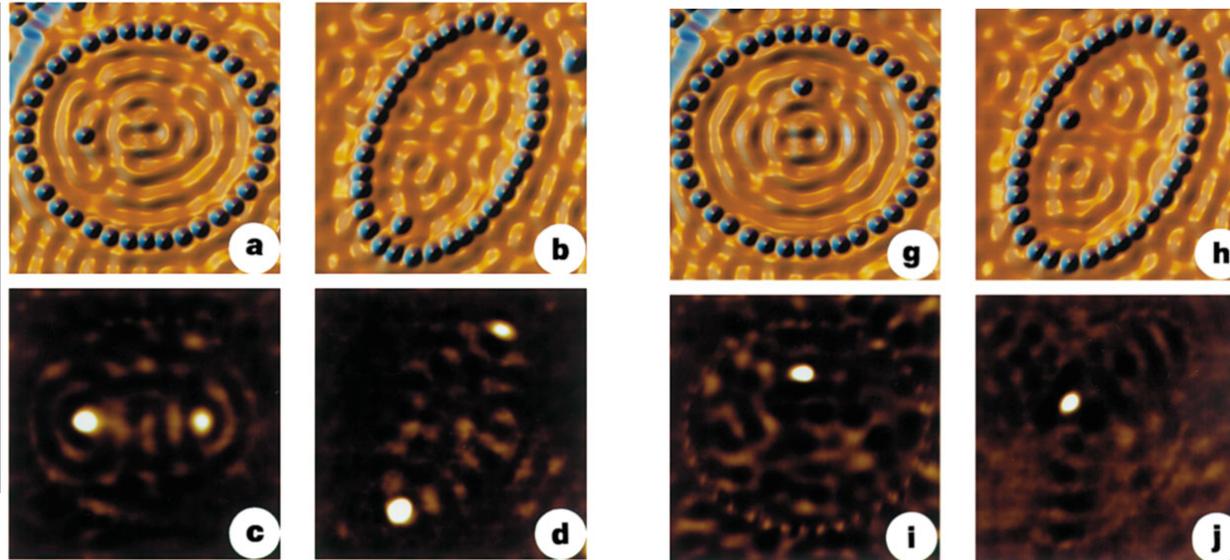
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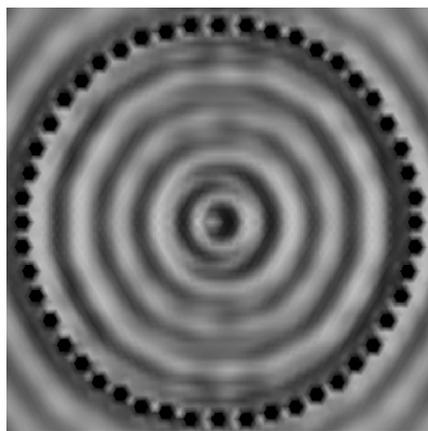
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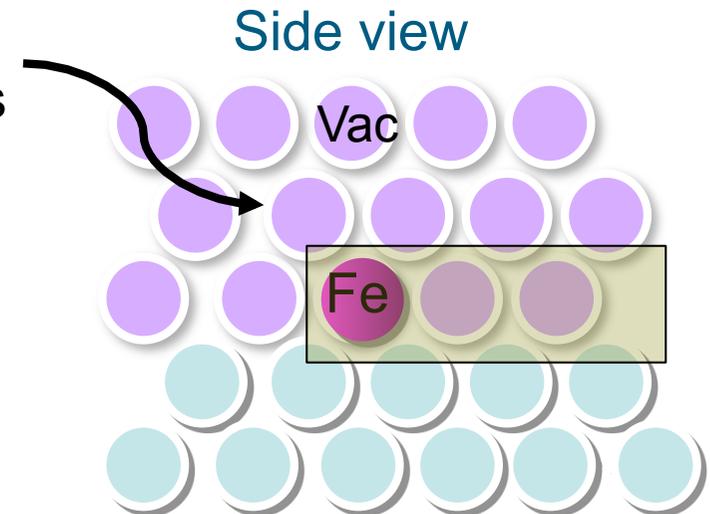


Manoharan, Lutz, and Eigler, Nature (2000)

Related *ab-initio* calculations:



3-Solve the Dyson eq.  
for corral + vacuum sites



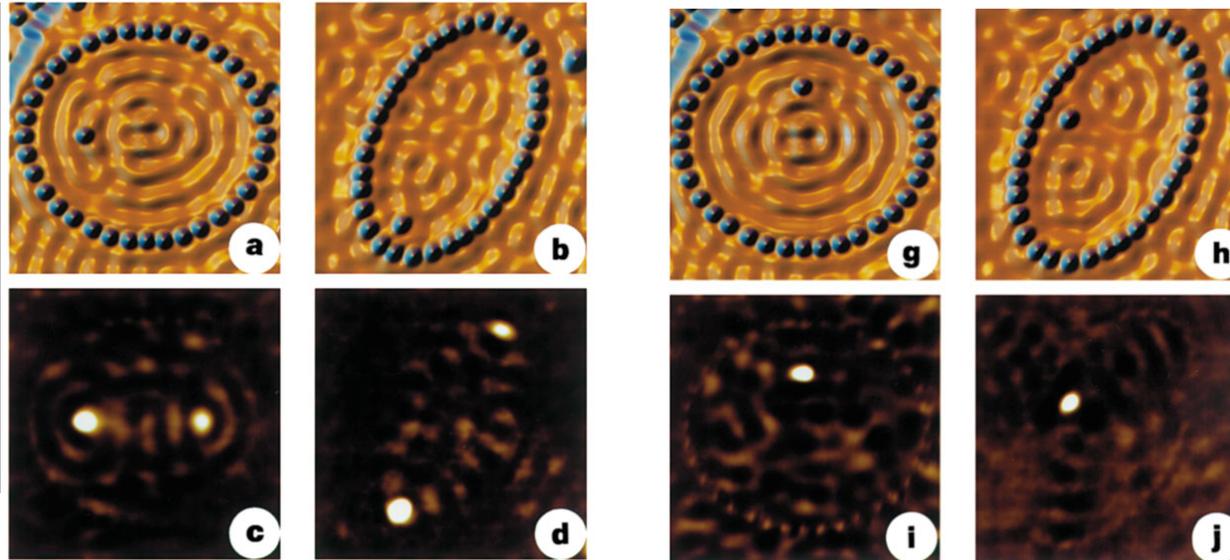
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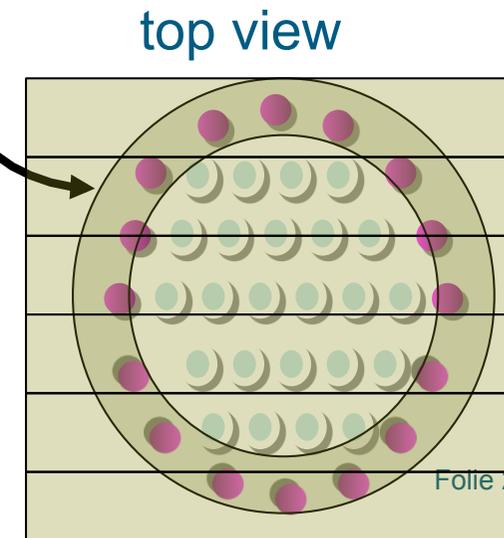
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Manoharan, Lutz, and Eigler, Nature (2000)

