Simulation of fluence-dependent photocurrent in terahertz photoconductive receivers

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Abstract

A semi-classical Monte Carlo simulation of carrier dynamics in photoconductive detectors of terahertz (THz) radiation is presented. We have used this simulation to elucidate the importance of carrier trapping in the operation of photoconductive detectors. Simulations of the detection of single-cycle THz pulses by photoconductive antennas based on GaAs with trap densities between $2 \times 10^{17}$ and $2 \times 10^{18}$ cm$^{-3}$ are presented. We show that the high frequency ($>1$ THz) spectral response of photoconductive devices decreases with increasing excitation fluence. Our simulations reveal that this effect is a direct consequence of the saturation of trapping centres.

(Some figures may appear in colour only in the online journal)

1. Introduction

Terahertz (THz) time-domain spectroscopy (TDS) has dramatically evolved over the last 25 years \cite{1, 2} to become a relatively well-established technique to access the far-infrared region of the electromagnetic spectrum (between $\sim 100$ GHz and $\sim 10$ THz) \cite{3, 4}. This tool has allowed the study of a large number of systems that range from bulk \cite{5} and nanostructured semiconductors, such as nanowires \cite{6, 7} and nanostructured semiconductors, to proteins \cite{9, 10}. The rapid evolution of this technique is, in part, the consequence of the advances in ultrafast laser technology as well as the progress in understanding of both nonlinear optical processes and carrier dynamics in semiconductors that are used as broadband single-cycle THz emitters \cite{11}.

A photoconductive receiver (PCR) detects pulses of THz radiation via the transient photocurrent between metal contacts on a semiconductor surface \cite{12-14}. While PCRs provide a compact and convenient method to detect linear or arbitrarily polarized THz radiation, the photoconductive decay time of the semiconductor material needs to be tailored carefully. The role of the trapping time in the response of PCRs has been discussed previously and two limiting cases were identified \cite{16, 17}.

(i) Direct sampling: when the decay time of free carriers in the PCR is much shorter than the duration of the THz transient. To a good approximation in this case $E_{\text{THz}}(t_0) \propto I(t_0)$, where $I(t_0)$ is the measured photocurrent as a function of the delay $t_0$ between the THz and gate pulses.

(ii) Integrating sampling: when the lifetime of free carriers in the PCR is much greater than the THz transient’s duration. In this case, $E_{\text{THz}}(t_0) \propto dI(t_0)/dt_0$ is an appropriate approximation.

In order to improve the signal-to-noise performance of these devices, there is a compromise between carrier lifetime and mobility, which proved to be optimum for lifetimes in between these two regimes. However, care has to be taken to ensure that the photo-excited carrier density is lower than the trap density; otherwise, the carrier density does not decay exponentially. The saturation of traps has been suggested as an explanation for the gate-fluence dependence of the spectral response experimentally observed for THz PCRs \cite{18}.
Figure 1. (a) The instantaneous photocurrent \( I(t, t_0) \) as calculated by the simulation for different delays \( t_0 \) between the optical pulse (always arriving at \( t = 0 \)) and the THz pulse. The inset shows the time-dependent THz applied electric field (time scale consistent with main figure). (b) The signal measured by a PCR as calculated using equation (3). The circles and arrows denote some of the values that correspond to the specific curves displayed in (a) when integrated.

While the dynamics of photocarriers in the surface-field, photo-Dember and photoconductive THz emitters has been well studied [19–29], very little attention has been paid to this aspect for photoconductive detectors. In this paper, we present a semi-classical Monte Carlo simulation of the current response of PCRs to pulsed THz radiation (section 2). The photoconductive material included saturable traps. The fluence dependence of the THz photocurrent at various trap densities indicates the regimes where a PCR will operate in direct or indirect sampling mode (section 3). Finally, we discuss the carrier–carrier scattering mechanism and its influence on the photocurrent in section 4.

