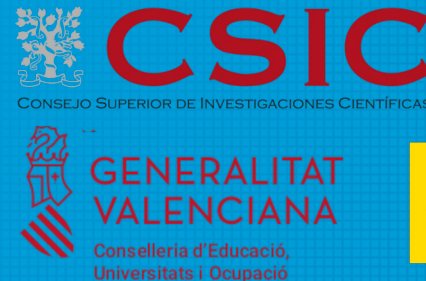


Hunting for the Cosmic Neutrino Background

Jack Shergold

& Martin Bauer; 2207.12413

JCAP 01 (2023), 003



Contents

- What is the CvB?

Contents

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- How might we go about detecting it?

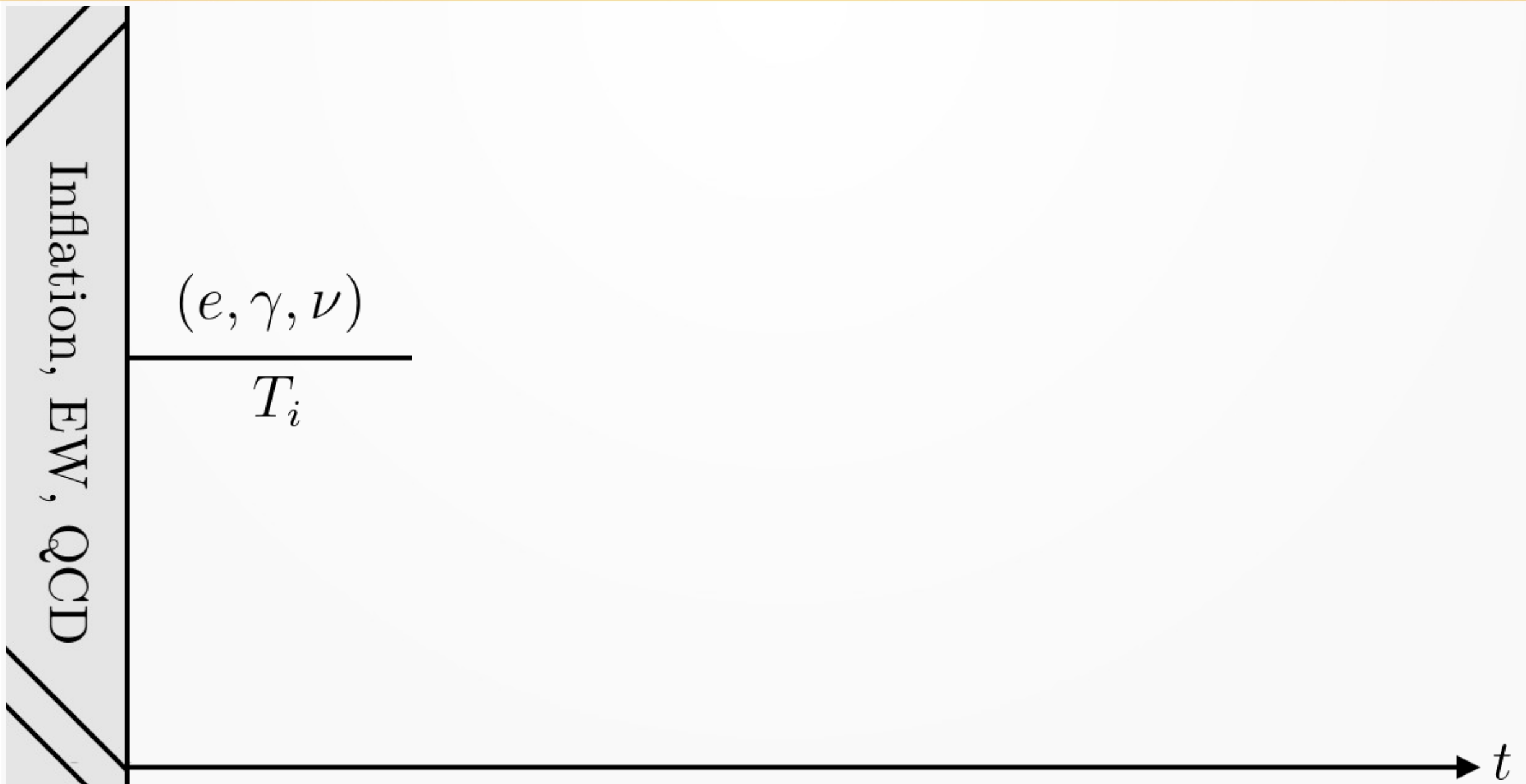
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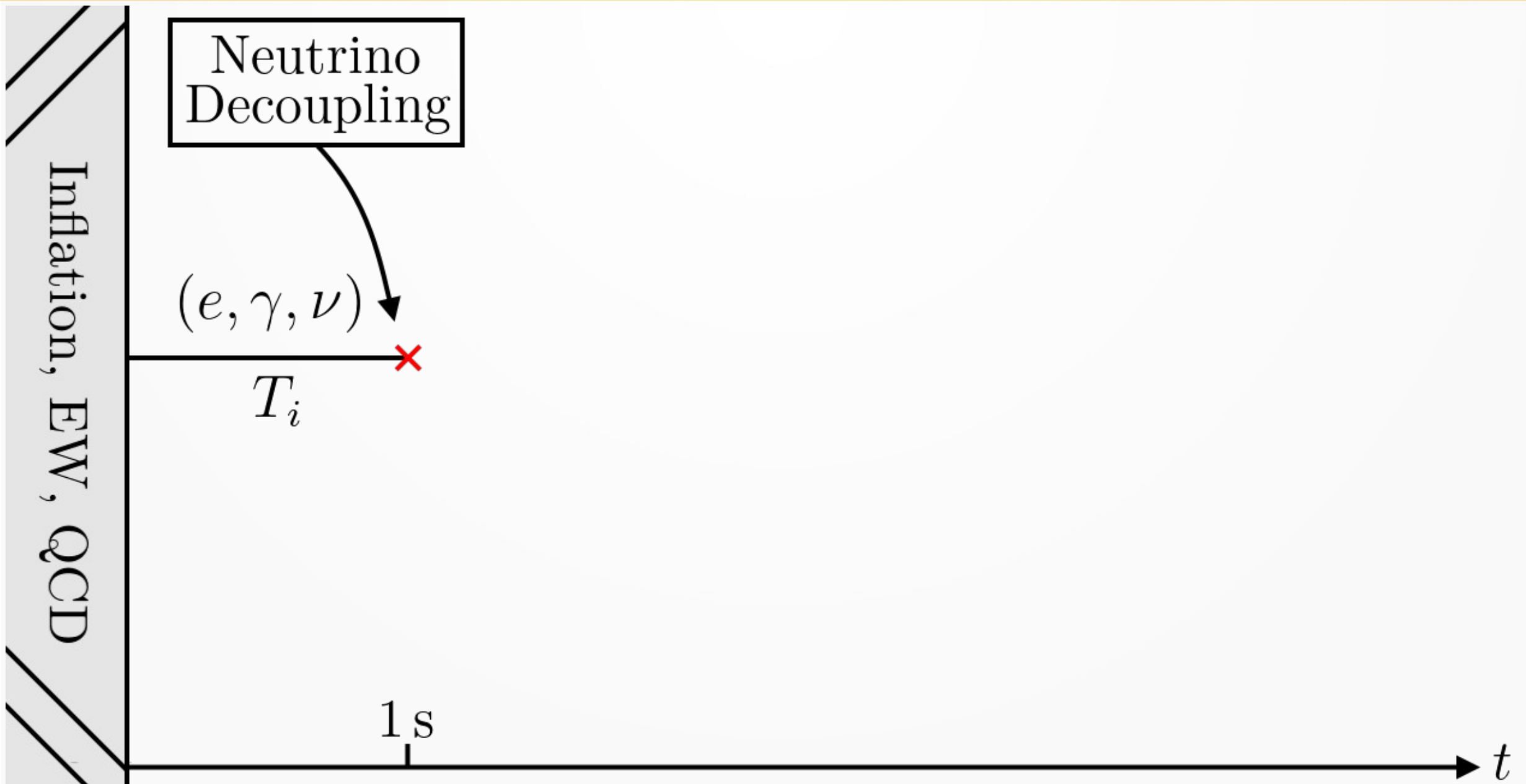