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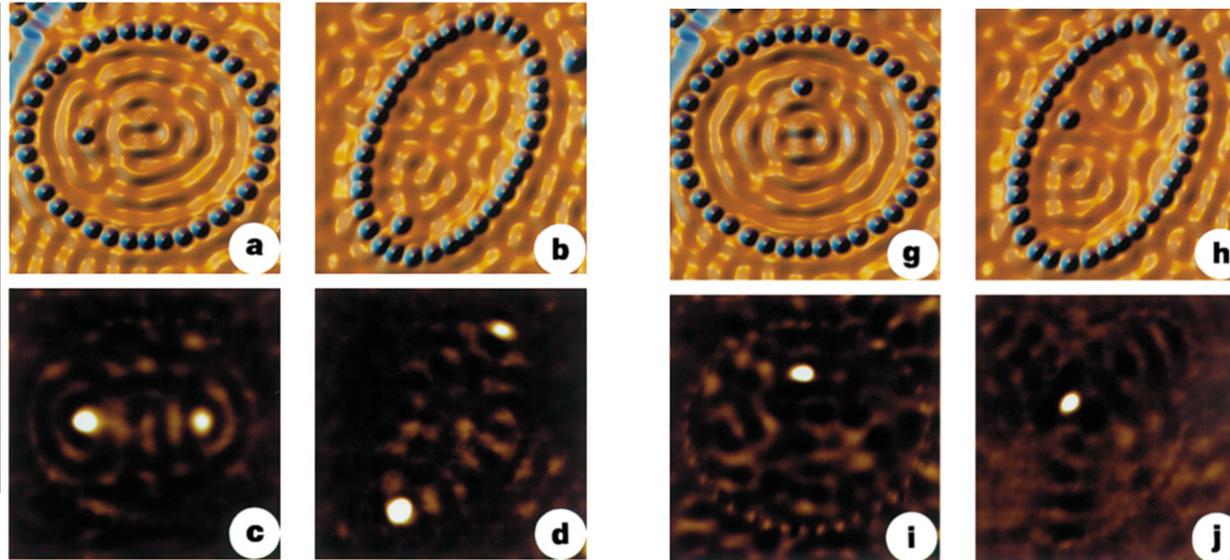
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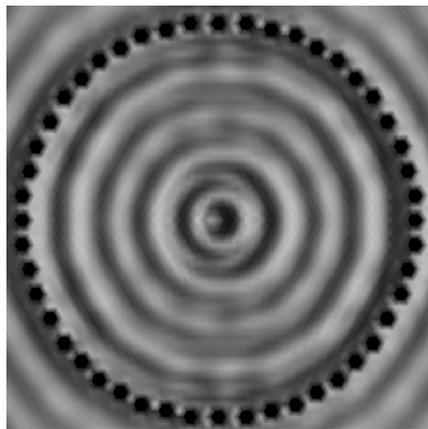
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Manoharan, Lutz, and Eigler, Nature (2000)

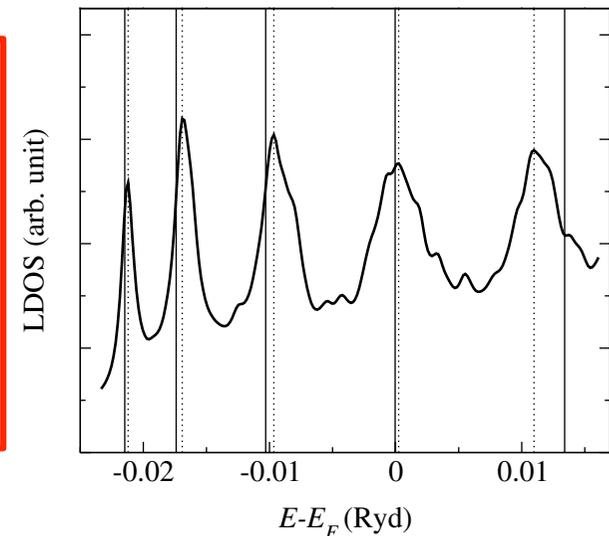
Related *ab-initio* calculations:



Circular quantum well model

$$V(\vec{r}) = \begin{cases} 0 & \text{if } r < R \\ +\infty & \text{if } r \geq R \end{cases}$$

Solutions are besse  
l functions of the first kind



Center of quantum coralls

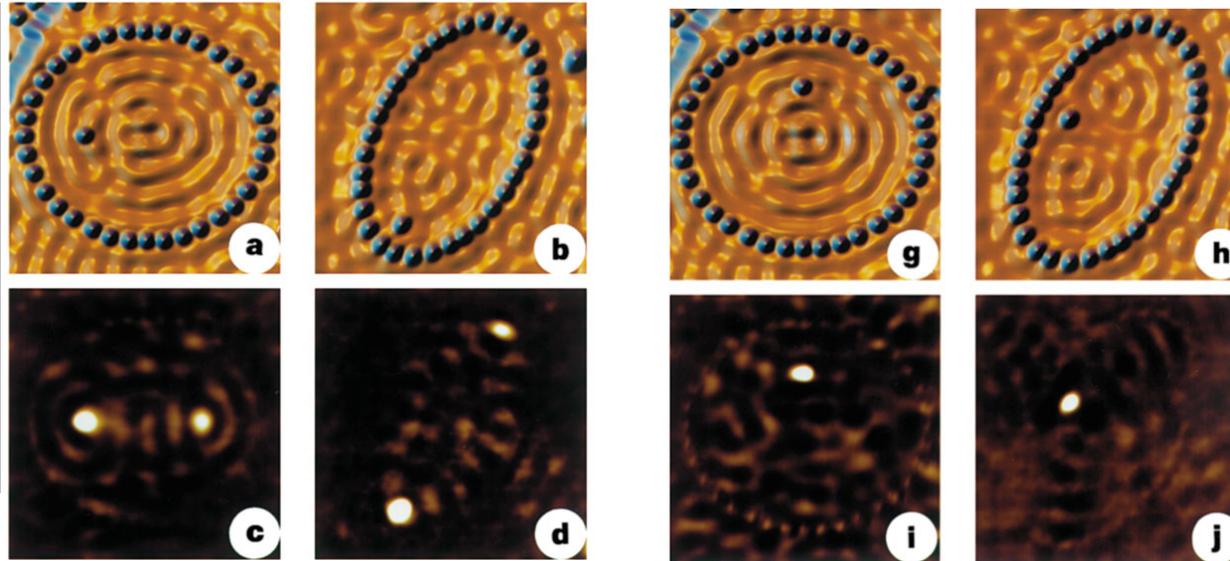
Lazarovits, Ujfalussy, Szunyogh,  
Gyorffy, Weinberger, J.Phys. Cond. Matt. (2005)

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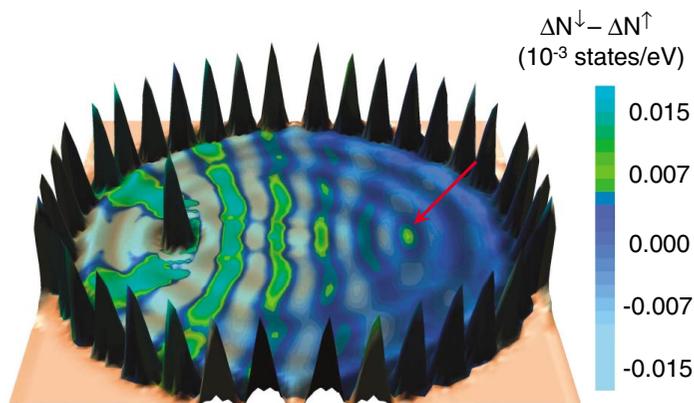
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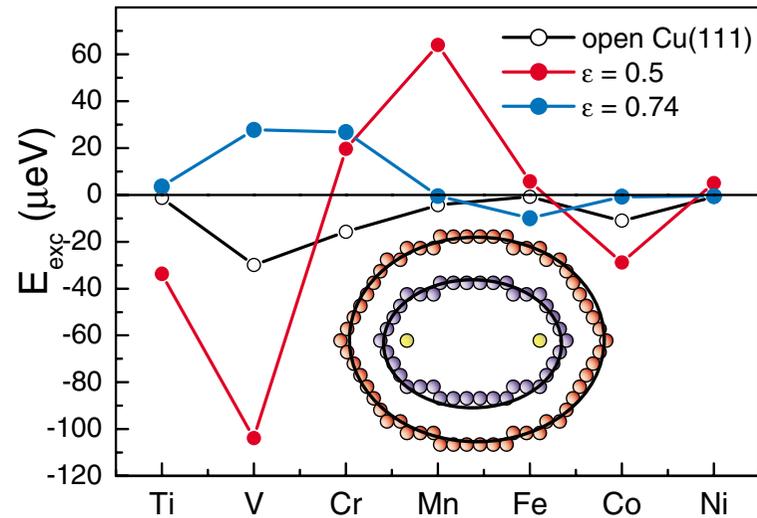