2. Model

2.1. Description

The three-dimensional semi-classical Monte Carlo model presented here is analogous to one used previously to study THz emitters [19, 20, 30] with two modifications. Firstly, a finite trap density was included resulting in a bi-exponential decay of the number of free carriers, as discussed in section 2.2. Secondly, an externally applied electric field with a temporal profile

\[
E_{\text{THz}}(t) = -E_0 \frac{t-t_0}{0.4285\sigma} e^{-\frac{(t-t_0)^2}{\sigma^2}}
\]

was included, where \( t_0 \) is the relative delay of the incoming THz pulse, \( E_0 = 10 \text{ kV cm}^{-1} \) is its peak amplitude and \( \sigma = 0.1 \text{ ps} \) is half of the peak-to-peak time duration (see inset of figure 1(a)). This form of \( E_{\text{THz}} \) assumes that the incident radiation field is uniform across the entire simulation volume. This is a good approximation given that the THz field will be diffraction limited, in the best case, and that the THz radiation will take \( \sim 10 \text{ fs} \) to go across the photocarrier layer of \( \sim 1 \mu\text{m} \).

As low-temperature-grown [31, 32] and ion-implanted [33–36] GaAs are currently the most prevalent materials in PCRs [37], we utilized the parameters of GaAs shown in table 1 (taken from [38] and [39]). The model assumes a thermal distribution of carriers that are present before photoexcitation at a concentration of \( 2 \times 10^{14} \text{ cm}^{-3} \). The motion of carriers is calculated following Newton’s second law

\[
\mathbf{\dot{r}}(\mathbf{r}, t) = \frac{q}{m^*} (\mathbf{E}(\mathbf{r}, t))
\]

over short periods of time inside a parallelepiped box, where \( q \) and \( m^* \) are the charge and effective mass of the electron or hole and \( \mathbf{E} \) is the total electric field.

At each time step, scattering probabilities are calculated quantum mechanically for the following mechanisms: LO-phonon emission and absorption, TO-phonon intervalley transfer (\( \Gamma, L \) and \( X \)) which is proportional to the intervalley deformation potential and the number of final valleys available \( \beta_i \) (with \( i = \Gamma, L \) and \( X \)), acoustic phonon, charged impurity and carrier–carrier scattering [20]. Pseudorandom numbers are used to decide whether each particle is scattered, its scattering angle and energy loss. Subsequently, Poisson’s equation is solved over a fine grid across the parallelepiped. The resulting potential is used to calculate the space-charge electric field \( \mathbf{E}_\phi \), which when added to the incident THz electric field from

Table 1. Table showing some of the most important parameters for GaAs used in the Monte Carlo simulations presented in this paper.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>GaAs</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \Gamma ) valley effective mass</td>
<td>0.067m_0</td>
</tr>
<tr>
<td>L valley effective mass</td>
<td>0.56m_0</td>
</tr>
<tr>
<td>X valley effective mass</td>
<td>0.85m_0</td>
</tr>
<tr>
<td>Hole effective mass</td>
<td>0.5m</td>
</tr>
<tr>
<td>Band-gap energy</td>
<td>1.42 eV</td>
</tr>
<tr>
<td>L valley offset</td>
<td>0.29 eV</td>
</tr>
<tr>
<td>X valley offset</td>
<td>0.48 eV</td>
</tr>
<tr>
<td>( \beta_\Gamma )</td>
<td>1</td>
</tr>
<tr>
<td>( \beta_L )</td>
<td>4</td>
</tr>
<tr>
<td>( \beta_X )</td>
<td>3</td>
</tr>
<tr>
<td>Def. potential (( \Gamma = L ))</td>
<td>0.4 eV A(^{-1})</td>
</tr>
<tr>
<td>Def. potential (( \Gamma = X ))</td>
<td>2.9 eV A(^{-1})</td>
</tr>
<tr>
<td>( \epsilon_0 )</td>
<td>12.95</td>
</tr>
<tr>
<td>( \epsilon_\infty )</td>
<td>10.9</td>
</tr>
<tr>
<td>( \alpha )</td>
<td>1.2 \times 10^9 m(^{-1})</td>
</tr>
</tbody>
</table>
equation (1) gives the total electric field \( \mathbf{E} \) acting on each carrier for the next time step.

Carrier photoinjection is performed using a Gaussian temporal and spatial profile (across the surface) with an exponential distribution in the depth direction corresponding to an absorption coefficient \( \alpha \).