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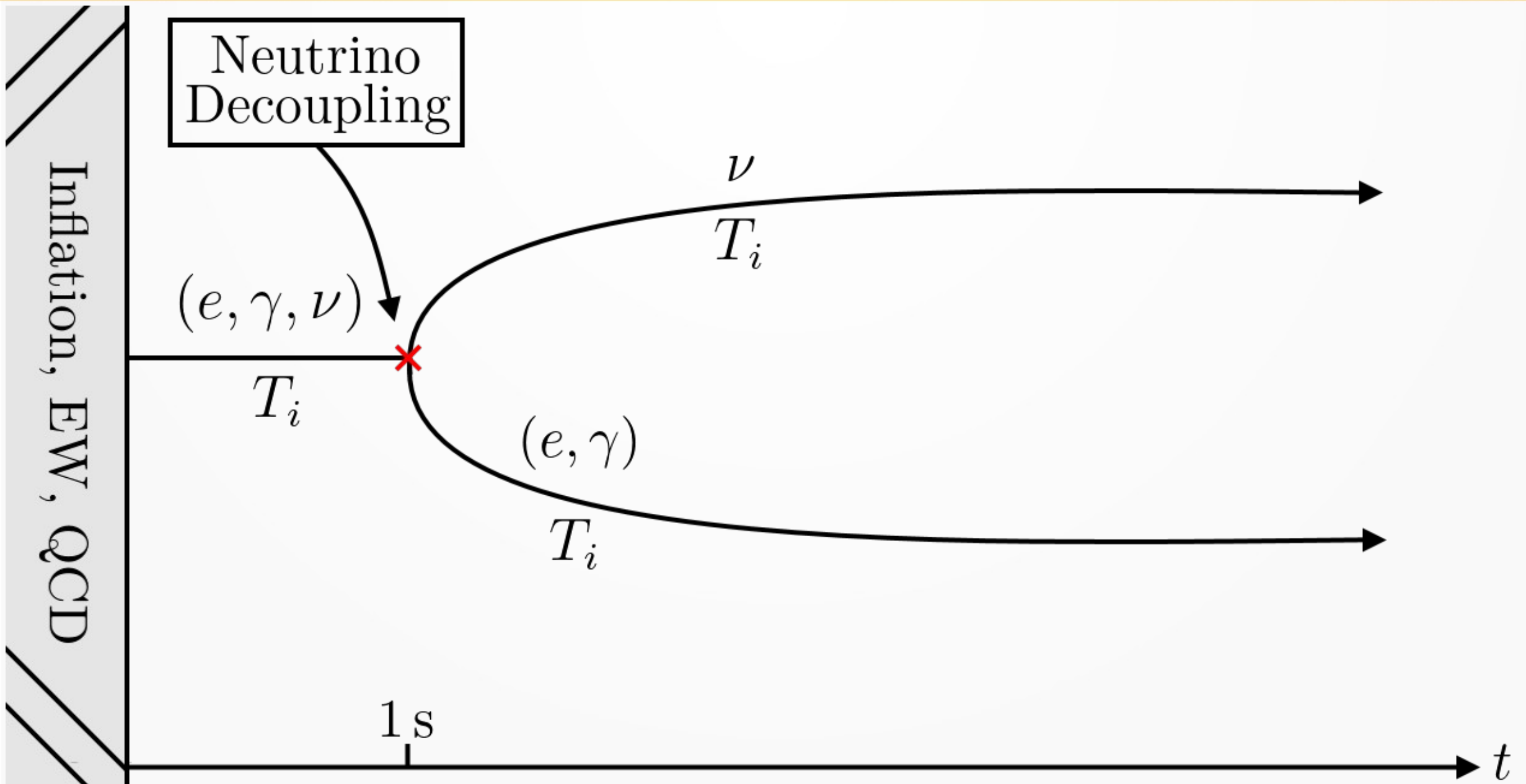
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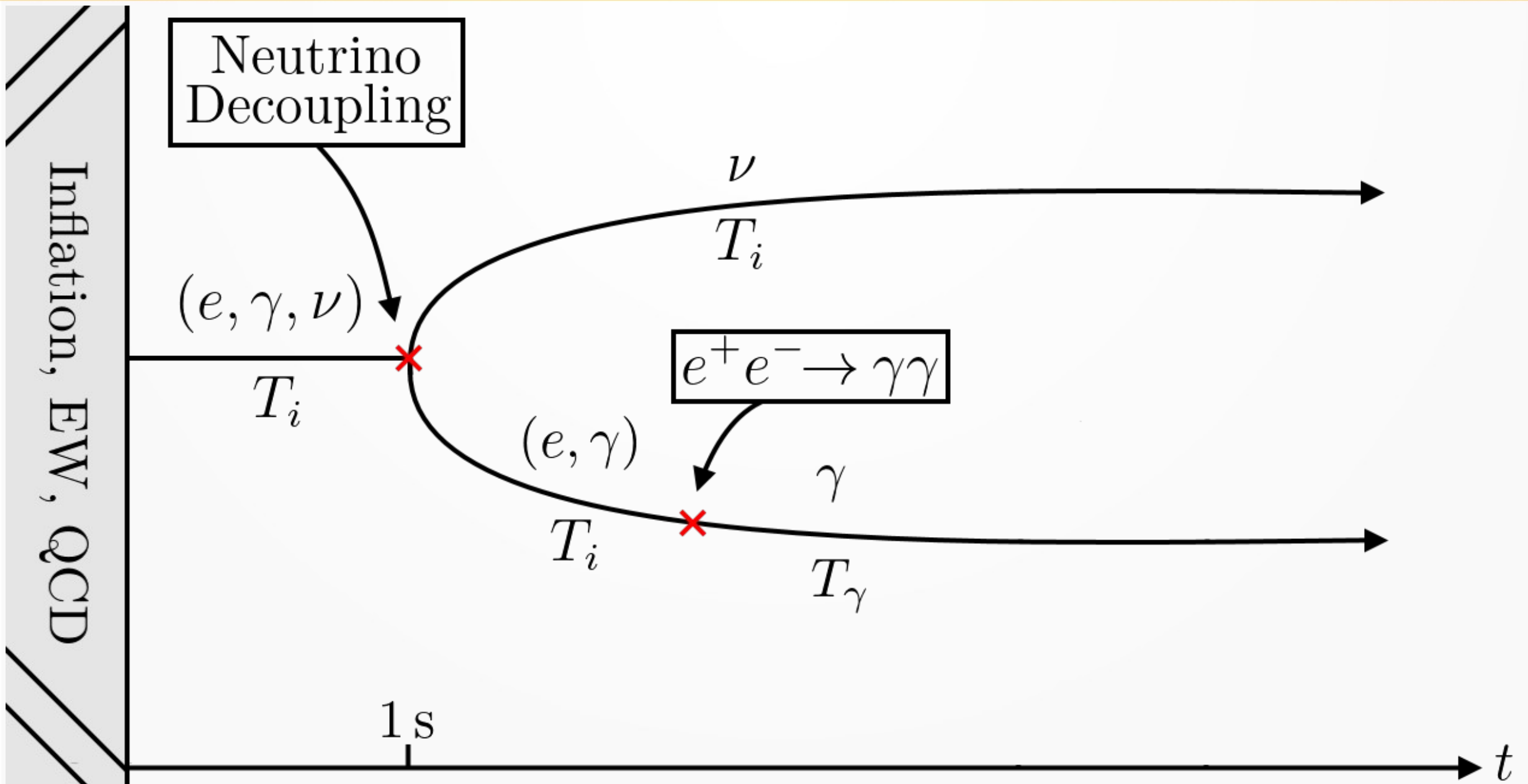
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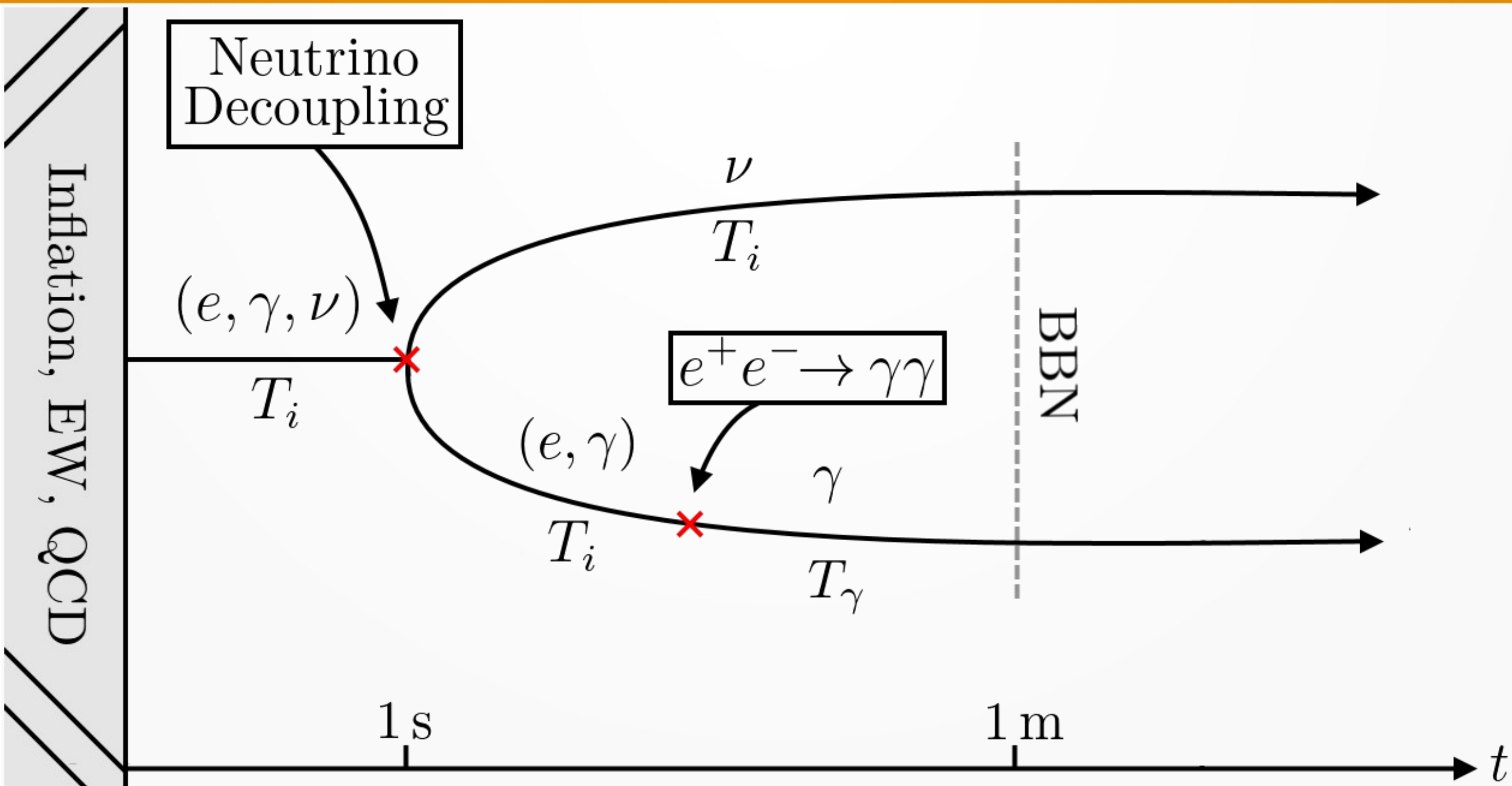
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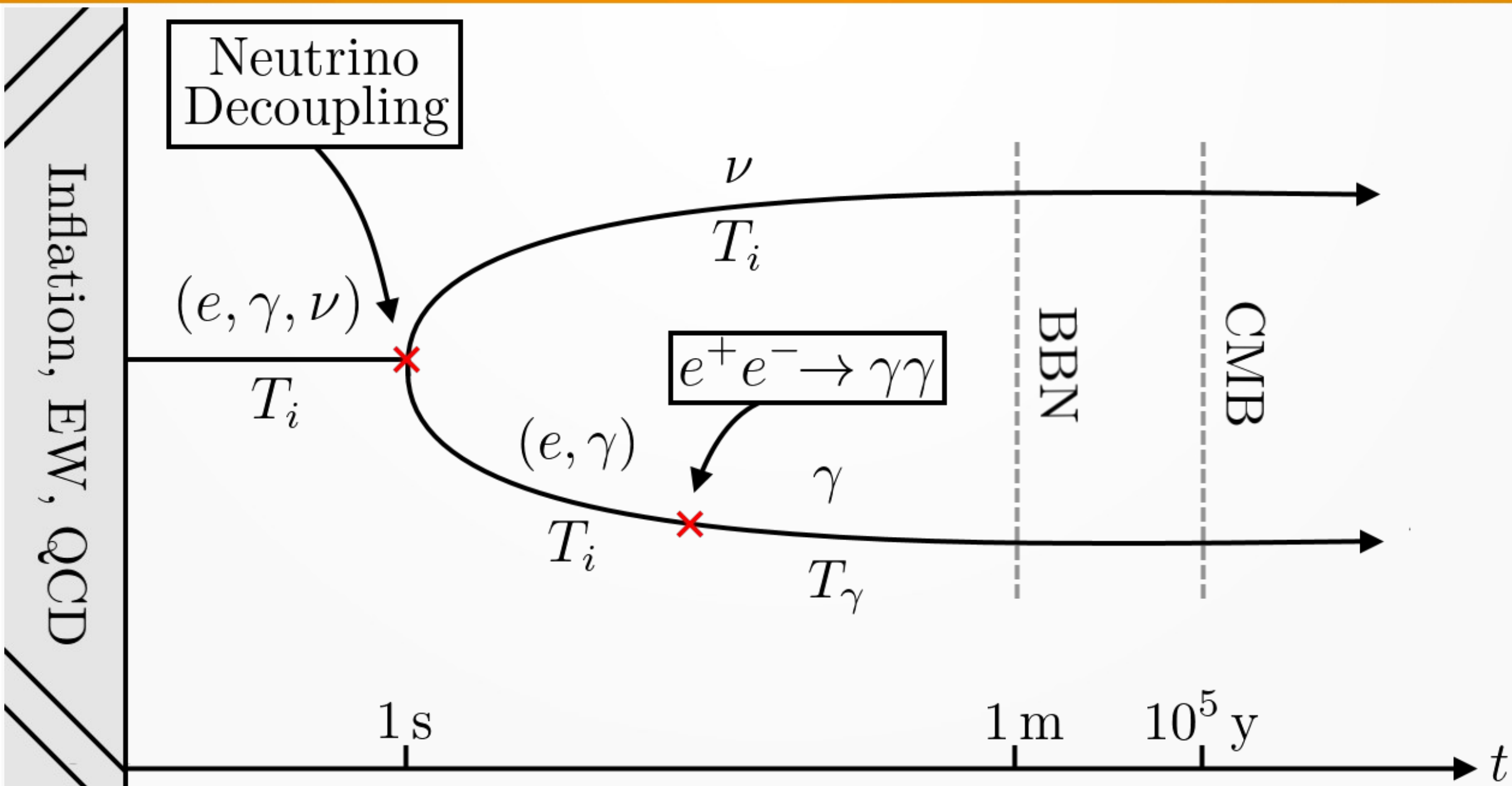
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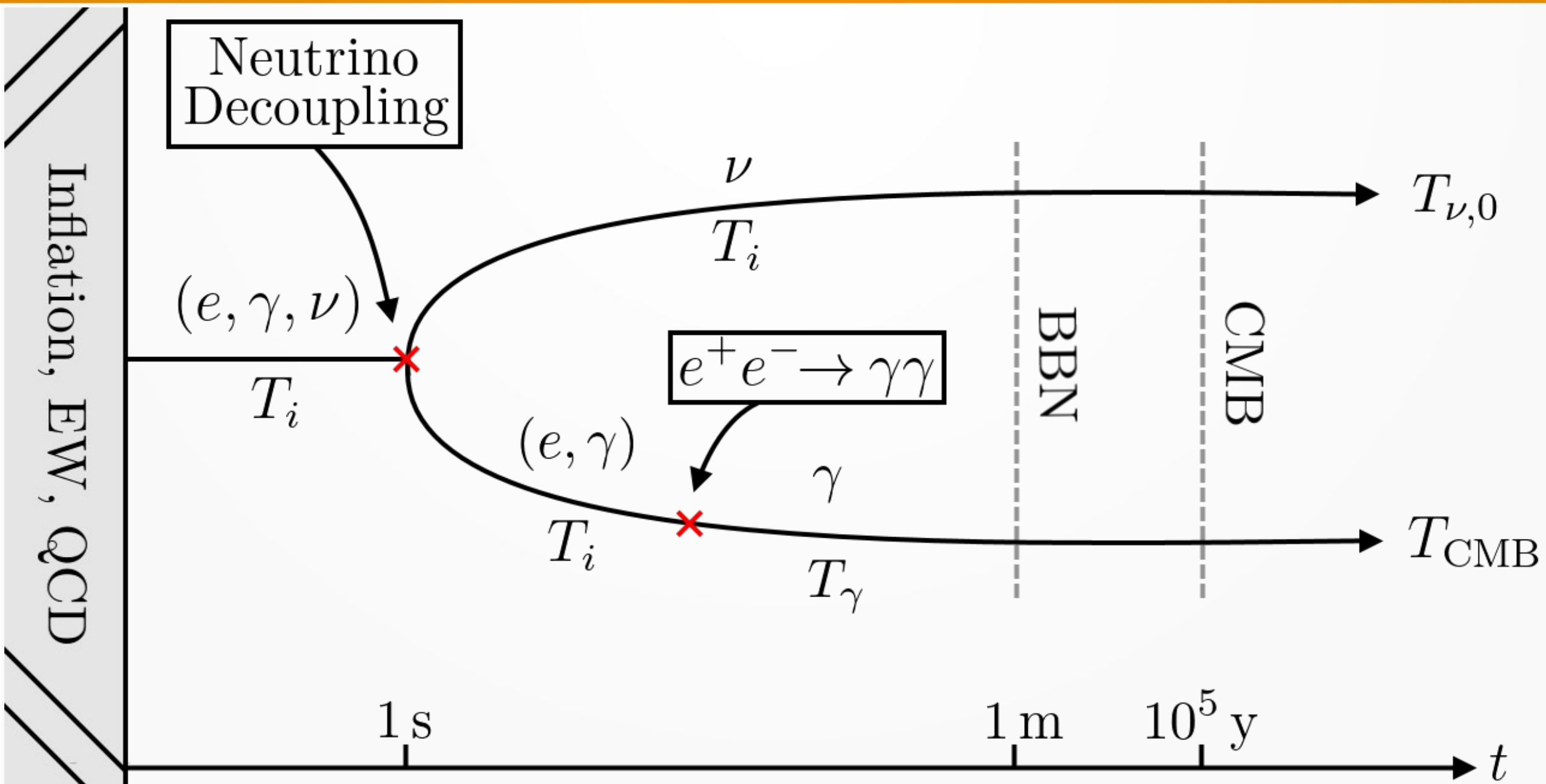
What is the CνB?