Manoharan, Lutz, and Eigler, Nature (2000)

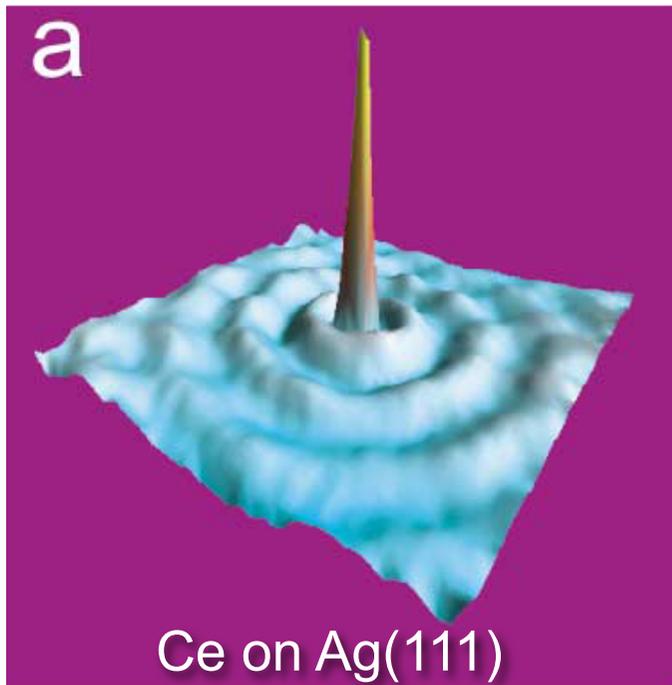
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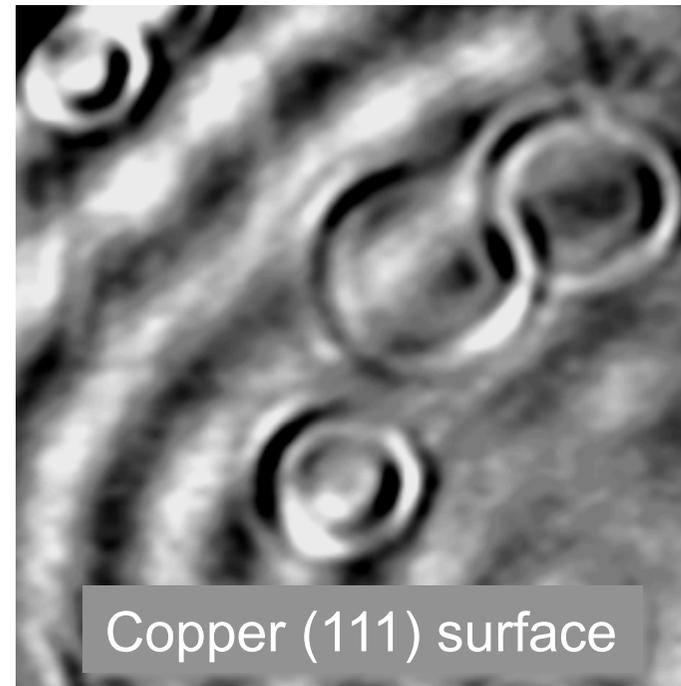
Stepanyuk, Niebergall,  
Hergert, Bruno, PRL (2005)



# Electron distribution induced by adatoms or buried atoms



Silly et al., PRL 92, 16101 (2004)



STM picture by  
A. Weismann, M. Wenderoth, R.G. Ulbrich  
University of Göttingen

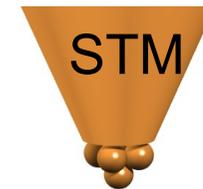
# Method

Tersoff-Hamann  
Model:

$$I(\vec{r}_{\parallel}, z, V) \propto n_T \int_{E_F}^{E_F + eV} n(\vec{r}_{\parallel}, z, \epsilon) d\epsilon$$

