

$$\Rightarrow t_{\text{cool}} \approx 5 \times 10^{17} \text{ s} = 1.5 \times 10^{10} \text{ yrs} = \underline{\underline{\text{Hubble time!}}}$$

So gas cools very slowly, all E_s should have hot gas, explains why they not forming stars.

5. Active galaxies / galactic nuclei

→ Seyfert, 1943, discovered that 1% of nearby S_s have a bright point source at the centre

→ Seyfert galaxies.

→ Optical spectra show intense broad emission lines
 ⇒ high velocity ionised gas.

→ Two distinct types

Type I - v. broad lines ($1000s \text{ km s}^{-1}$)

Type II - relatively narrow lines ($100s \text{ km s}^{-1}$)

→ Also found to be X-ray sources

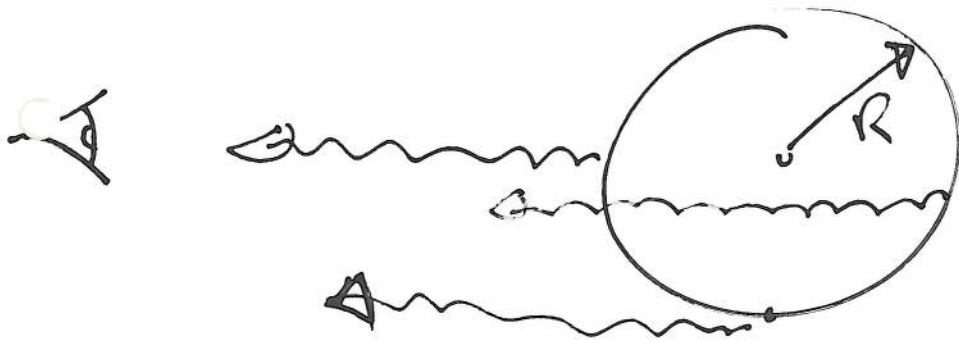
Type I - unabsorbed X-ray spectra

Type II - strongly absorbed X-ray spectra.

The nature of active galactic nuclei (AGN). ^{14.16.2}

AGN are observed to vary rapidly, on time scales as short as 1 hour.

Variability to constrain the size of the object.



observe a range of time delays due to light travel time across the object

$$\Delta t \sim \frac{R}{c}$$

So if an object varies on $\Delta t \sim 1$ hour

$$\Rightarrow R \lesssim 10^{12} \text{ m} = \underline{\underline{7 \text{ AU}}}$$

So AGN emission must arise from a region \simeq Solar system, much smaller than galactic scales (e.g. nearest stars, $\sim 1 \text{ pc}$, $\underline{\underline{\sim 10^5 \text{ AU}}}$).

14.16.3

2nd constraint, luminosity places a limit on the mass of an object, limited by the Eddington limit, L_{Edd} , luminosity at which an object is disrupted by its own radiation pressure.

Radiation pressure from photon momentum:

$$p = \frac{E}{c} \quad \text{--- energy of photon}$$

Energy flux from an object

$$f = \frac{L}{4\pi r^2} \quad \begin{array}{l} \text{--- luminosity} \\ \text{--- area of shell} \end{array}$$

$$\text{momentum flux} = \frac{f}{c} = \frac{L}{4\pi r^2 c}$$

The fraction of this flux transferred to material depends on its opacity,

Assume opacity is dominated by e^- scattering, which is the lowest plausible opacity, and wavelength independent.

Consider average force on each e^-

$$F_{e^-} = \frac{\sigma_T L}{4\pi r^2 c}$$

Thomson cross-section for e^- scattering = $6.65 \times 10^{-29} \text{ m}^2$

For Eddington limit, equate the radiation force with gravity

$$\frac{\sigma_T L_{\text{Edd}}}{4\pi r^2 c} = \frac{G M m_p}{r^2}$$

mass of central object
mass of a proton.

(note e^- & p^+ held together by the electric force).

$$\Rightarrow L_{\text{Edd}} = \frac{4\pi G M m_p c}{\sigma_T}$$

$$= 1.5 \times 10^{31} \frac{M}{M_{\odot}} \text{ (W)}$$

A powerful AGN can have $L \sim 5 \times 10^{39} \text{ W}$.

$$\Rightarrow M > 3.3 \times 10^8 M_{\odot} !$$

So must fit $\sim 10^8 M_{\odot}$ into a region the size of our Solar system.