What is the CνB?



What is the CνB?



The CνB today

- Redshifted to temperature:

$$T_{\nu,0} = \left(\frac{4}{11}\right)^{\frac{1}{3}} T_{\text{CMB}}$$

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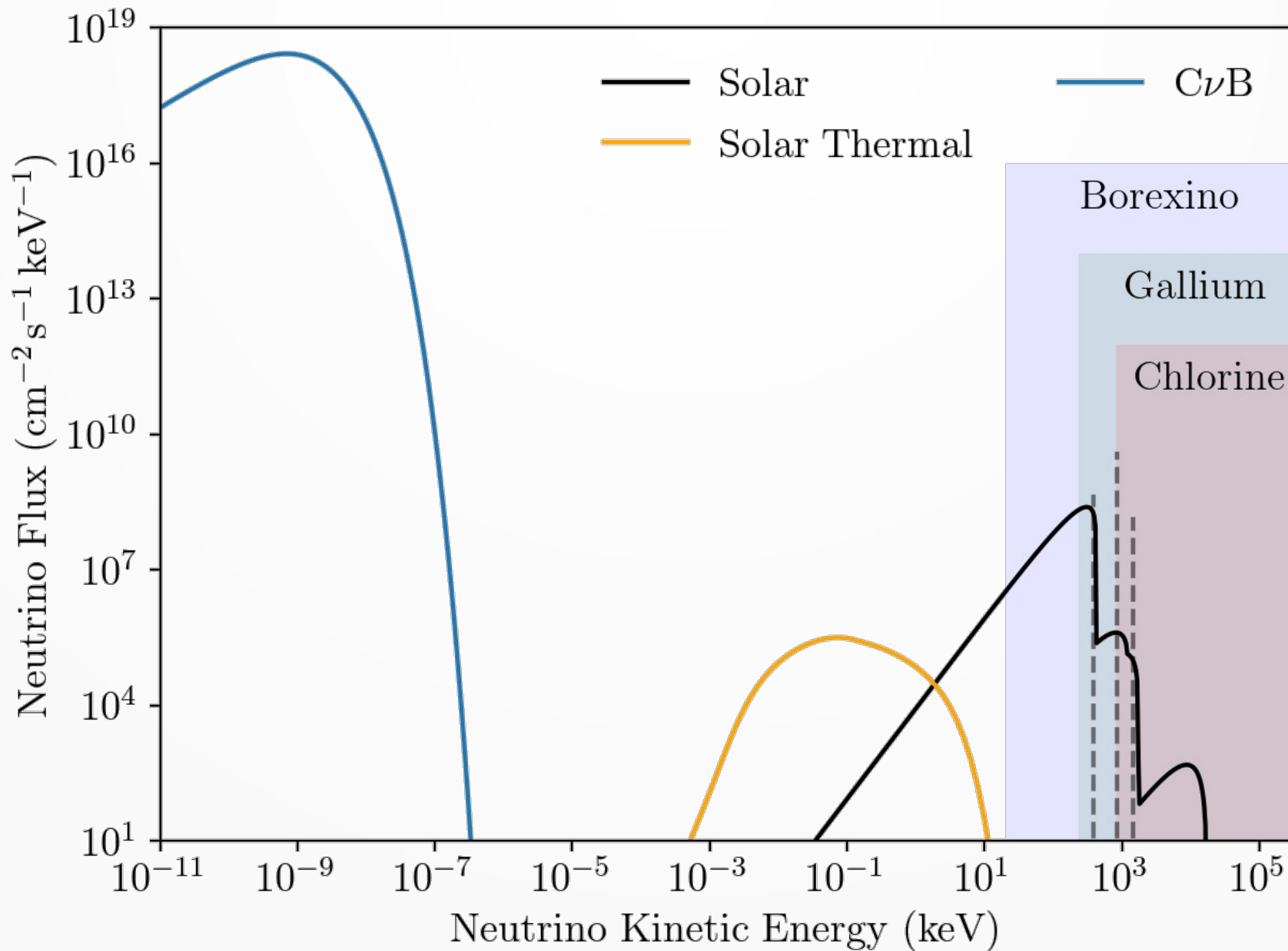
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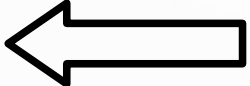
$$n_{\nu} = 56 \text{ cm}^{-3}$$

- May be overdense, *e.g.* clustering, decays to neutrinos

The CνB today



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How to detect the CvB

- Threshold:

-

-

- Event rate:

-

-

How to detect the CvB

- Threshold:
 - Look for thresholdless process
 -
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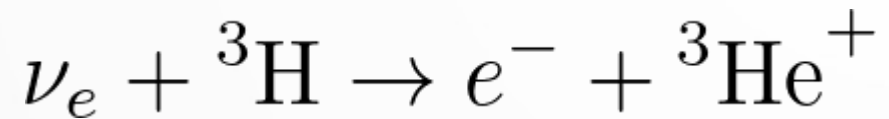
- Threshold:
 - Look for thresholdless process
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- Event rate:
 - Use a huge number of targets
 -

How to detect the CvB

- Threshold:
 - Look for thresholdless process
 - Find some way to bridge it
- Event rate:
 - Use a huge number of targets
 - Increase the cross section

The PTOLEMY experiment

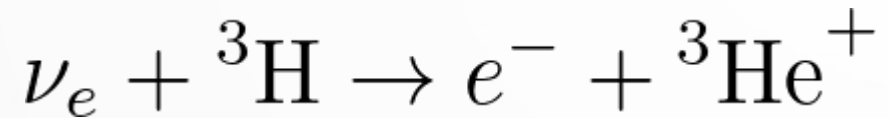
- Proposed by Weinberg in 1962 [1]:



[1] S. Weinberg, Phys. Rev. **128**, 1457 (1962)

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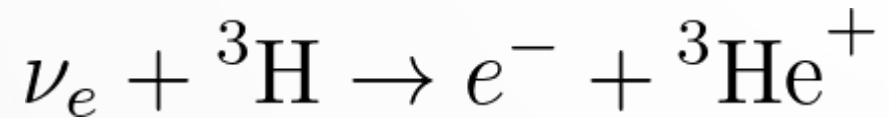
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The PTOLEMY experiment

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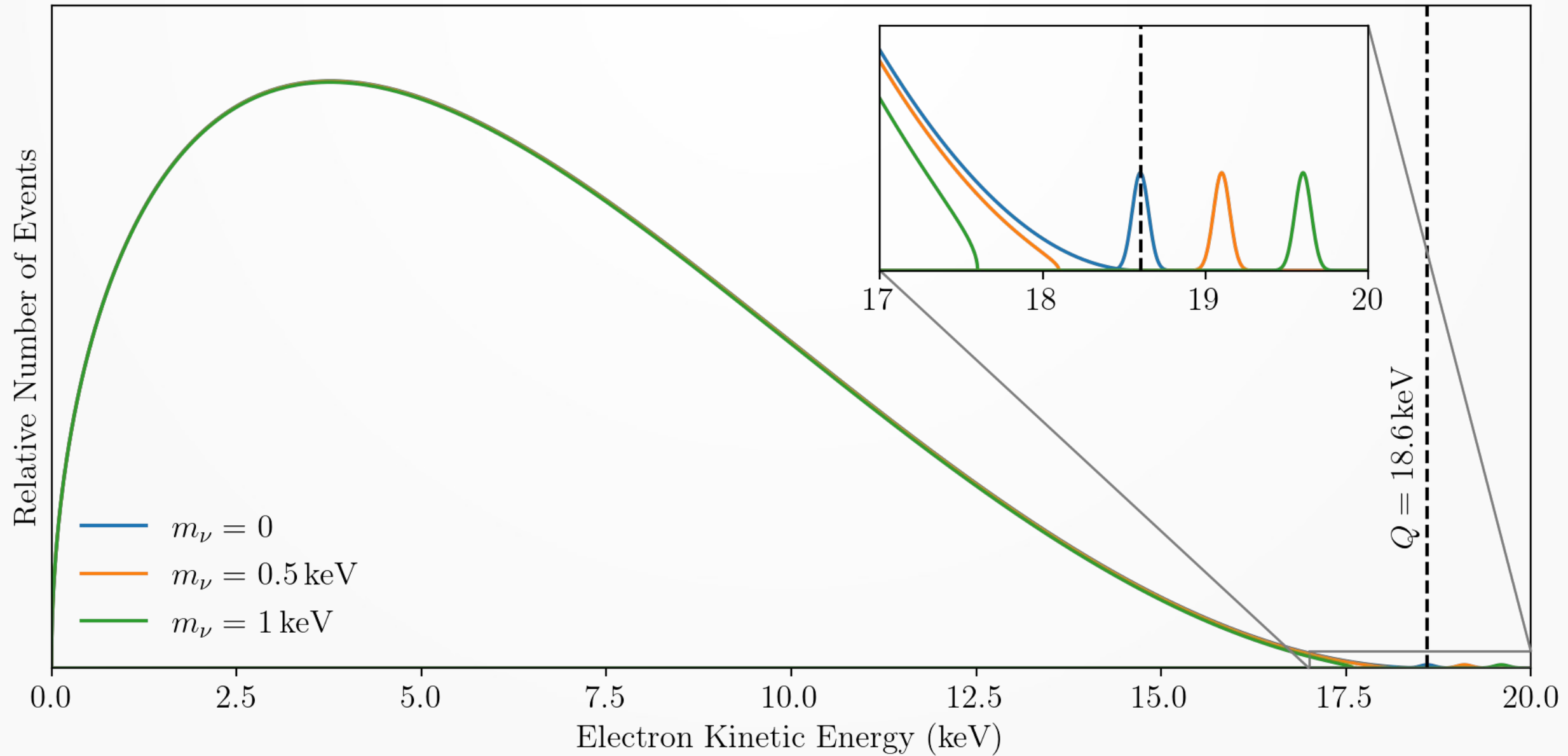


- This process has no threshold
- Tritium already well understood from neutrino mass experiments



[1] S. Weinberg, Phys. Rev. **128**, 1457 (1962)

PTOLEMY



The PTOLEMY experiment

- Neutrino capture cross section [2]:

$$\langle \sigma \beta_\nu \rangle \propto G_F^2 E_e p_e \sim 10^{-45} \text{ cm}^2$$

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- This event rate is doubled for Majorana neutrinos

What's the catch?

- Extreme sensitivity required to detect signal:

$$\Delta \leq 2m_\nu$$

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What's the catch?

- Extreme sensitivity required to detect signal:

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- Obtaining and storing 100g of tritium
- cf. KATRIN, uses $\sim 300\mu\text{g}$ of tritium [3]

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$$m_{\nu_h} \gtrsim 50 \text{ meV}$$

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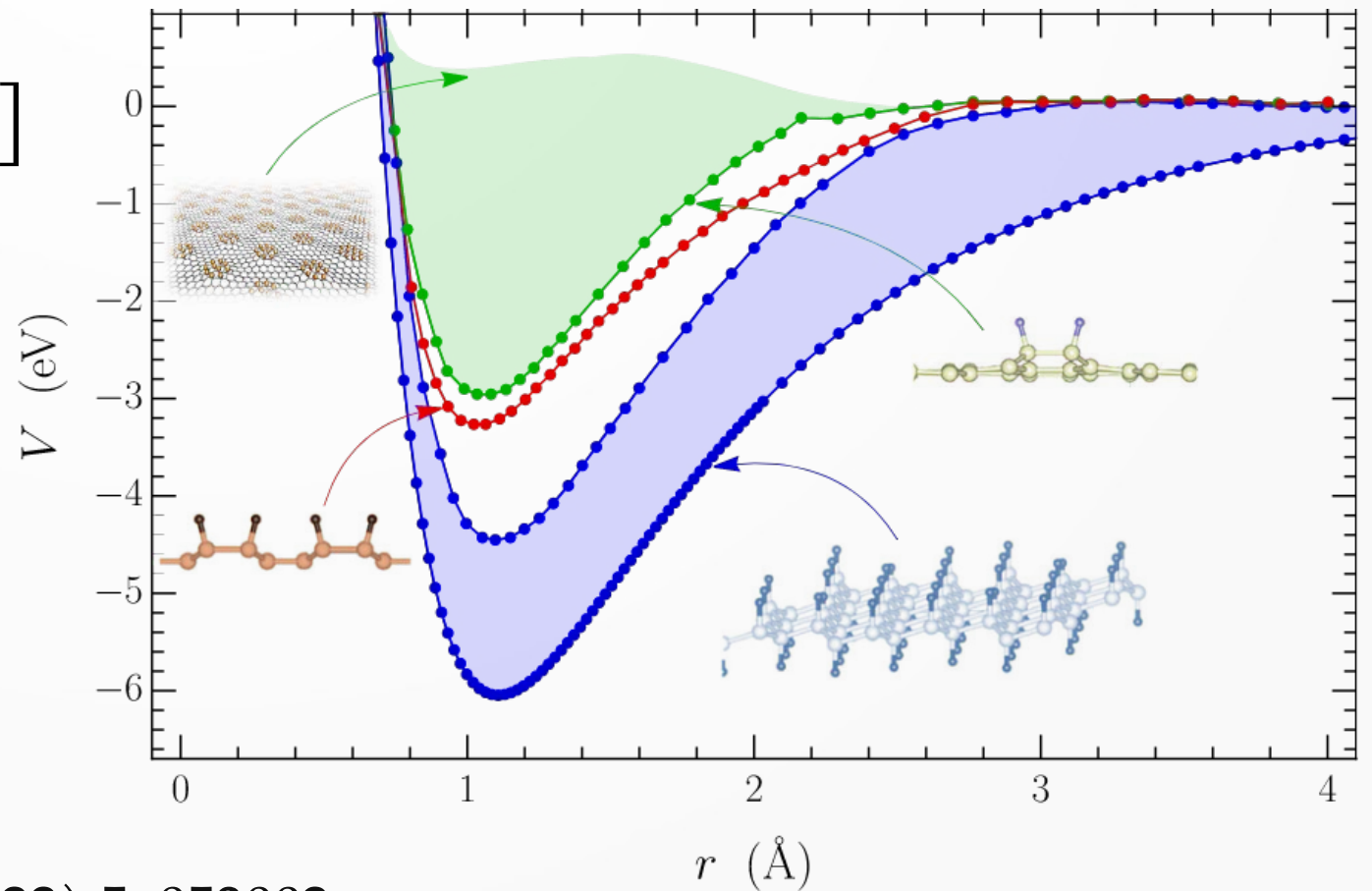
- PTOLEMY should at least see something!

What's the catch?

- Obtaining and storing 100g of tritium

What's the catch?

- Obtaining and storing 100g of tritium
- Graphene substrate [4]



[4] PTOLEMY, Phys. Rev. D **106** (2022) 5, 053002

What's the catch?