In order to model the receiver’s response, full sets of simulations were performed for a number of relative delays \( t_0 \) between the THz pulse and the gate pulse (always arriving at \( t = 0 \)). The simulated time resolved current \( I(t, t_0) \) parallel to \( \mathbf{E}_\text{THz} \) is shown for various delays \( t_0 \) in figure 1(a). The photocurrent signal \( PC(t_0) \) that would be measured experimentally is assumed to be

\[
PC(t_0) \propto \int_{-\infty}^{+\infty} I(t, t_0) \, dt
\]

and is shown in figure 1(b). The small current signals seen for \( t < 0 \) in figure 1(a) are the thermal carriers being accelerated by the THz pulse with a relatively fast negative contribution and a smaller long-lived positive tail. The integral of this contribution is substantially smaller (\( \sim 0 \)) than that from the photo-excited carriers (close to \( t = 0 \)).

The data presented in this paper were extracted from 824 individual simulations for different relative THz-gate delays, fluences, trap densities and scattering conditions ran on a 12-core (3.1 GHz) cluster node with 128 GB of RAM. Twelve simulations were run at a time, one on each core, taking \( \sim 48 \) h of CPU time.

2.2. Trap saturation model

The density of free electrons after photoexcitation is calculated by numerically solving the set of rate equations

\[
\frac{dN}{dt} = -\frac{N}{\tau_e} - \gamma N(T_0 - T), \tag{4}
\]

\[
\frac{dT}{dt} = \gamma N(T_0 - T), \tag{5}
\]

where \( T_0 \) is the density of traps, \( N \) is the total density of photo-excited electrons, \( T \) is the density of occupied traps, \( \tau_e (\sim 10 \text{ ns}) \) [40] is the electron–hole recombination time constant and \( \gamma \) is an electron–trap coupling constant that was set to \( \sim 10^{-5} \text{ cm}^3 \text{ s}^{-1} \) to fit experimentally available data. The density of photo-excited electrons and the density of occupied traps for various optical fluences (between 2 and 60 \( \mu \text{J cm}^{-2} \)) as function of time are shown in figures 2(a) and (b), respectively. This calculation was performed assuming a trap density of \( 2 \times 10^{18} \text{ cm}^{-3} \) typical of low-temperature-grown or ion-implanted semiconductors after annealing [17, 41].

3. Influence of fluence

Sets of simulations were performed over a time interval of 3 ps by varying the pump fluence in the range from 2 to 60 \( \mu \text{J cm}^{-2} \). The resulting integrated photocurrent curves as a function of relative delay are plotted in figures 3(a) and (b) which correspond to trap densities of \( 2 \times 10^{17} \) and \( 2 \times 10^{18} \text{ cm}^{-3} \), respectively. Note that in figure 3(b) the current curves for low fluences are bipolar, showing a direct-sampling-like behaviour. In the case of high fluences, the current curve becomes unipolar which corresponds to an integrating-sampling-like behaviour. This effect is a natural consequence of the trap saturation illustrated in figure 2. The greater degree of trap saturation in the low trap density simulation (figure 3(a)) also produces a long-lived current tail after the main pulse which is caused by carriers that follow their ballistic trajectories after the main pulse for a time significantly longer than the pulse duration.
The spectral response of photoconductive detectors can be examined by investigating the Fourier transform of the photocurrent, as shown in figures 3(c) and (d). It is clear that low-frequency components (<1 THz) tend to increase with fluence, due to an enhanced persistent photocurrent. This also produces a modulation in the spectrum caused by the step produced between the first and last points in the time-domain curve.

In the high-frequency region (3.5 THz), the trend is a reduced spectral amplitude with increasing gate fluence. This effect has been observed experimentally before [18]. The spectral effect of the gate fluence is more pronounced in the higher trap density simulations. The $2 \times 10^{17}$ cm$^{-3}$ trap density simulation becomes saturated even for the lowest gate fluence shown (2 $\mu$J cm$^{-2}$). In comparison, the simulation with a higher trap density ($2 \times 10^{18}$ cm$^{-3}$) results in a fast saturation of traps at 60 $\mu$J cm$^{-2}$ and unoccupied traps at 2 $\mu$J cm$^{-2}$, explaining the difference seen in the simulations.