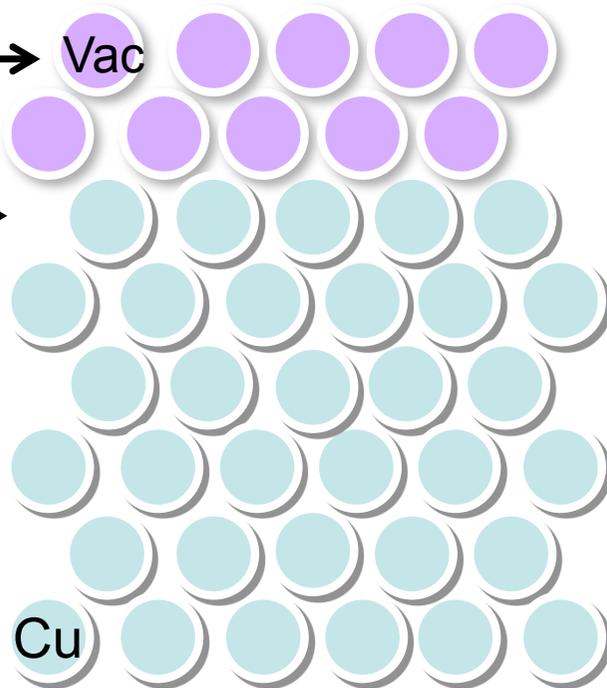
$$G(E) = G^0(E) + G^0(E)V G(E)$$

~ few 1000 sites

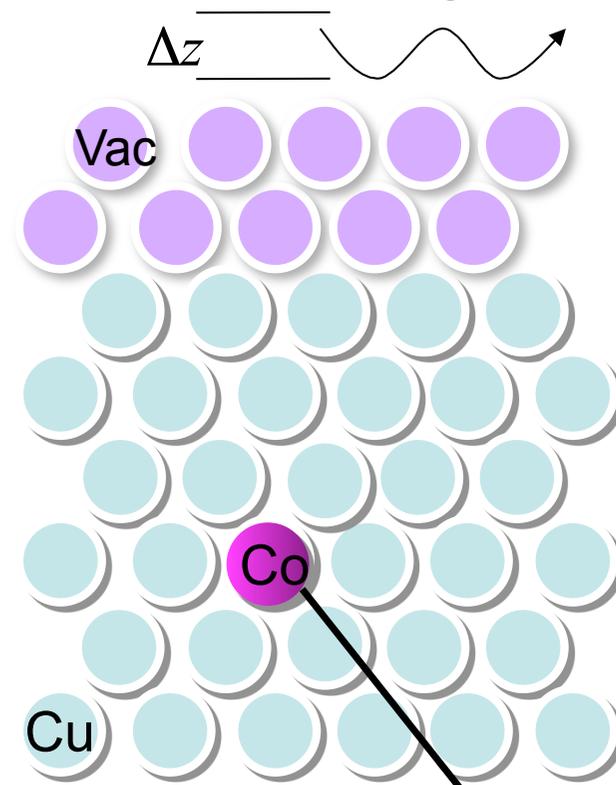


STS

Surface



$G^0$



$G$

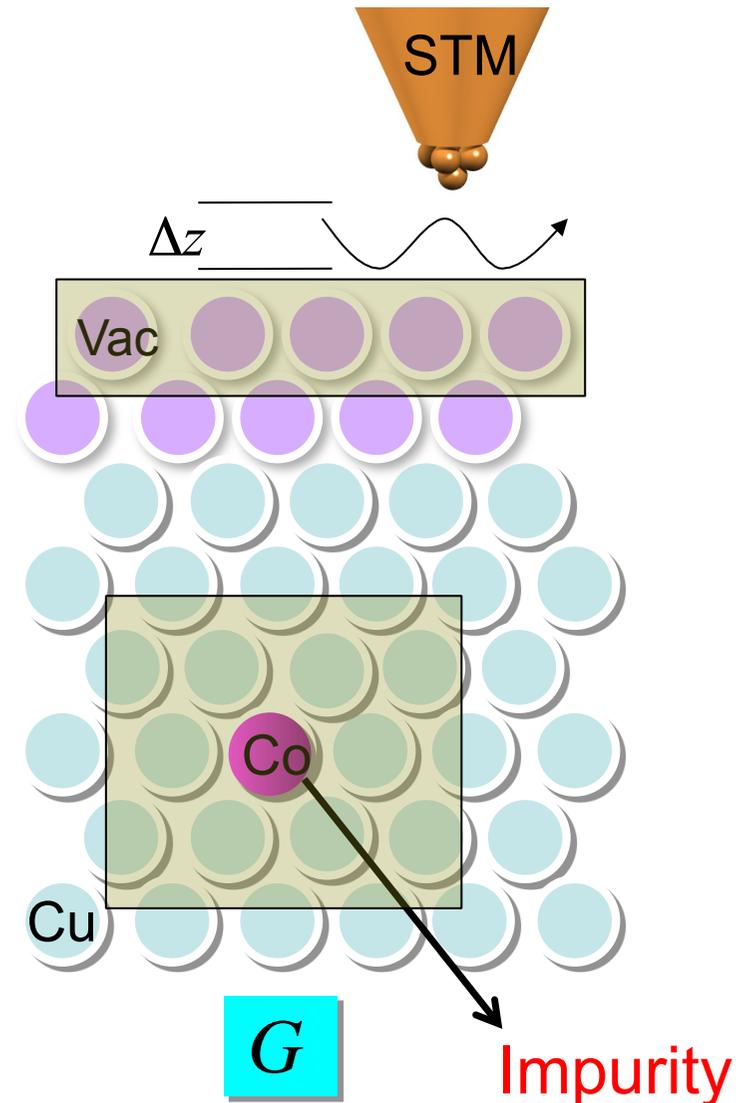
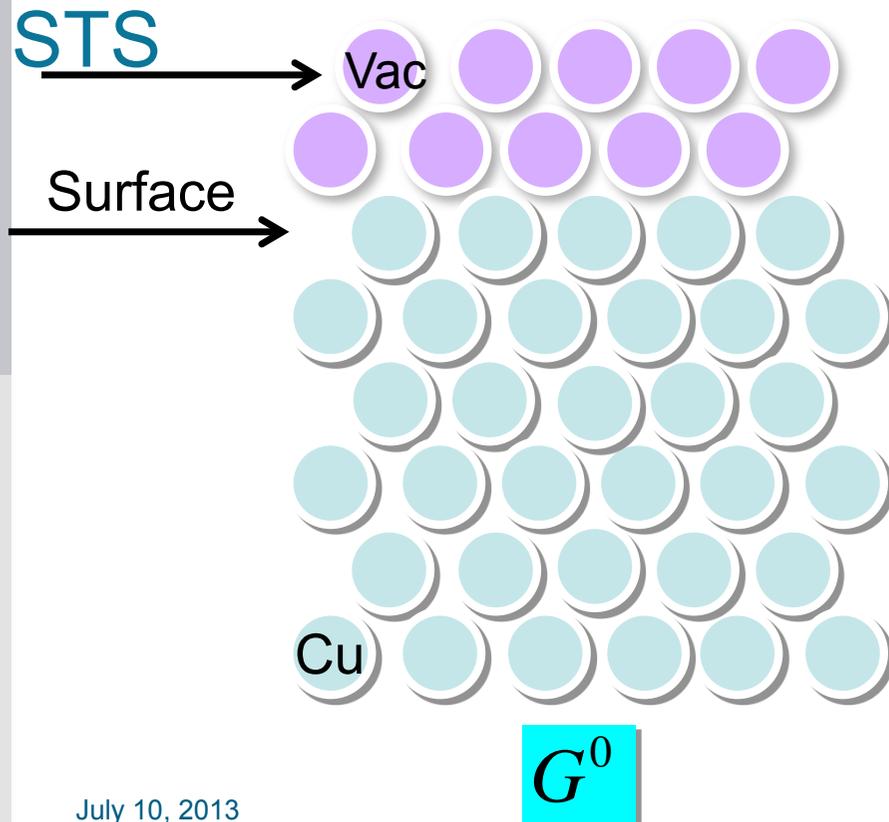
Impurity

# Method

Tersoff-Hamann  
Model:

$$I(\vec{r}_{\parallel}, z, V) \propto n_T \int_{E_F}^{E_F + eV} n(\vec{r}_{\parallel}, z, \epsilon) d\epsilon$$

$$\Delta G_{vac} = G_{vac-imp}^0 V_{imp} G_{imp-vac}^0$$

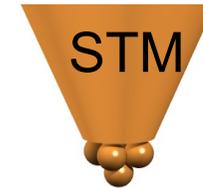


# Method

Tersoff-Hamann  
Model:

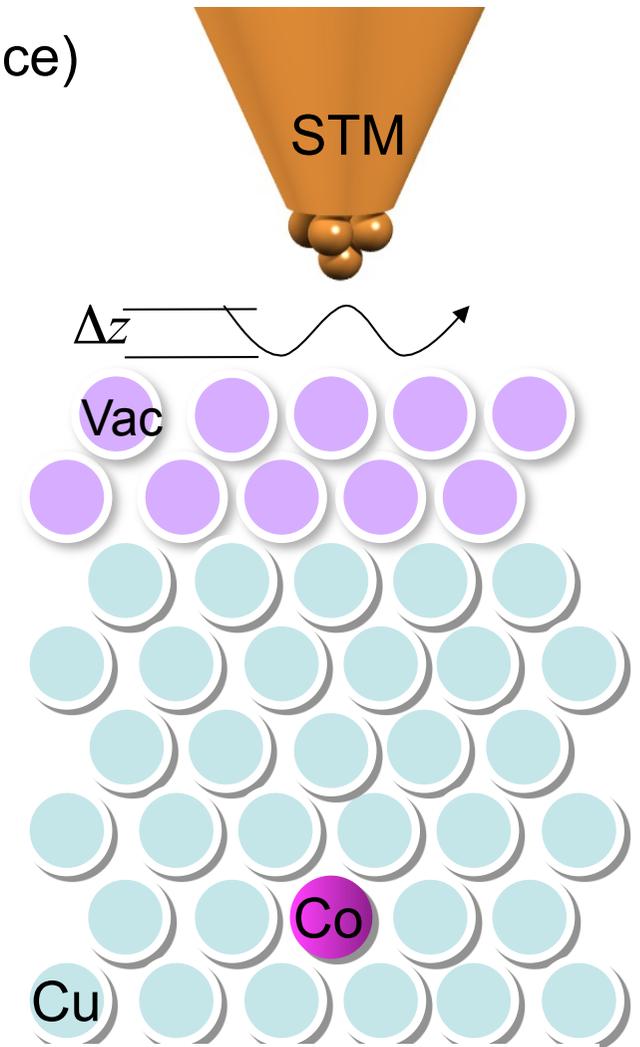
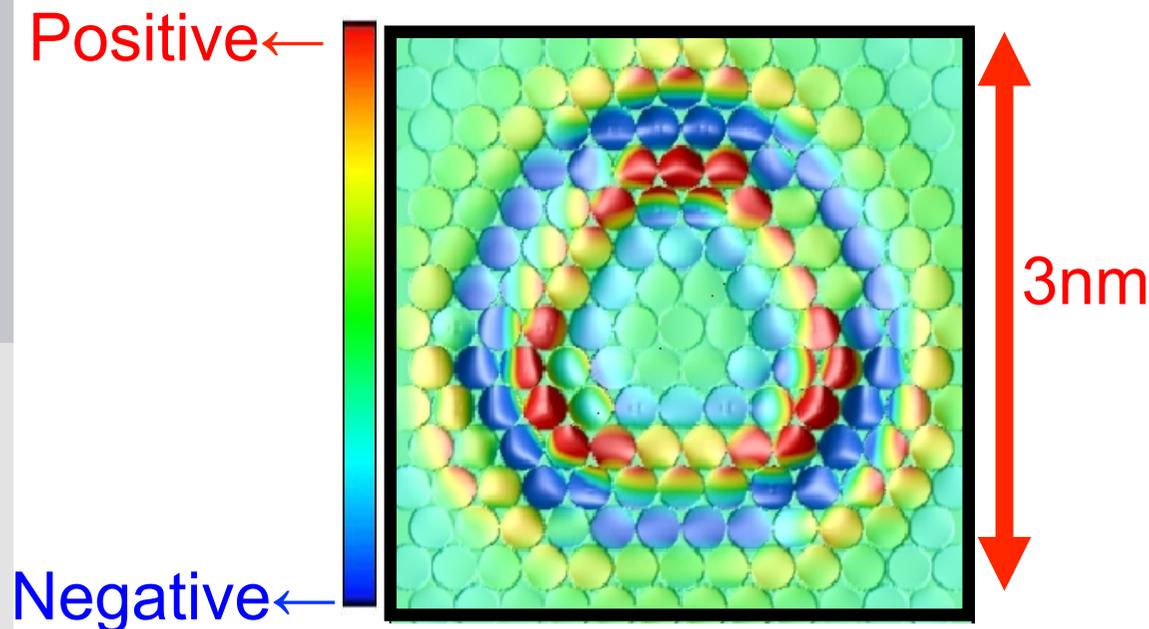
$$I(\vec{r}_{\parallel}, z, V) \propto n_T \int_{E_F}^{E_F + eV} n(\vec{r}_{\parallel}, z, \epsilon) d\epsilon$$

$$\Delta G_{vac} = G_{vac-imp}^0 V_{imp} G_{imp-vac}^0$$



# Result: Constant Current STM-image Co buried below Cu(111) surface

- Charge density in vacuum ( $\sim 6.1\text{\AA}$  above the surface)
- Bias Voltage  $V$ : 100 meV below  $E_F$
- Co at 6<sup>th</sup> layer below the surface ( $\sim 12.1\text{\AA}$ )

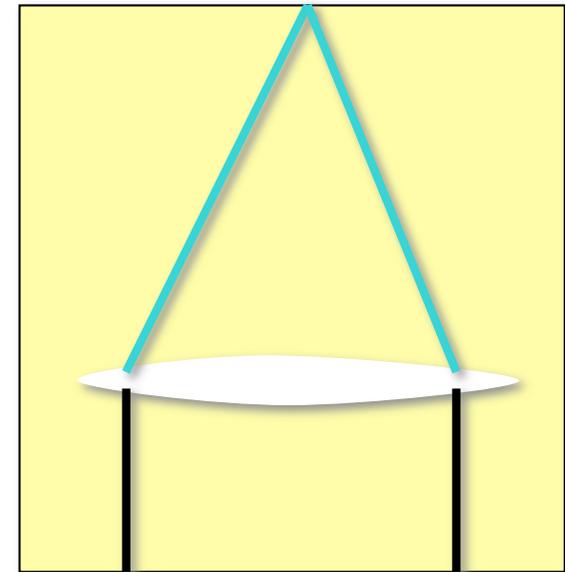
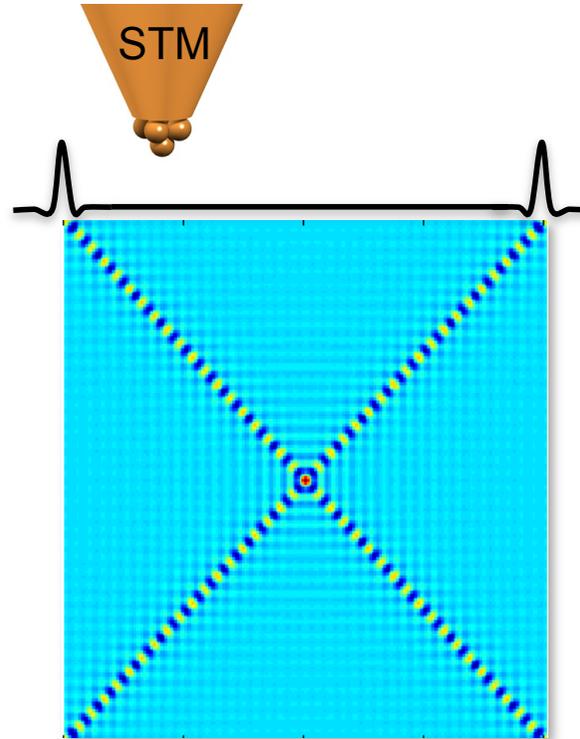
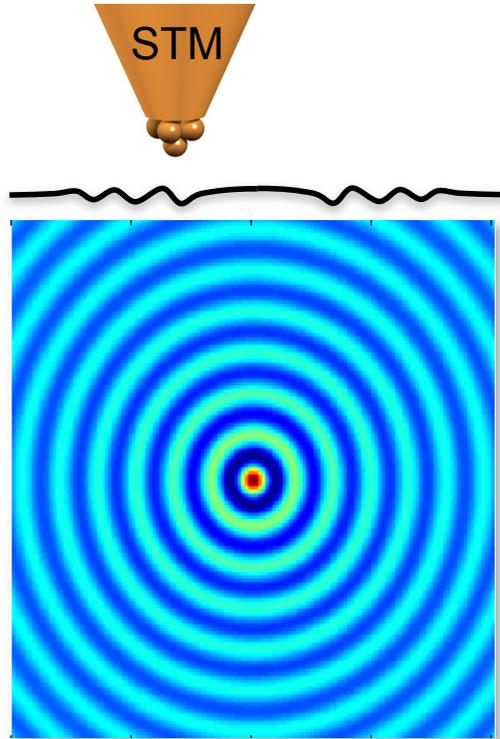


- ▣ Weismann, Wenderoth, Lounis, Zahn, Quaas, Ulbrich, Dederichs, Blügel, *Science* (2009)
- ▣ Lounis, Zahn, Weismann, Wenderoth, Ulbrich, Mertig, Dederichs, Blügel, *PRB* (2011)