\Rightarrow supermassive black hole.

Only plausible source of energy is accretion
 - the release of grav. potential energy from a falling object.

$$E_{\text{acc}} = \frac{GMm}{R_{\text{min}}} - \frac{GMm}{R_{\text{max}}}$$

- max energy release from a compact object (maximising $\frac{M}{R}$).

Radius of a B.H. (event horizon) can be estimated by equating escape velocity to c .

$$R_s = \frac{2GM}{c^2}$$

↑ Schwarzschild radius.

for $M \sim 10^8 M_{\odot} \Rightarrow R \sim 8 \text{ AU}$.

subst $\frac{M}{R}$ for a B.H.

$$\Rightarrow E_{\text{acc}} = \frac{GMm}{2R} = \frac{1}{2} mc^2$$

mass of infalling material.

so half the rest mass energy of infalling material is potentially liberated.

c.f. with $\sim 1\%$ of rest mass liberated by nuclear fusion ^{14.17-2}

Can we grow these B.H.s. by accretion?

$$L = \frac{dE}{dt} = \epsilon c^2 \frac{dm}{dt}$$

ϵ luminosity. $\frac{dm}{dt}$ accretion rate.

radiative efficiency factor
(some energy can be advected into the B.H.).

To explain luminosities of A.G.N., need $\frac{dm}{dt} \sim 1 M_{\odot}/y$
($\sim 10^{39}$ W).

Equate L with L_{Edd} & rearrange.

$$\frac{dM}{dt} = M \frac{4\pi G m_p}{\epsilon c \sigma_T}$$

Solve by integrating.

$$\int_{M_0}^M \frac{1}{m} \cdot dm = \frac{4\pi G m_p}{\epsilon c \sigma_T} \int_0^t dt$$

initial mass $\rightarrow M_0$

$$\underline{M = M_0 e^{t/\tau}}$$

$$\tau = \frac{\epsilon c \sigma_T}{4\pi G m_p}$$

14.17.3

Assume $M_0 \approx 10 M_\odot$, which is available from a single supernova, want $M \approx 10^9 M_\odot$ (maximum seen in AGN)

$$\Rightarrow \frac{M}{M_0} = 10^8 = e^{t/\tau} \Rightarrow t = 8 \times 10^8 \text{ yr} \leq \text{Hubble time } (10^{10} \text{ yr}).$$

Two other types of AGN discovered.

① Radio galaxies

- brightest radio sources in the sky,
- dual-lobed emission, fed by jets of material from a galactic nucleus.
e.g. Cygnus A, $d = 100 \text{ Mpc}$, $L_{\text{radio}} \approx 10 L_{\text{m.w.}}$
- optical spectra of central objects show strong broad emission lines,
- Type I & II objects seen.
- most radio galaxies are Es, thought that recent mergers has stirred up the gas and increased accretion rate onto B.H.

② Quasars (quasi-stellar radio source).

- Bright point sources, associated with strong radio emission.

- strong broad emission lines.

e.g. 3C 48 $z = 0.37$

$\Rightarrow d \sim 1500 \text{ Mpc}$

$\Rightarrow L \sim 10^2 - 10^5 L_{\text{M.W.}}$

so look like point sources because the AGN is much more luminous than the galaxy.