The PCR’s signal amplitude will present a strong dependence on gate fluence. To a first approximation the signal is expected to increase with conductivity, which is proportional to the carrier density and therefore to the gate fluence. Yet, the Monte Carlo model presented here accounts for several other effects, including energy-dependent effective masses or carrier-density-dependent scattering rates for each carrier, in addition to trap saturation, predicting the response of the PCRs more accurately. In figure 4, the simulated signal amplitude for two trap densities is shown at fluences from 0.2 to 200 $\mu$J cm$^{-2}$. For the low trap density sample, there is a clear sub-linear behaviour (the dotted curve has a gradient of 1), similar to that reported in previous experimental studies [18, 42]. The high trap density simulation has an almost linear dependence for low fluences ($<10$ $\mu$J cm$^{-2}$), then a super-linear increase for intermediate fluences (between 10 and 60 $\mu$J cm$^{-2}$) and a sub-linear dependence for high fluences. The super-linear region is mostly caused by the effective carrier lifetime that increases as traps saturate, therefore producing a super-linear increase of the average conductivity over the duration of the THz pulse.

4. Influence of scattering mechanisms

Carrier–carrier scattering has been suggested as an additional mechanism that could influence the gate-fluence dependence of photoconductive devices [21]; however, carrier–carrier scattering is an elastic mechanism that might have relatively small effect on the total current. The Monte Carlo model presented here allows this scattering mechanism to be turned on and off, in order to distinguish its contribution to the PCR’s response. Simulations at 2 and 60 $\mu$J cm$^{-2}$ with and without including carrier–carrier scattering were performed. The time-domain and Fourier-transformed spectra resulting from these simulations showed no significant change when the carrier–carrier mechanism was excluded as seen in figures 5(a) and (b). These calculations demonstrate that the effect of carrier–carrier scattering on the receiver’s response is negligible compared to the effect of trap saturation.

The evolution of the rates for different scattering mechanisms can be directly extracted from our Monte Carlo simulation. Interestingly, for the simulations where the carrier–carrier scattering is included, it turns out to be the dominant scattering mechanism across most of the simulation. However, for the duration of the THz transient, which is the period when
carriers are strongly accelerated, the carrier–carrier scattering rate becomes comparable to the LO-phonon emission rate \( W_{cc} \approx W_{LO-en} \approx 8 \times 10^{12} \text{ s}^{-1} \) for both the low (2 \( \mu \text{J cm}^{-2} \)) and high (60 \( \mu \text{J cm}^{-2} \)) gate-fluence simulations. Given that LO-phonon scattering is non-elastic, it is expected to produce a greater effect on the current. This explains the negligible effect of carrier–carrier scattering on the photoconductive detector’s responsivity and dynamic range will not be affected when performed at different gate fluences, given that both the responsivity and dynamic range will not be affected evenly across the spectrum.

5. Conclusions

In conclusion, we have presented a Monte Carlo simulation of THz photoconductive detectors and elucidated the role of trap saturation on the time- and frequency-domain response of photoconductive detectors. The contribution of carrier–carrier scattering was found to be marginal in comparison. We expect this simulation to become a very useful tool to design new materials with tailored optoelectronic properties for PCR device applications.

We demonstrated that trap saturation plays an important role in defining the spectral responsivity of PCRs. In order to fabricate photoconductive detectors with either direct sampling or integrating behaviour, this effect has to be taken into account. This has some important implications as follows.

(i) In order to optimize ion-implantation or low-temperature growth and annealing of materials for photoconductive detectors, the gate-fluence regime in which they will be used should be taken into account.

(ii) Different spectroscopic measurements performed with a photoconductive detector should be compared with care when performed at different gate fluences, given that both the responsivity and dynamic range will not be affected evenly across the spectrum.

(iii) The analytic expression for response deconvolution (converting the measured signal to \( E_{THz} \)) presented in [17] is only valid when experiments are performed in the gate-fluence regime below trap saturation.

Auger recombination was not included in this model given that the calculations presented here are for fluences that produce carrier densities well below the regime where this effect is relevant. It might be of interest to include such a mechanism in the future if simulations are to be performed for higher fluences.

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