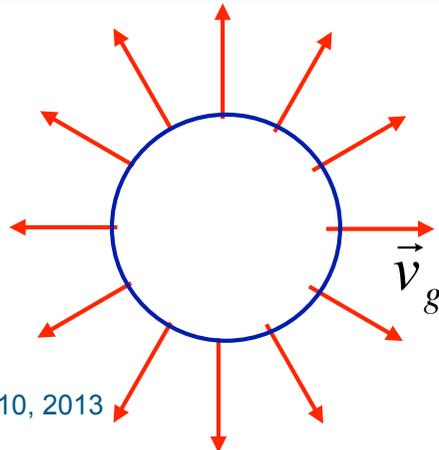
# Origin of effect

Dyson eq.:

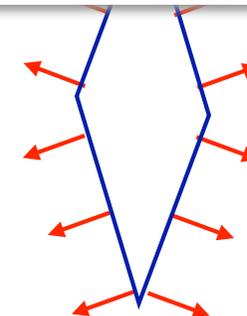
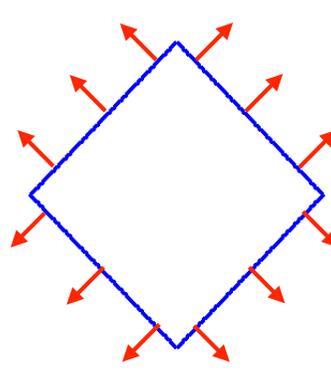
$$G(E) = G_0(E) + G_0(E)V G(E)$$



Lens focusing light



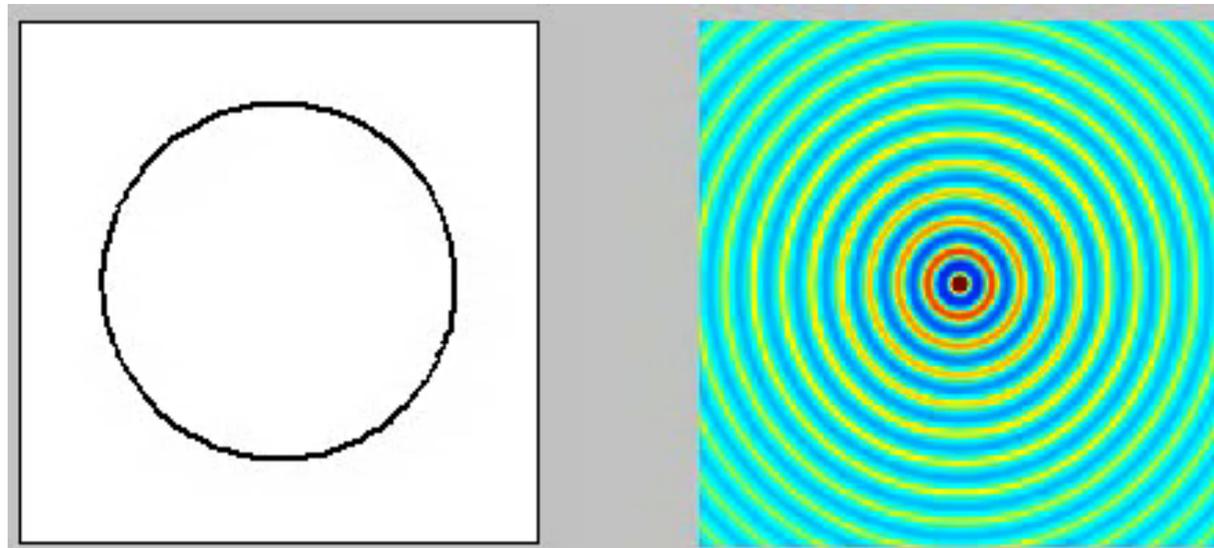
$$\vec{v}_g = \frac{\partial E}{\partial \vec{k}}$$



# Origin of effect

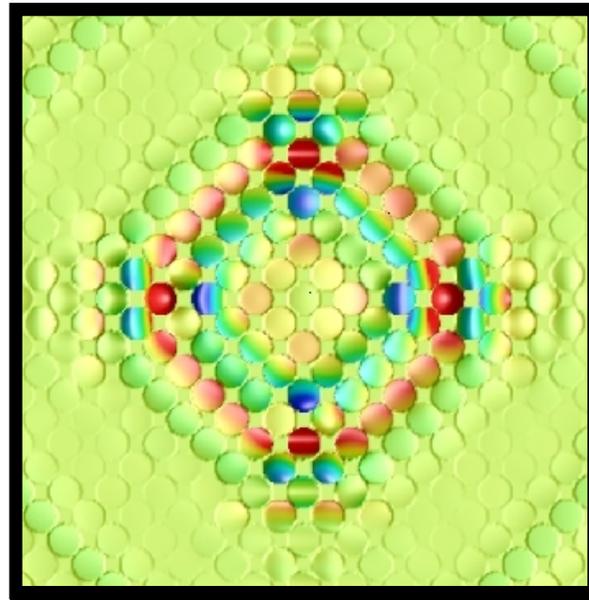
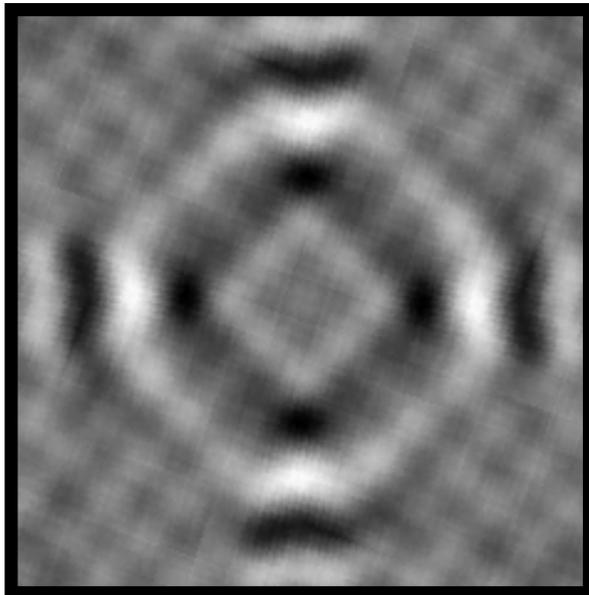
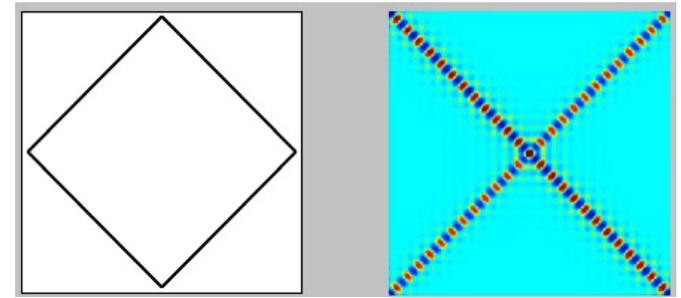
Dyson eq.:

$$G(E) = G_0(E) + G_0(E)V G(E)$$

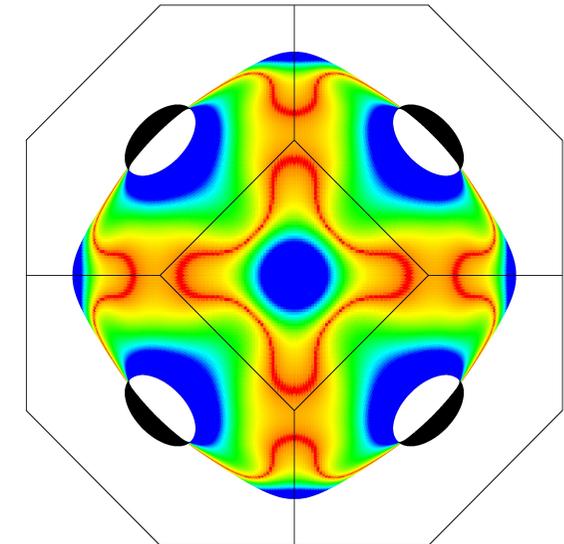


- Weismann, Wenderoth, Lounis, Zahn, Quaas, Ulbrich, Dederichs, Blügel, *Science* (2009)
- Lounis, Zahn, Weismann, Wenderoth, Ulbrich, Mertig, Dederichs, Blügel, *PRB* (2011)