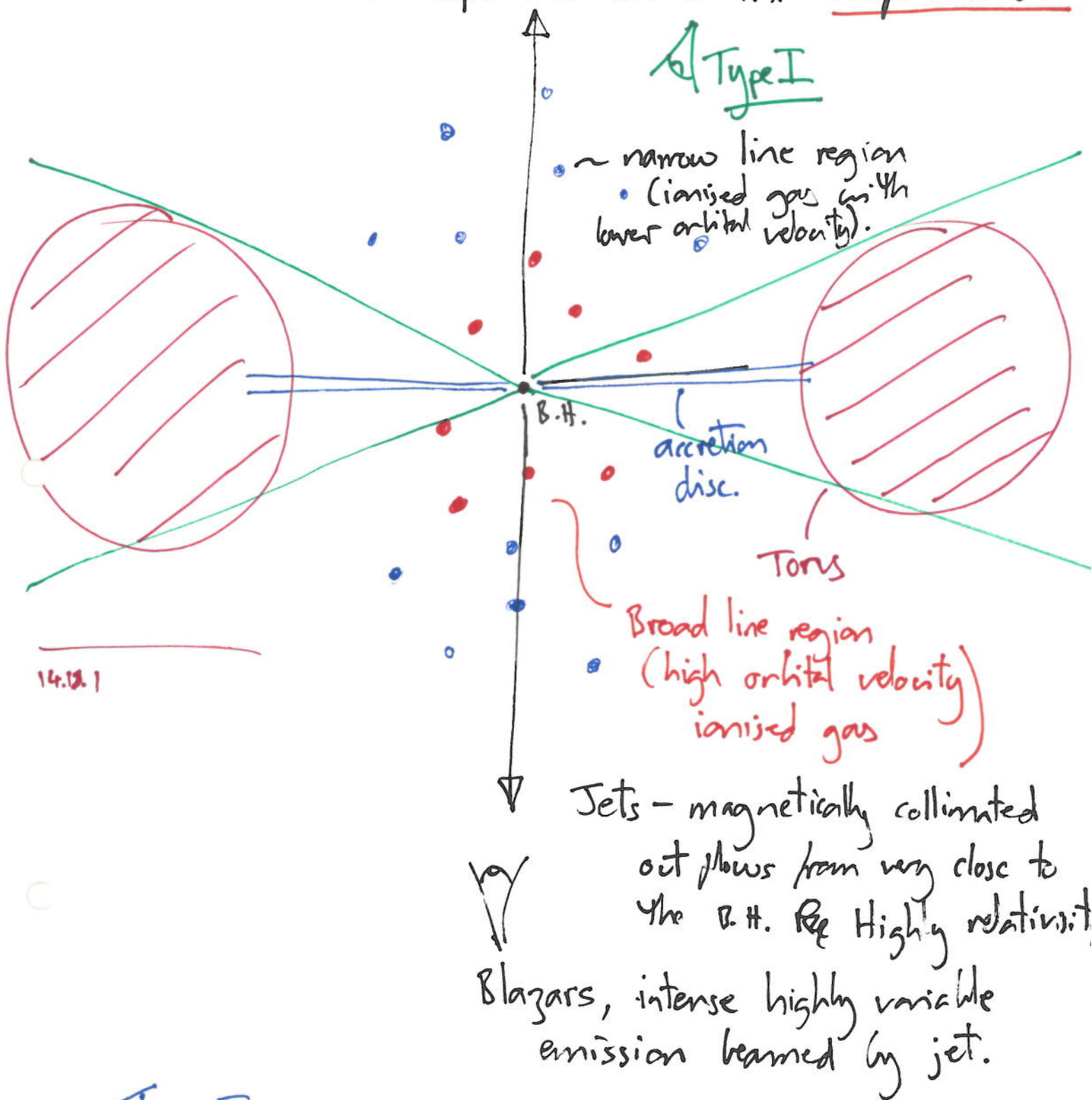
- type I & II objects seen + jets

- non-radio emitting versions "radio quiet"

\Rightarrow QSO (quasi-stellar objects).

All AGN now explained with the Unified model

14.17.5
+14.18.1



14.18.1

Type I - can see the broad line region, and the X-ray emission from inner accretion disc.

Type II - can only see the narrow line region, and X-rays absorbed by the torus.

A
Type II /

We see radio loud / quiet versions of type I & II AGN, associated with presence / absence of jet, may be related to ~~local~~ accretion rate.