- Uncertainty principle:

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$$\Delta x \simeq 0.1 \text{ \AA}$$

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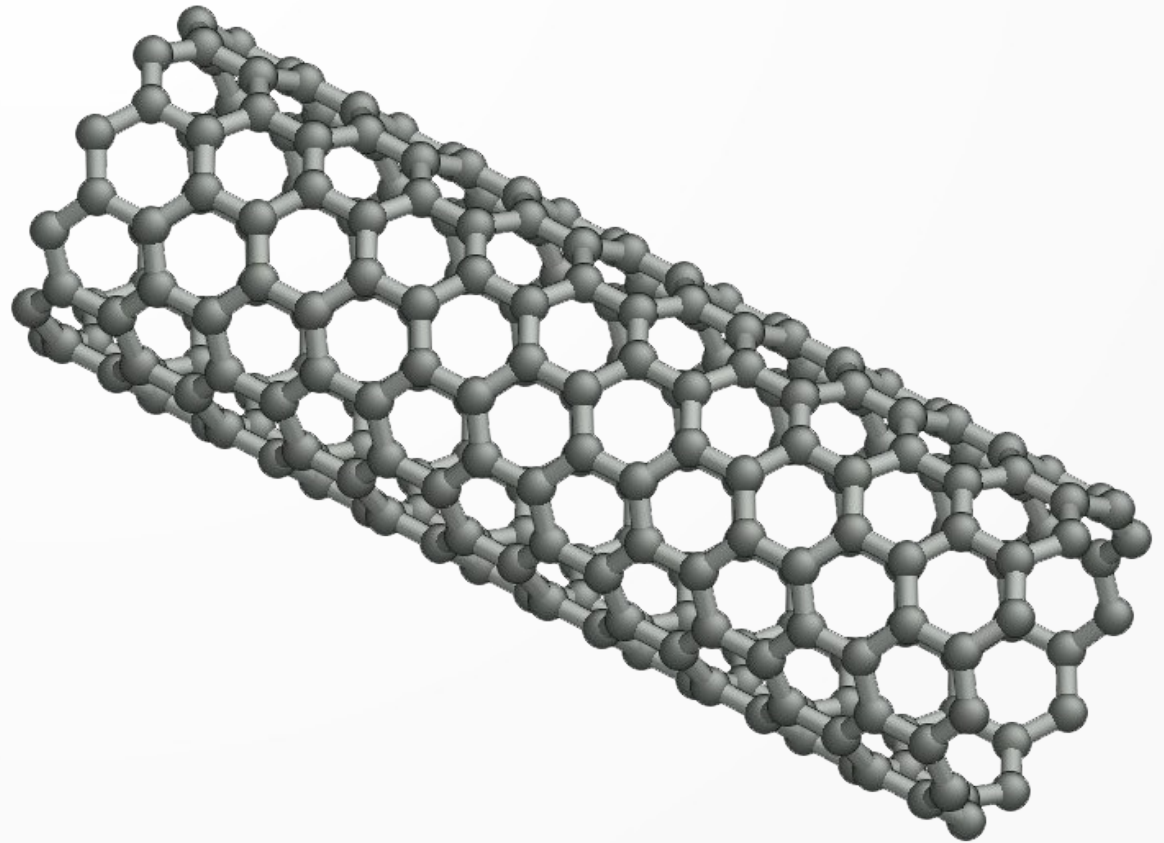
$$\Delta E_e \simeq 480 \text{ meV}$$

$$\Delta E_e \gg 2m_{\nu_h}$$

- No longer guaranteed to see anything!

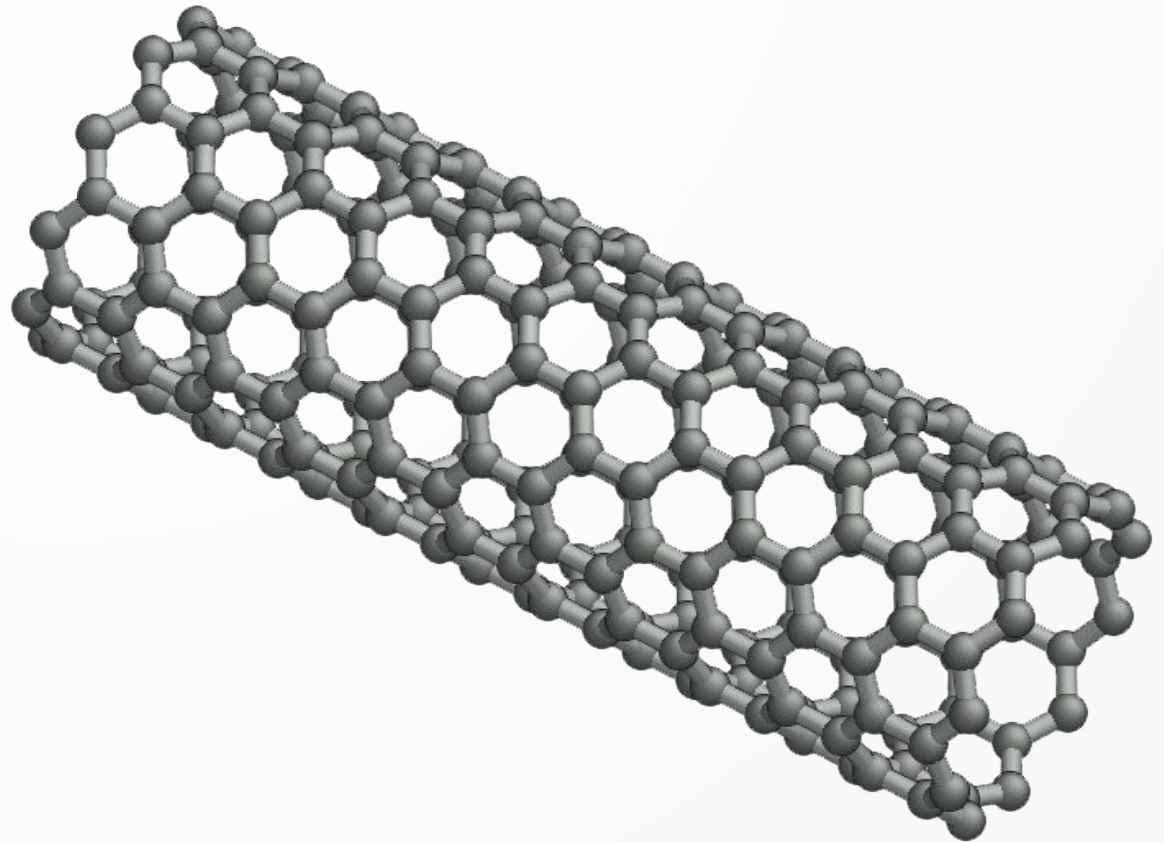
So now what?

- Carbon nanotubes?



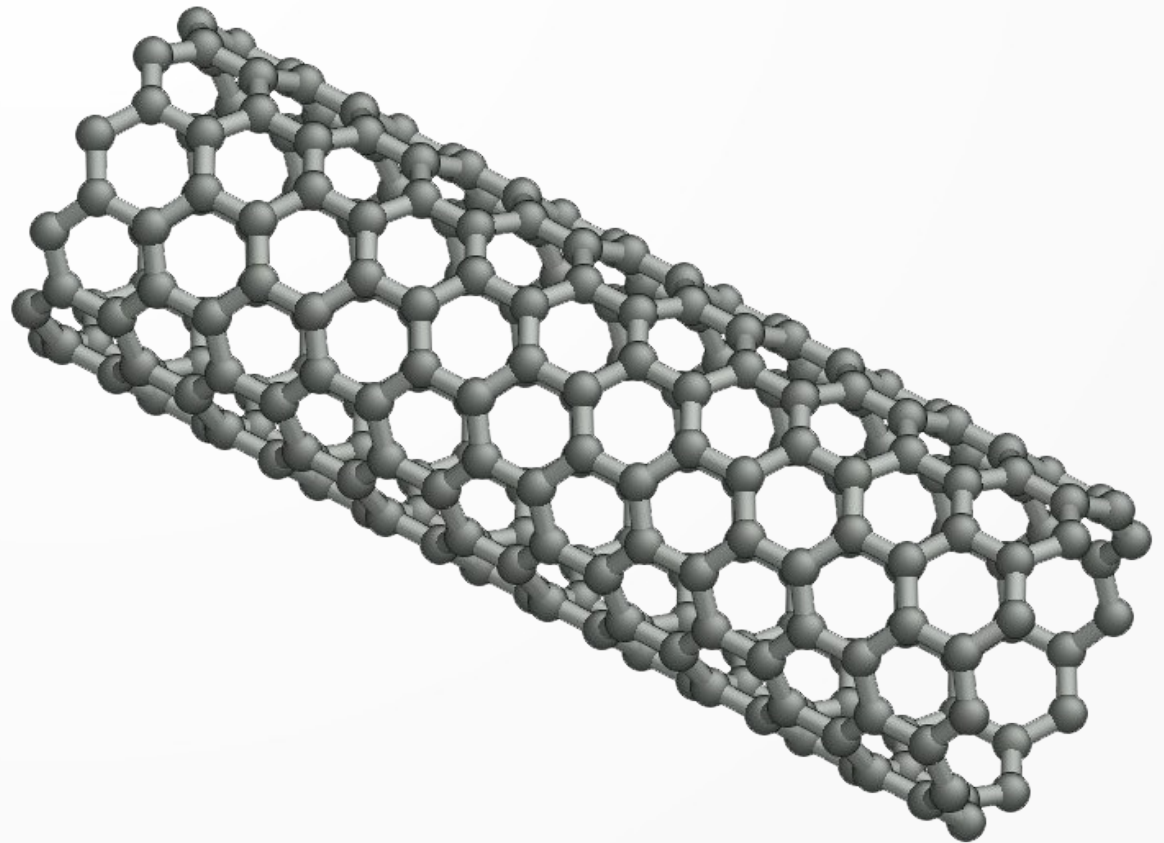
So now what?

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So now what?

- Carbon nanotubes?
- Allow tritium to *slide*
- Increases Δx !



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Coherent scattering

- Coherent scattering (Opher '74, ... , JS '21):

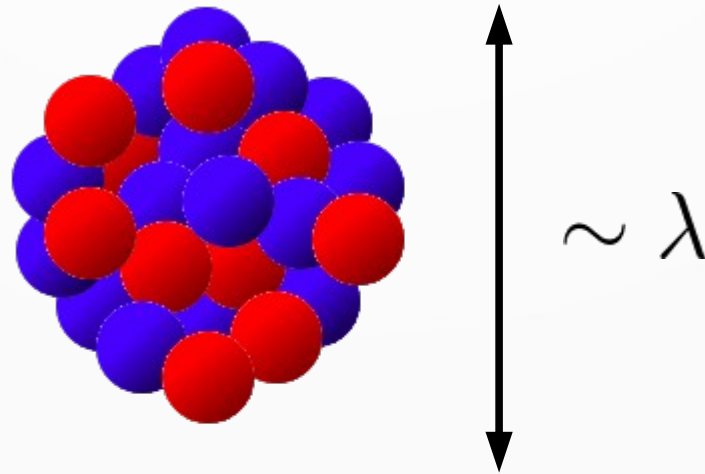
$$\nu + X \rightarrow \nu + X$$

Coherent scattering

- Coherent scattering (Opher '74, ... , JS '21):

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- Wavelength of order target size:



Coherent scattering

- Neutrino “sees” a larger charge:

$$\mathcal{M} \sim Q_T \qquad Q_T \sim N_T$$

Coherent scattering

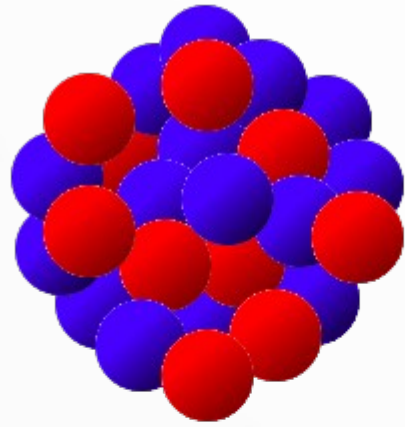
- Neutrino “sees” a larger charge:

$$\mathcal{M} \sim Q_T \qquad Q_T \sim N_T$$

- Significantly enhanced event rates:

$$\Gamma \sim N_T \longrightarrow \Gamma_{\text{coh}} \sim N_T^2$$

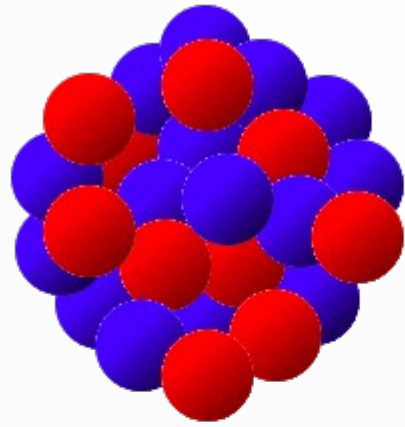
Coherent scattering



$$\lambda \sim \text{fm}$$

$$\Gamma \sim (A - Z)^2$$

Coherent scattering



$$\lambda \sim \text{fm}$$

$$\Gamma \sim (A - Z)^2$$



$$\lambda \sim \text{mm}$$

$$\Gamma \sim N_A^2$$

Coherent scattering

- Neutrino scattering rate:

$$\frac{\Gamma}{N_T} \simeq G_F^2 m_\nu^2 T_{\nu,0}^3$$

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- So why don't we see anything?