# Origin of effect

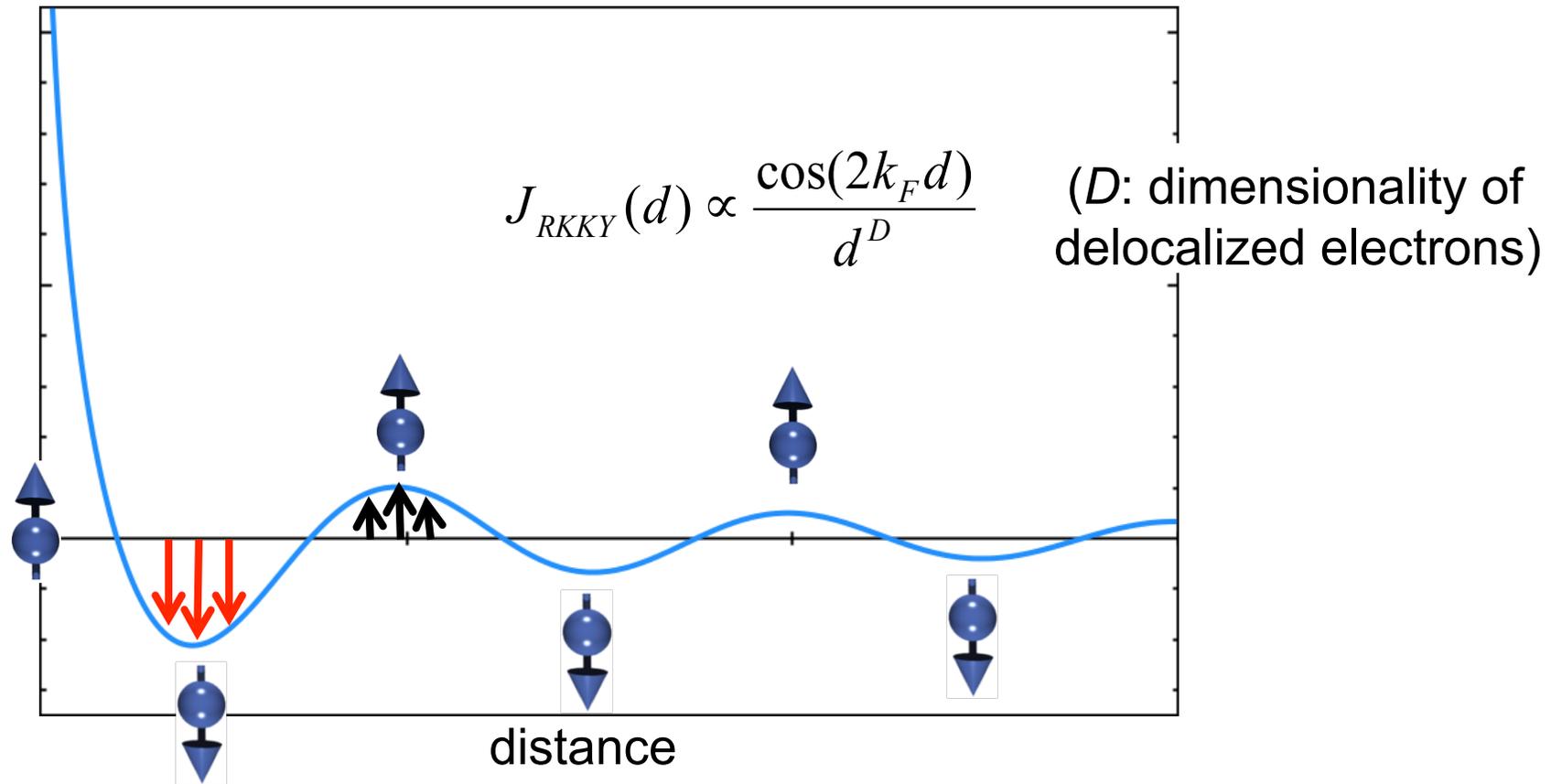


Co at 8<sup>th</sup> layer  
below  
Cu(001) surface



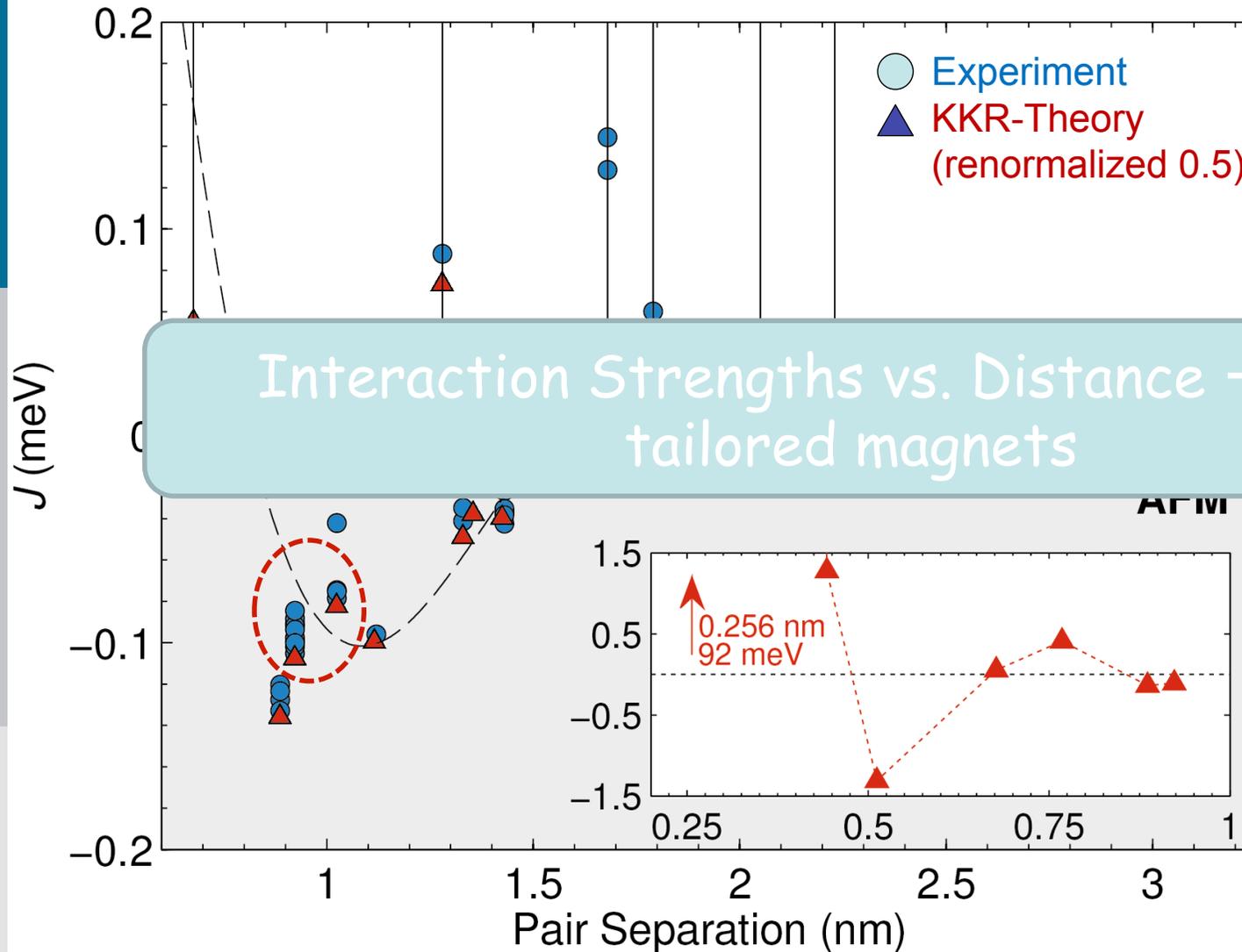
0.05 0.78 1.50  
Measure of curvature

Real space visualisation of Fermi surfaces with STM!