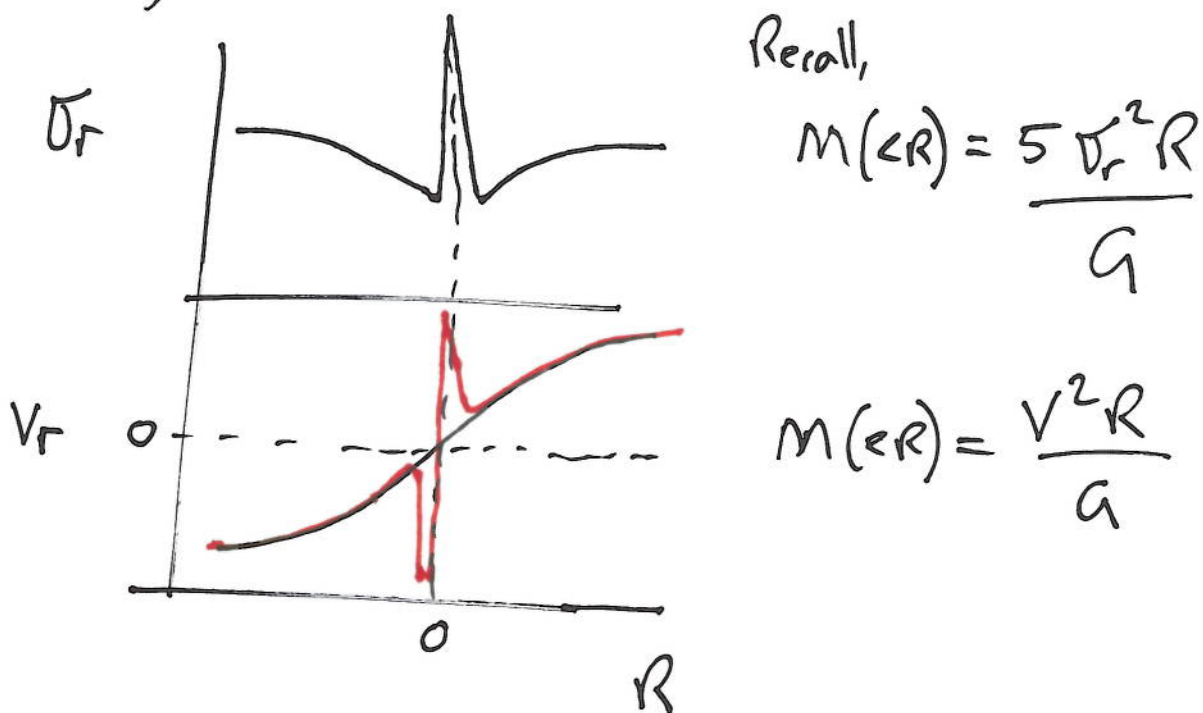
Crucial supporting evidence:

- Type I spectra hidden in the polarised (scattered) light of Type II objects.
- NGC 4151 transitioned from Type I to Type II.

Supermassive BHs in normal galaxies.

→ SMBHs were thought to be rare, until the discovery of many in normal galaxies.

→ e.g. M31



⇒ compact mass at the centre of M31

$$M = 3 \times 10^7 M_{\odot}$$

$$\text{and } \frac{M}{L} \geq 300.$$

→ many more examples discovered with HST

→ implies all giant galaxies were once active galaxies.

Also, in M.W.?!
 ○

→ observations in the infra-red (to avoid dust extinctions) with adaptive optics (to reach high spatial resolution),
 have ~~reve~~ revealed high velocity stars, very close to Galactic centre.

→ orbit of each star constrains enclosed mass

→ Best example, S2

$$P_{\text{orb}} = 15.2 \text{ yrs} \quad a = 0.119''$$

(semi-major axis)