Coherent scattering

- Relic neutrinos are cold and light:

$$\Delta p_\nu \sim \mathcal{O}(\text{meV})$$

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$$a_\nu \simeq 10^{-28} \left(\frac{m_\nu}{0.1 \text{ eV}} \right)^2 \text{ cm s}^{-2}$$

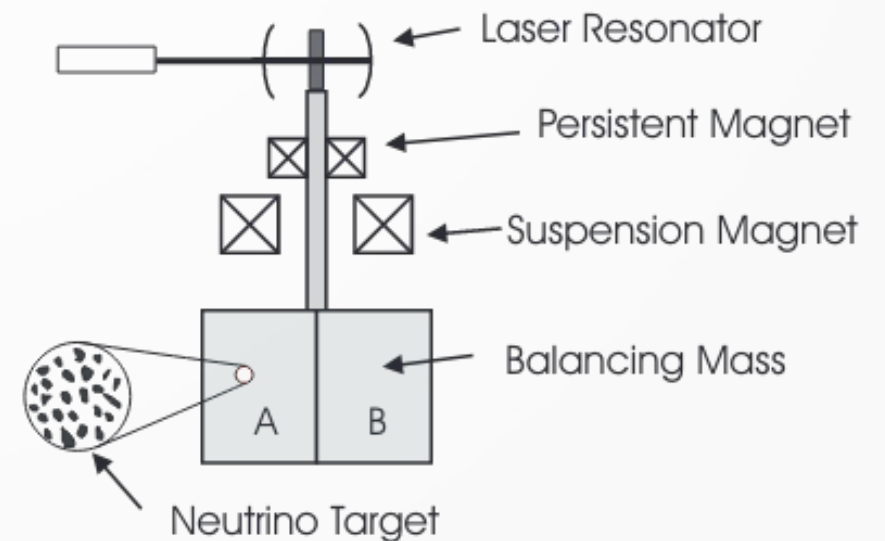


Fig: C. Hagmann, arXiv:astro-ph/9905258

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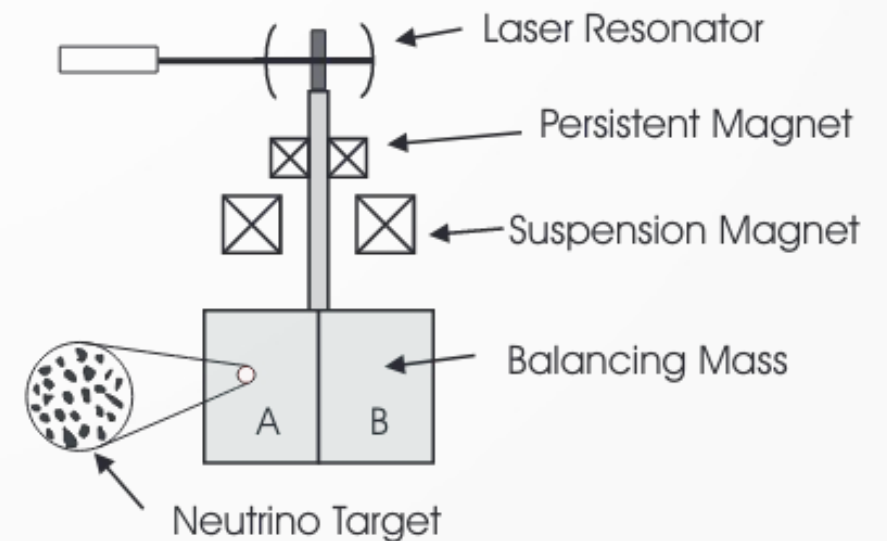


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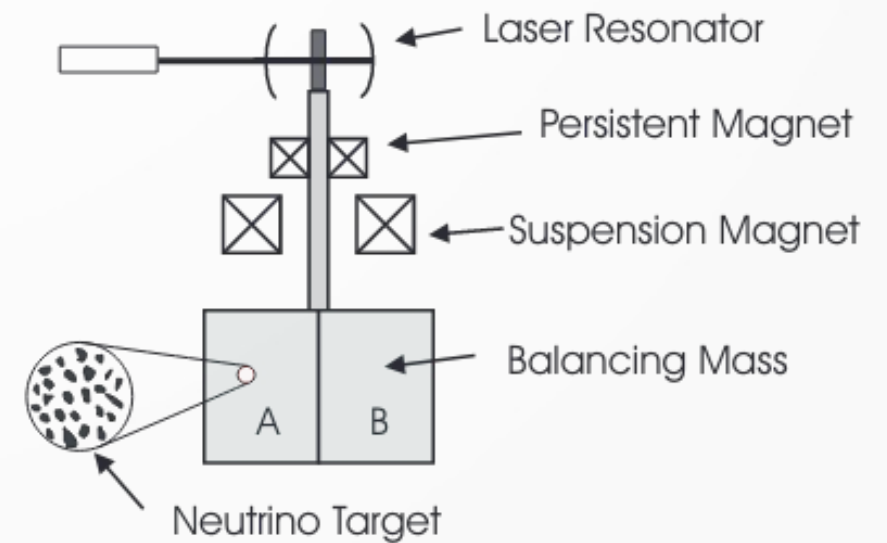
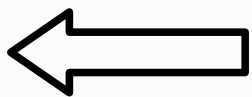


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Stodolsky effect

- Stodolsky effect (Stodolsky '75, Duda '01, JS '23)

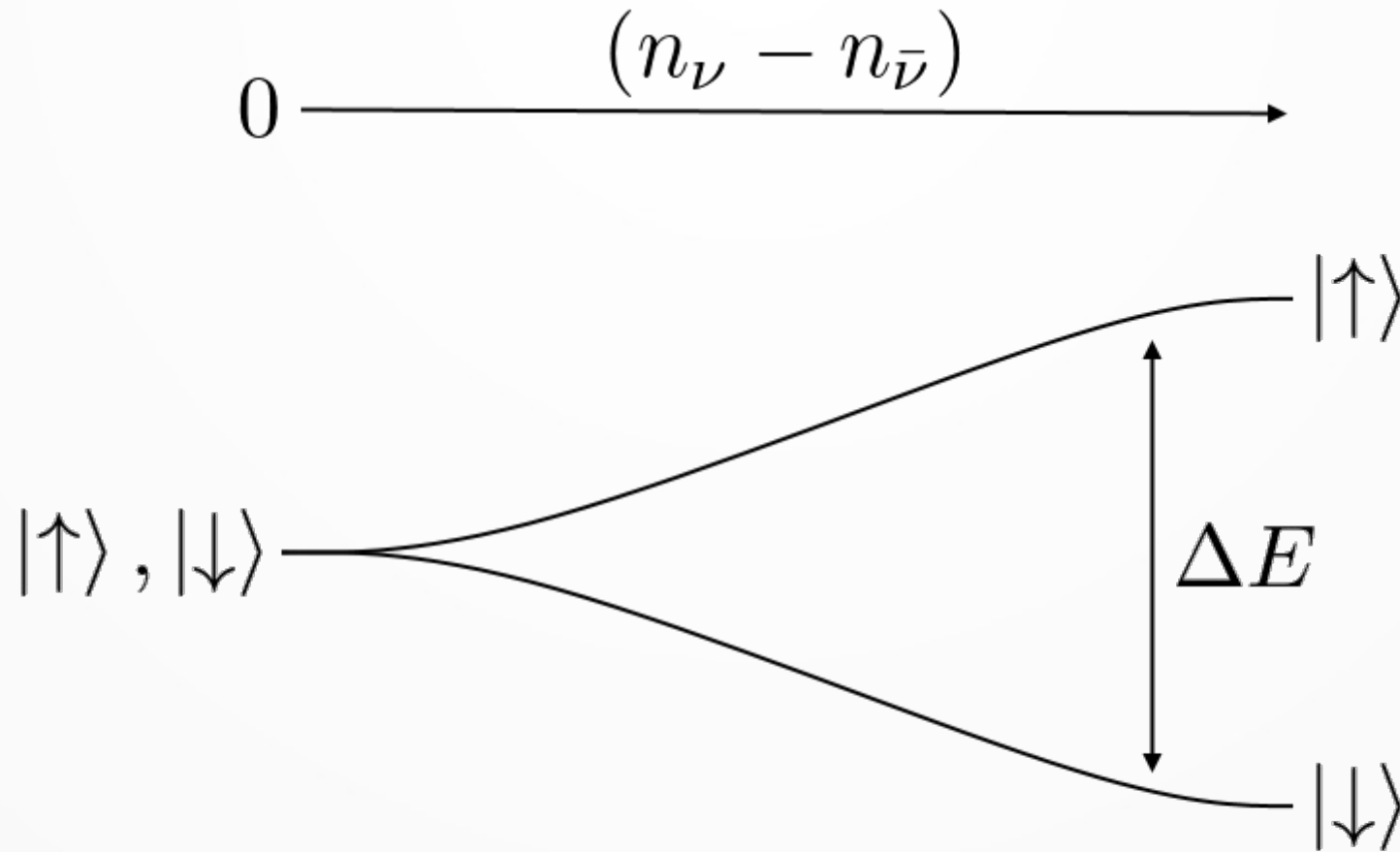
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- Analogous to the Zeeman effect

Stodolsky effect

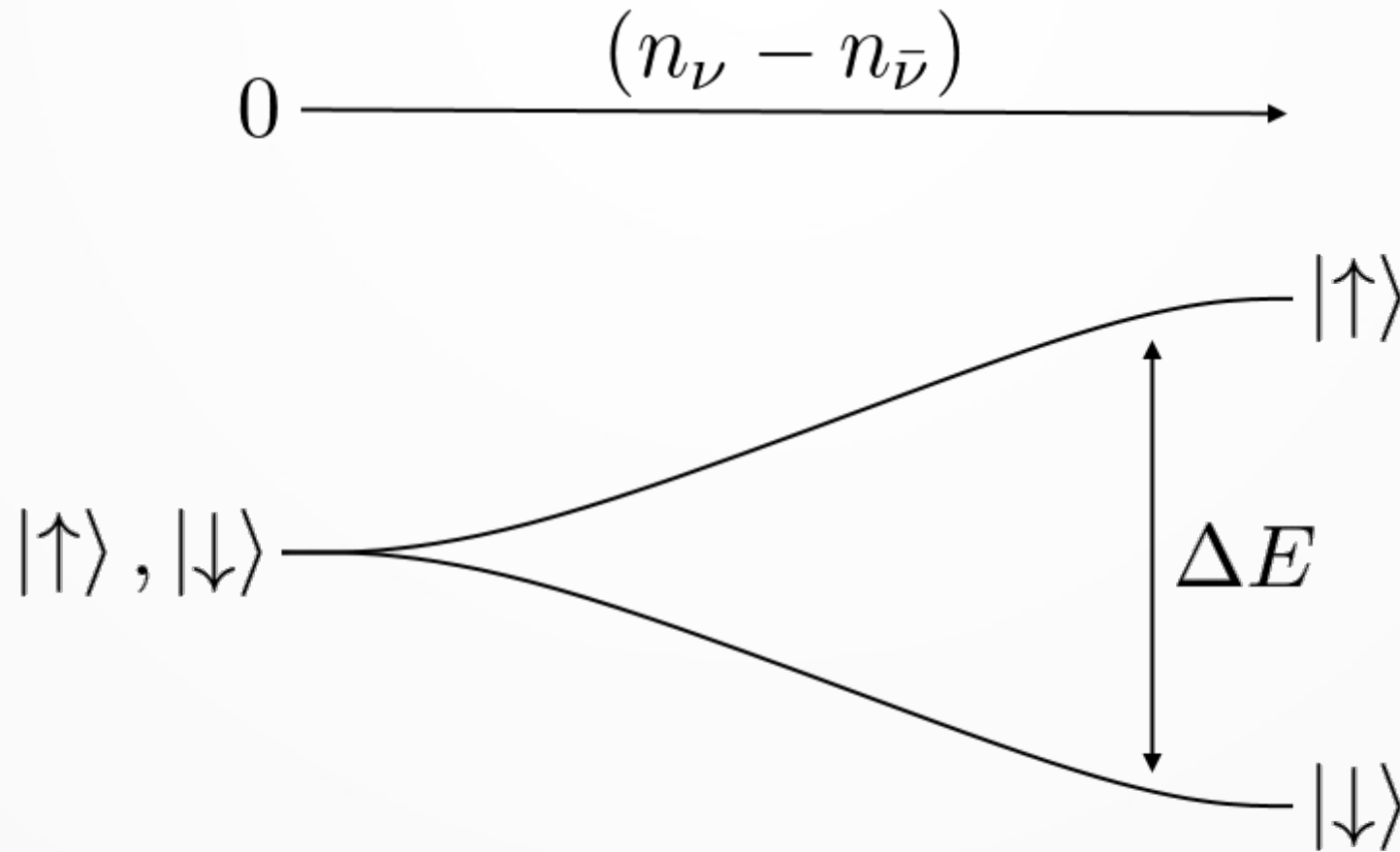
- Stodolsky effect (Stodolsky '75, Duda '01, JS '23)
- Analogous to the Zeeman effect
- Only* effect linear in G_F (Cabibbo '82, Langacker '83)

Stodolsky effect



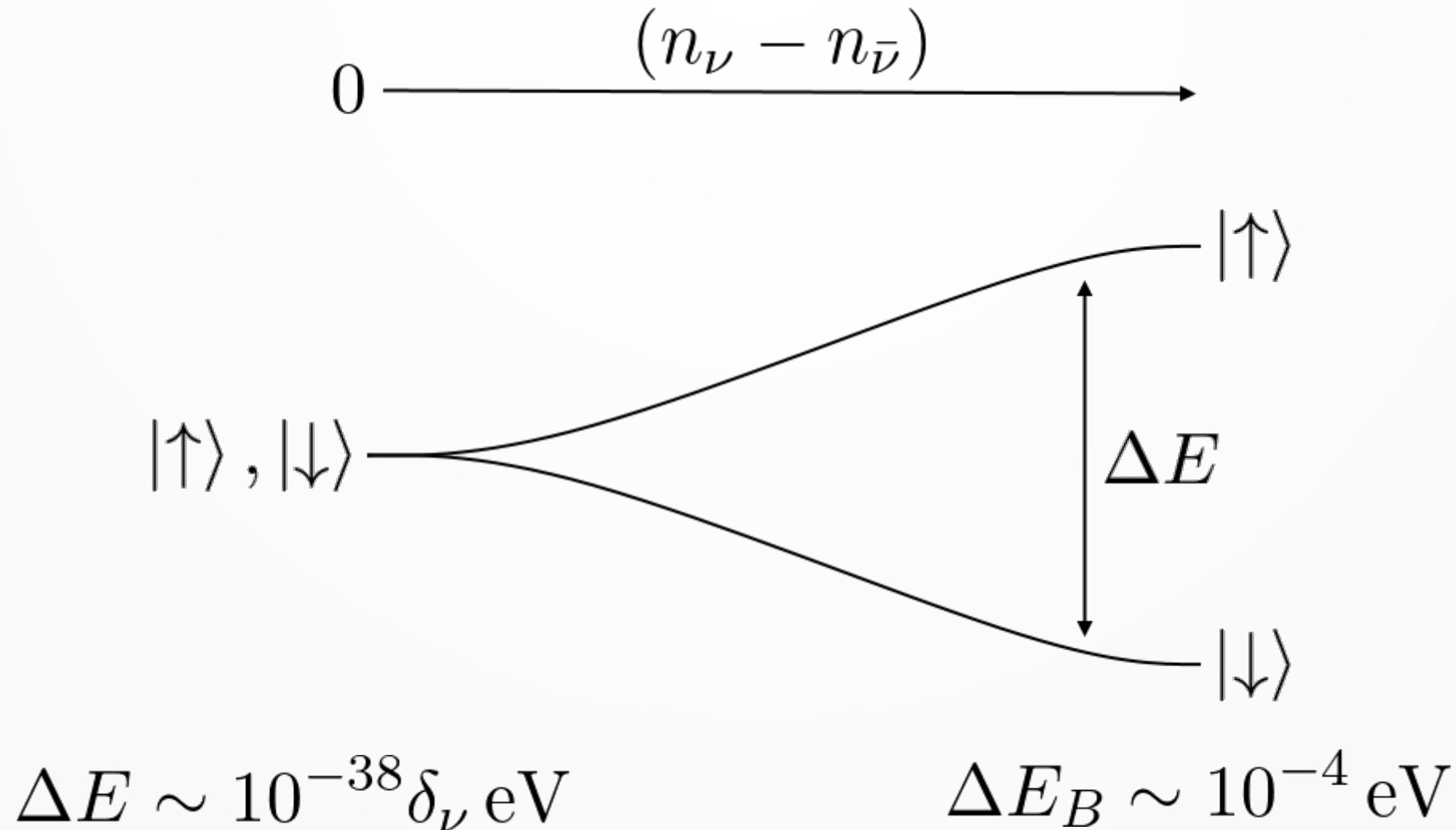
$$\Delta E \sim G_F \beta_{\oplus} (n_\nu - n_{\bar{\nu}})$$