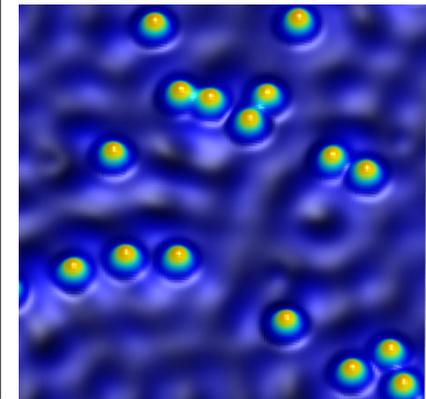
- M. A. Ruderman, C. Kittel, *Phys. Rev.* (1954);
- T. Kasuya, *Prog. Theor. Phys.* (1956);
- K. Yosida, *Phys. Rev.* (1957)

# RKKY Interaction in Fe Pairs on Cu(111)

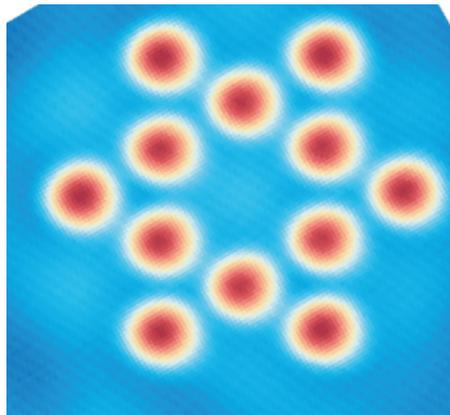


### Ab initio calculations:

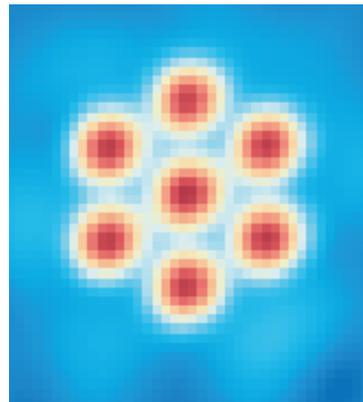
- fully-relativistic KKR Green function method
- LDA
- relaxed



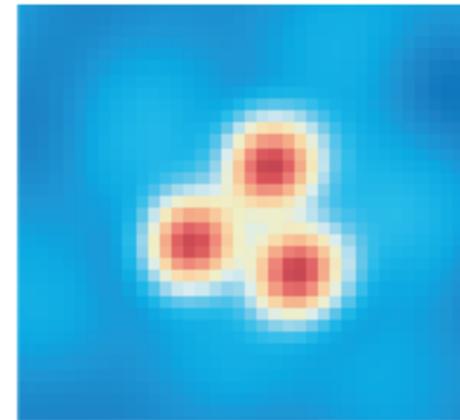
# Manufacturing and investigating antiferromagnetic nano-objects



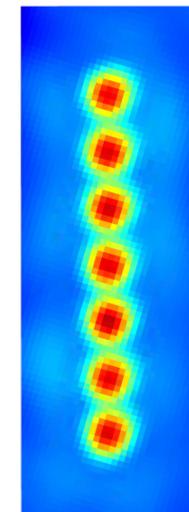
“Kagome”



Flower



Trimer

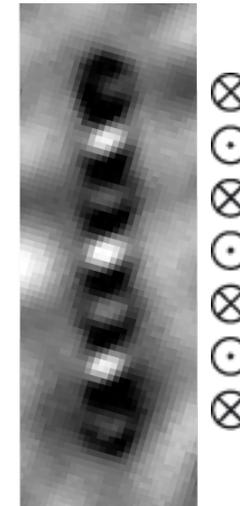
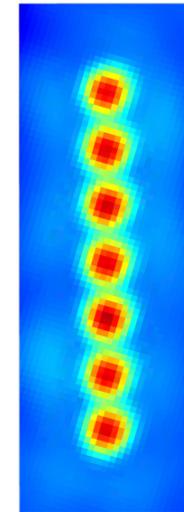
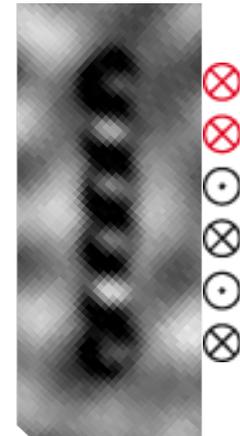
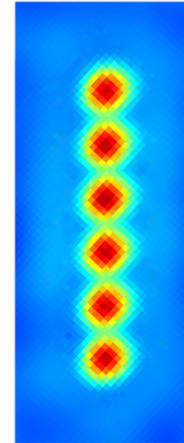
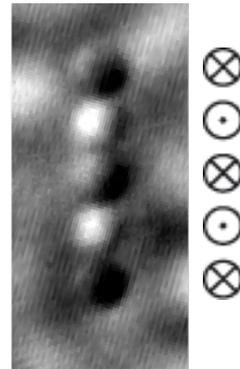
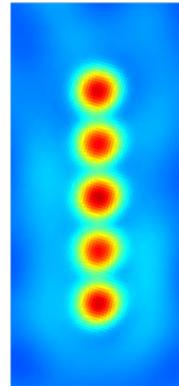
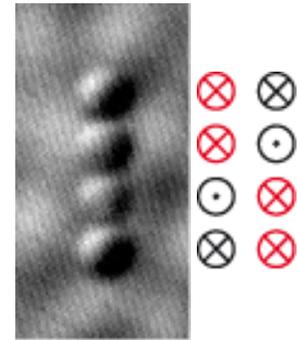
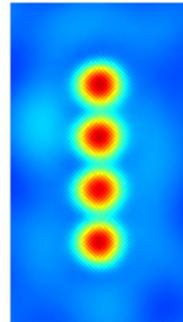
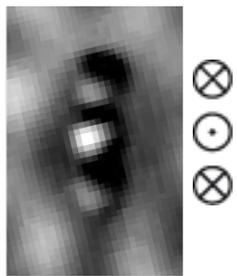
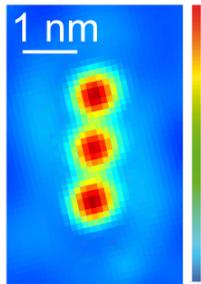


Wires

# Odd and Even Antiferromagnetic Chains

odd → one uncompensated moment  
 even → compensated moment

topography



spin-resolved  
 $dI/dV$   
**B = -0.6 T**

Here:  $J_2 = B$  and  $MAE K \gg J_1$  and  $B \rightarrow$  Ising-like system

# Summary

- Overview of recent novel applications of the KKR method
- One atom more or less matters!
- Impact on magnetism, frustration, electronic confinement, interactions
- KKR = elegant tool to investigate nanostructures