use Kepler's 3rd law,

$$P^2 = \frac{4\pi^2}{GM} a^3$$

$$R_{\odot} = 8 \text{ kpc}$$

$$\Rightarrow M(<r) = 3.74 \times 10^6 M_{\odot}$$

Peri closest separation = $0.0155''$

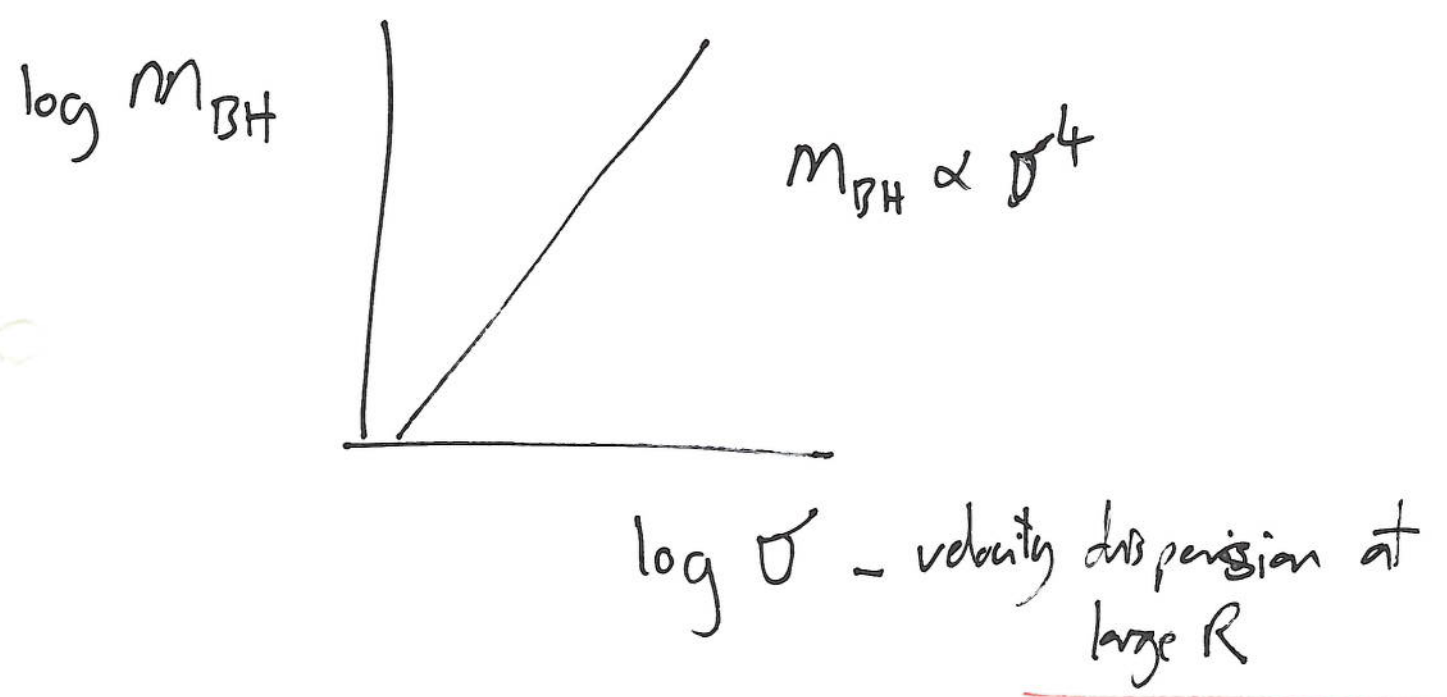
$$\Rightarrow R_{\text{B.H.}} \leq 124 \text{ AU}$$

$$\Rightarrow \rho_{\text{B.H.}} \geq 4.1 \times 10^{15} M_{\odot} \text{ pc}^{-3}$$

⇒ must be a B.H. !

14.18.6
+
14.19.1

→ The mass of BHs has be found to correlate with properties of the galaxy, tightest correlation is the $M-\sigma$ relation,



14.19.1

How can these properties know about each other? (The M_{BH} is negligible on the scale of the galaxy).

Most interpretations based AGN feedback.

Recall, $L_{acc} \leq L_{Edd} \propto M_{BH}$
at Eddington limited accretion rates we expect much of L_{acc} in K.E. of outflowing winds (driven by radiation pressure).

Eventually K.E. of wind can overcame grav. binding energy of gas in the galaxy \Rightarrow clear gas from galaxy \Rightarrow stop star formation \Rightarrow stop B.H. growth.

Recall, $U = -\frac{3}{5} \frac{GM_{gal}^2}{R}$ and $\sigma^2 = \frac{3}{5} \frac{GM_{gal}}{R}$
 \uparrow binding energy of uniform sphere

$\Rightarrow U \propto \sigma^4$

Balancing U & K.E. of outflow

$\Rightarrow M_{BH} \propto \sigma^4.$