Stodolsky effect

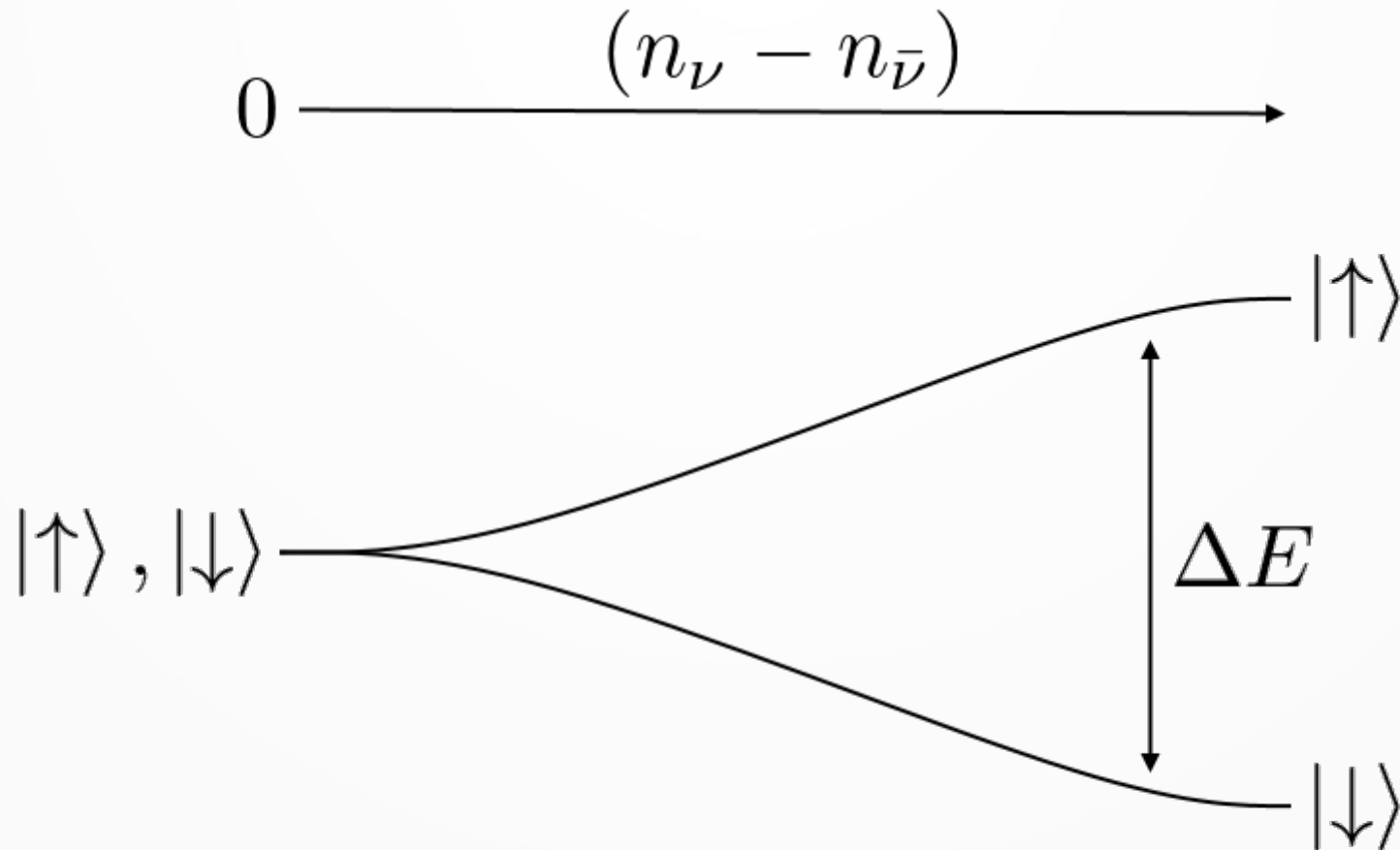


$$\Delta E \sim 10^{-38} \delta_\nu \text{ eV}$$

Stodolsky effect



Stodolsky effect



- Also an effect that depends on helicity asymmetry

Stodolsky effect

- So how do we see it?

Stodolsky effect

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- Spin precession:

$$\frac{dS_{\perp}}{dt} = i[H, S_{\perp}] \neq 0$$

Stodolsky effect

- Two observables:
- Torque [6]:

$$\tau \simeq \Delta E$$

Stodolsky effect

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$$\tau \simeq \Delta E \longrightarrow a_\nu \simeq 10^{-27} \delta_\nu \text{ cm s}^{-2}$$

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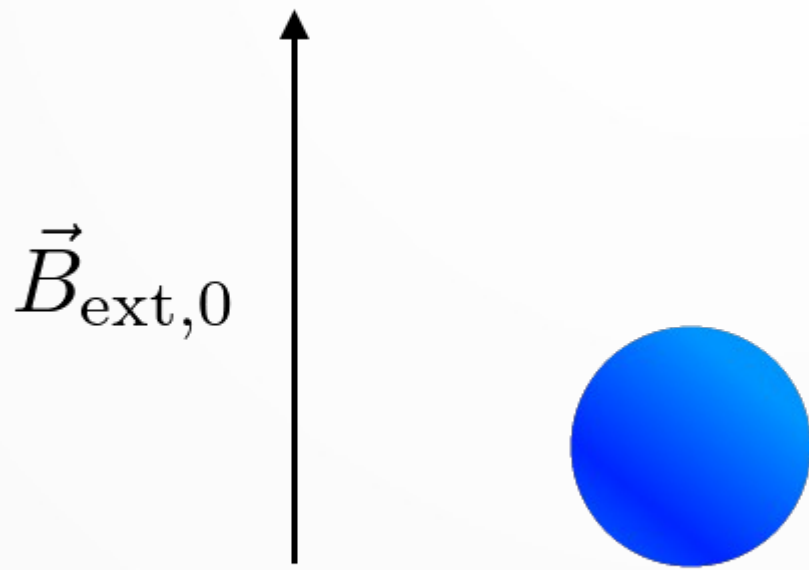
- Two observables:
- Magnetisation [6]:

$$\frac{dS_{\perp}}{dt} \neq 0 \implies \frac{dB_{\perp}}{dt} \neq 0$$

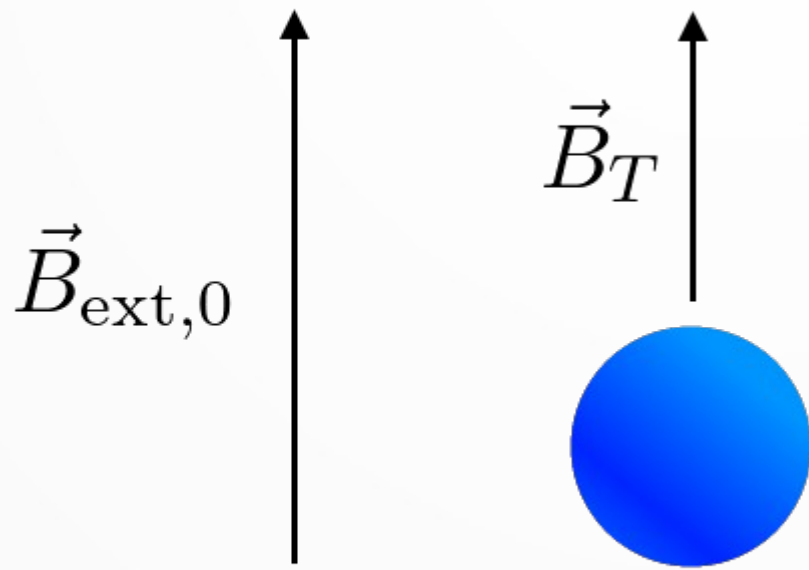
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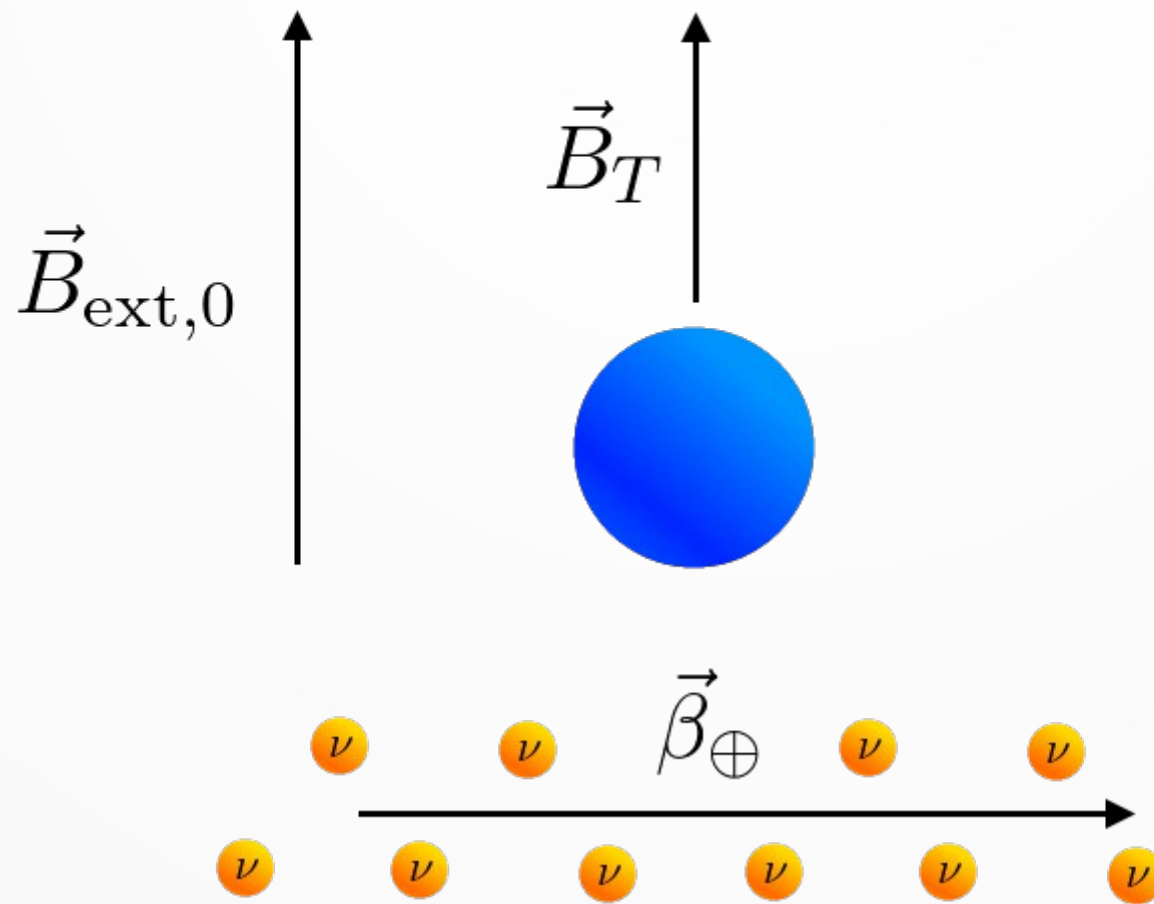
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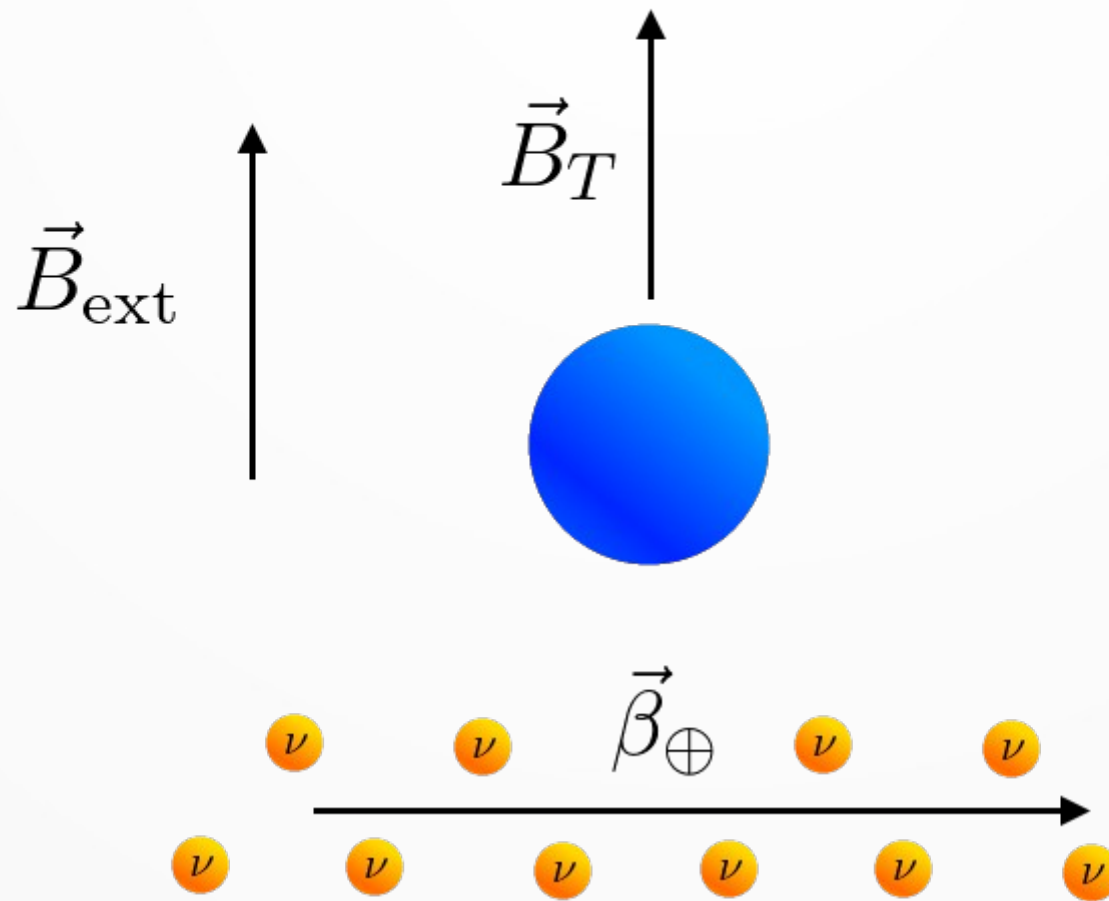
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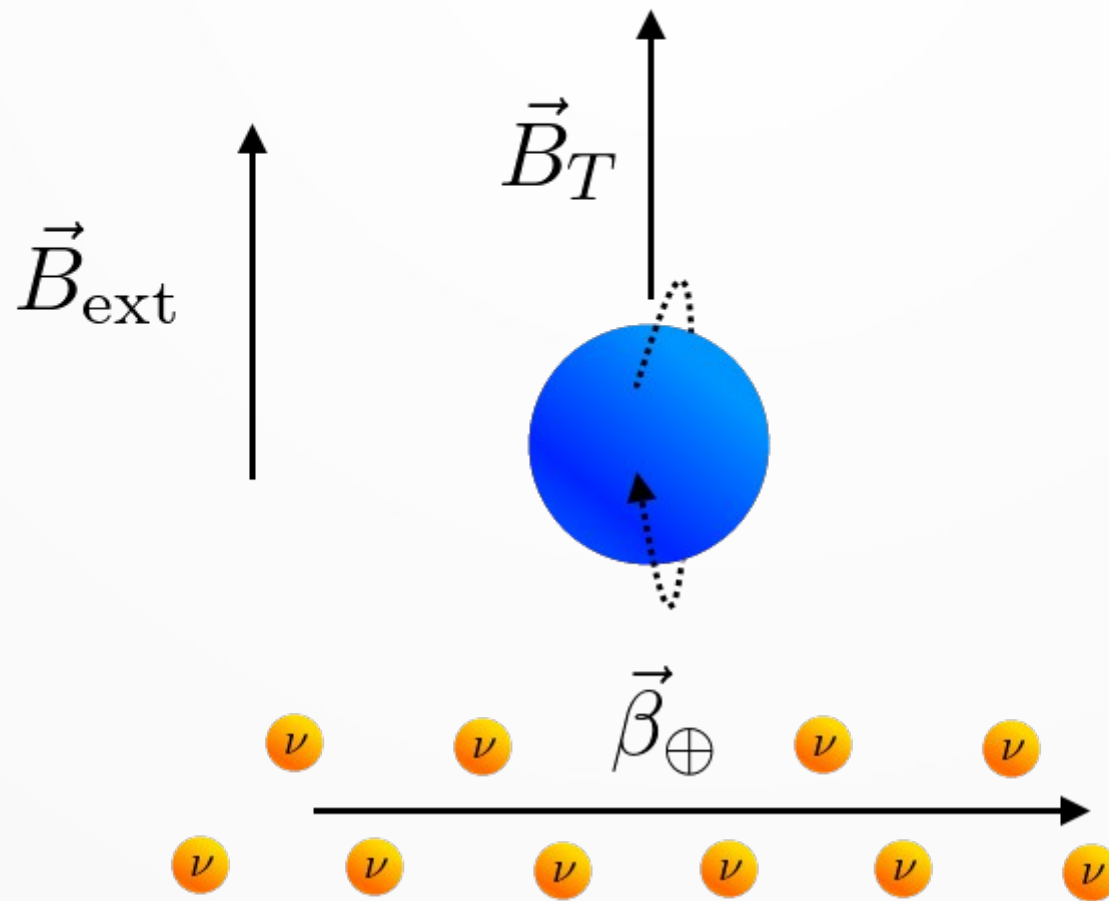
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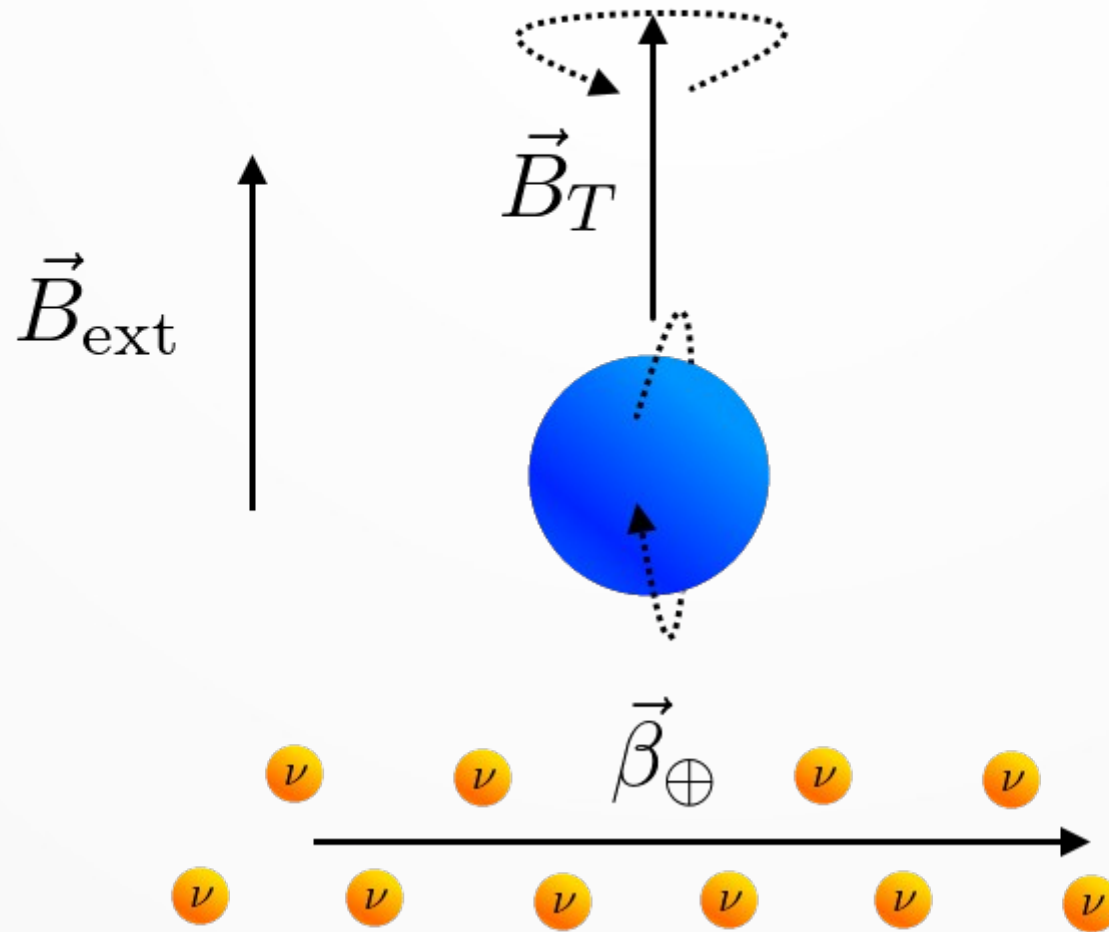
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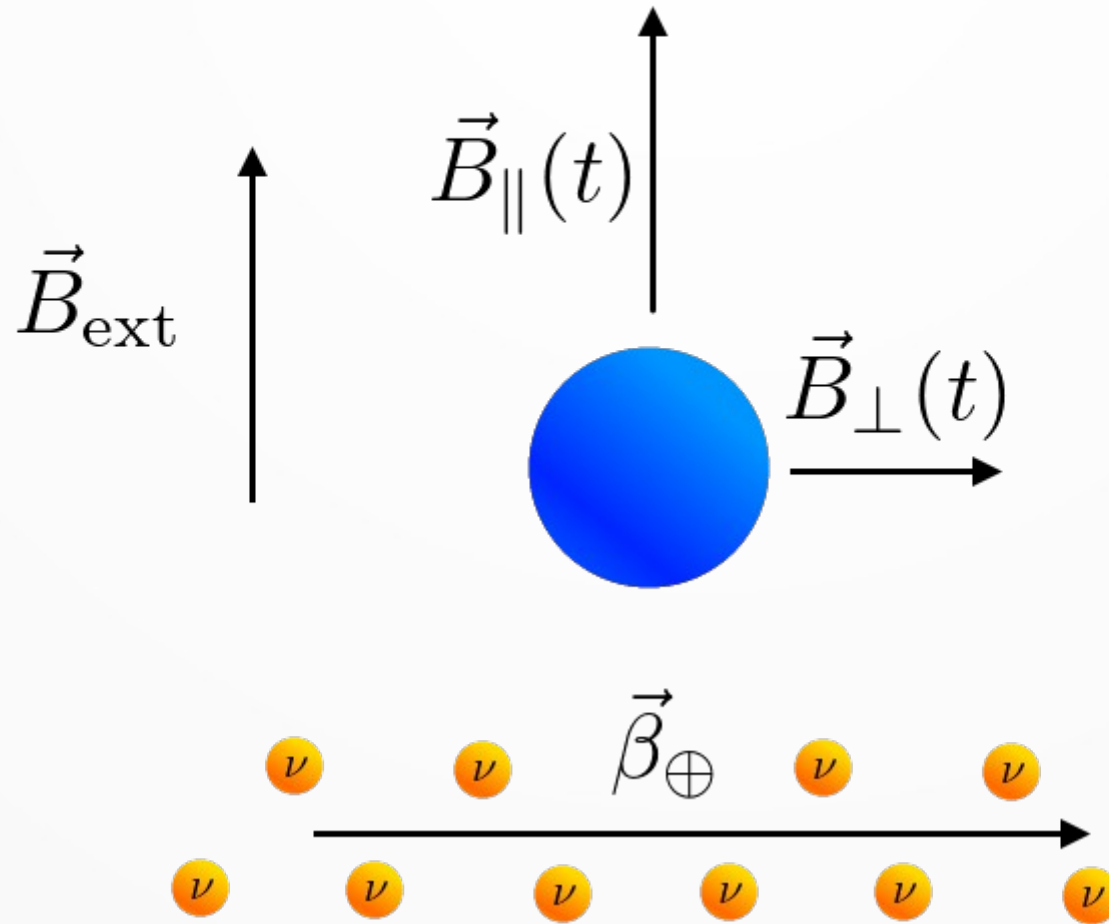
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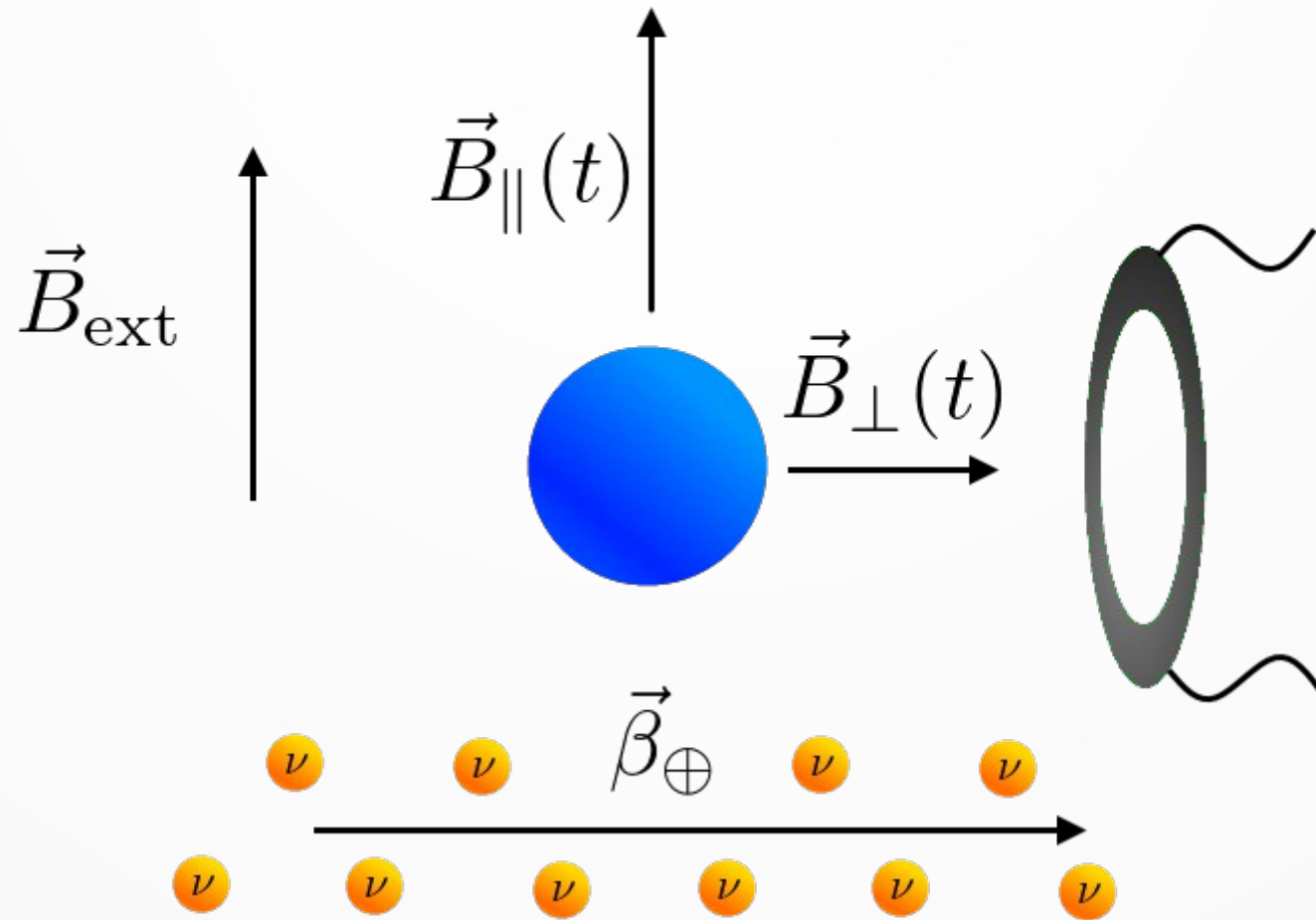
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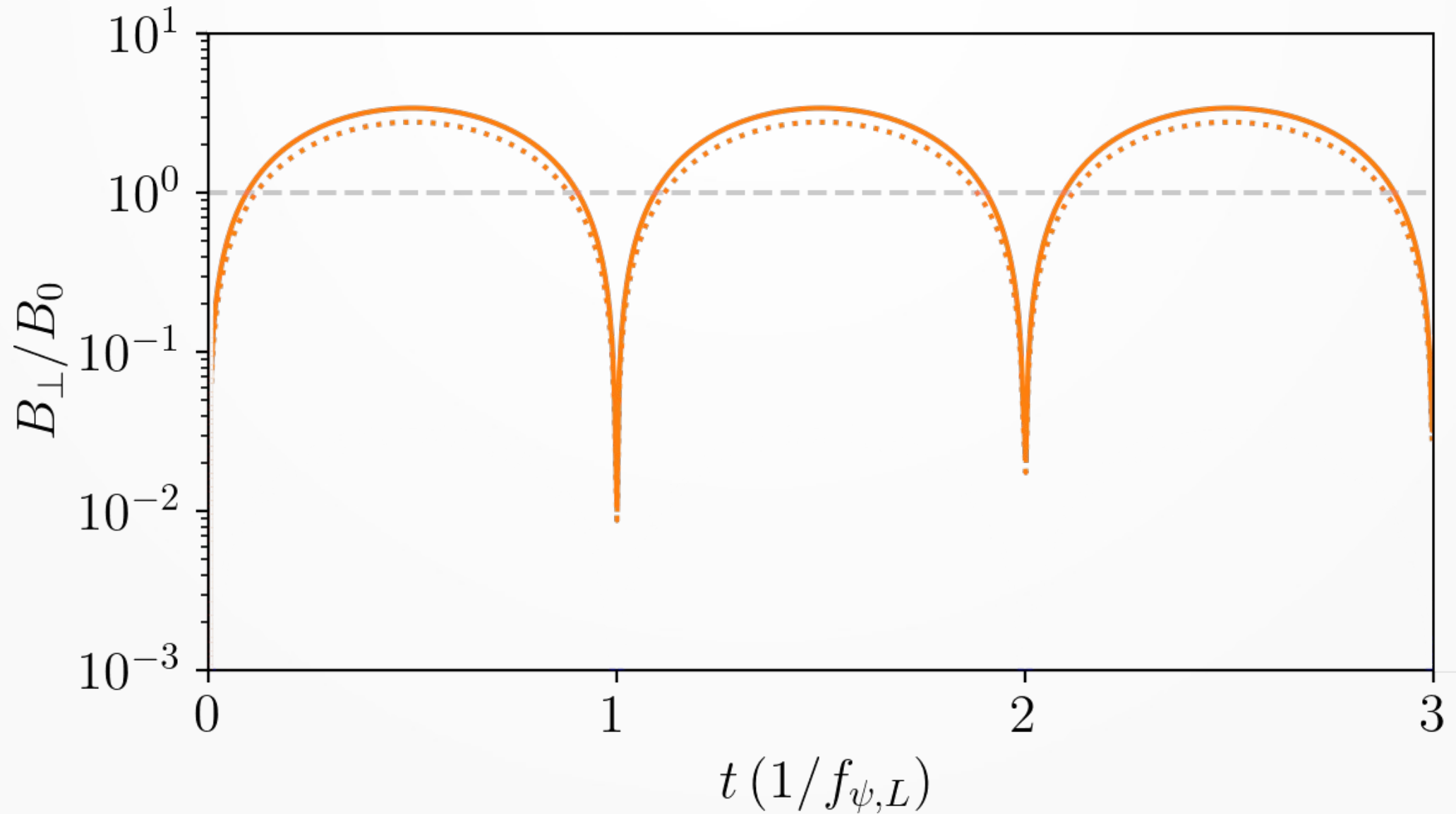
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- Helicity asymmetry term? 3 orders of magnitude larger!

Stodolsky effect

- Asymmetry?

Stodolsky effect

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- BBN constraint:

$$\delta_\nu = \delta_h \lesssim 10^{-2}$$

Stodolsky effect

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Stodolsky effect

- Asymmetry?
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- Still a way off, but better than coherent

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Accelerator

- PTOLEMY-on-a-beam?

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$$\langle \sigma \beta_\nu \rangle \propto G_F^2 E_e p_e \sim 10^{-45} \text{ cm}^2$$

- Doesn't really work...

$$E_\nu = \frac{m_\nu}{M} E_{\text{beam}} \implies E_{\text{beam}} \sim \mathcal{O}(\text{PeV})$$

- Thresholded processes?

Accelerator

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- Vastly larger cross section: $\sigma \propto \frac{1}{M_Z^2} \propto G_F$

Accelerator

- Accelerator experiment [7]:

$${}^A_Z P + e^- (\text{bound}) + \bar{\nu}_e \rightarrow {}^A_{Z-1} D$$

$${}^A_Z P + \nu_e \rightarrow {}^A_{Z+1} D + e^- (\text{bound})$$

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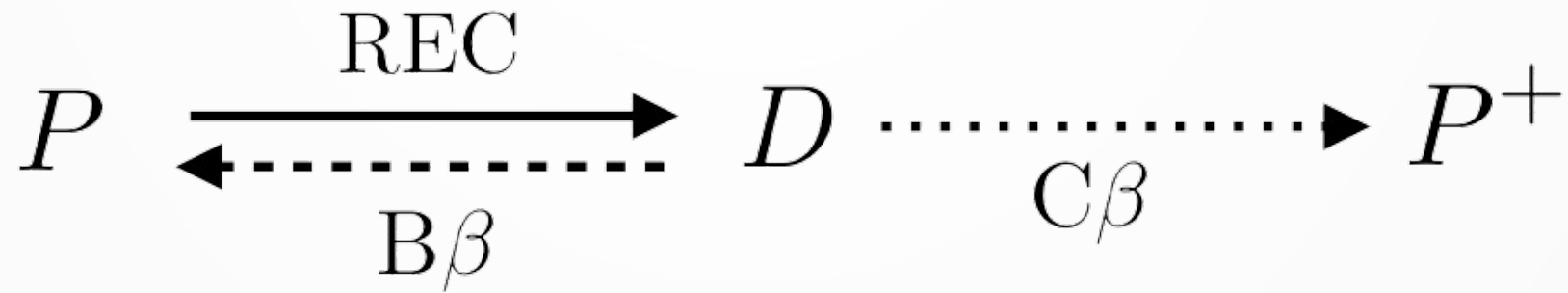
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$$\sigma_{\text{peak}} \simeq 10^{-15} \left(\frac{1 \text{ keV}}{Q} \right)^2 \text{Br}(D \rightarrow P) \text{ cm}^2$$

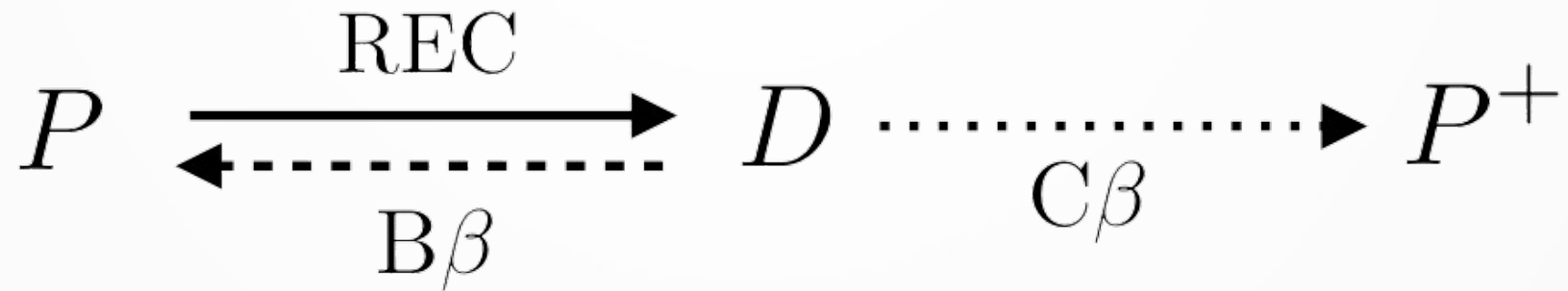
Accelerator

- Resonant electron capture:

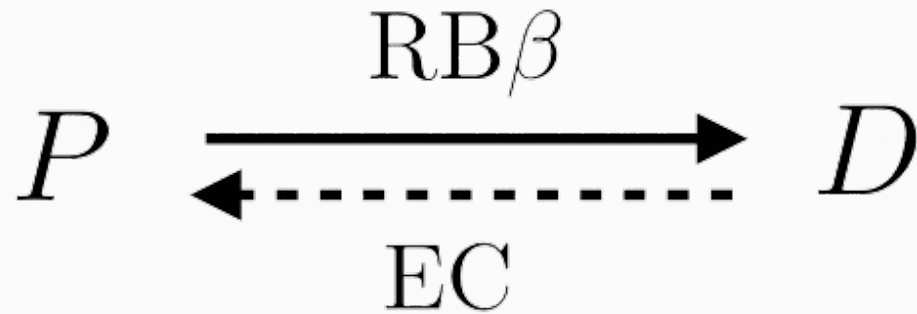


Accelerator

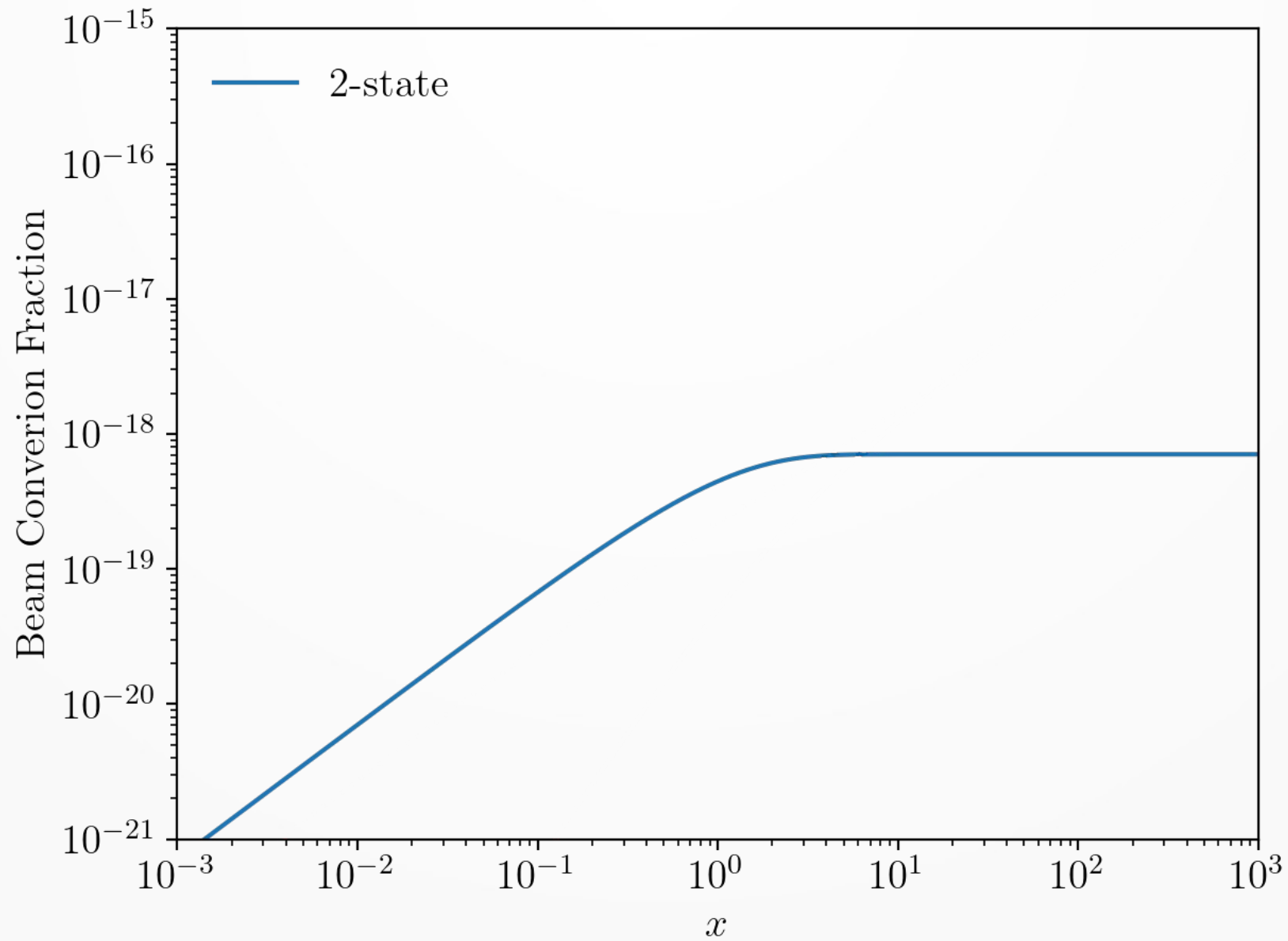
- Resonant electron capture:



- Resonant bound beta decay:



Accelerator



Accelerator

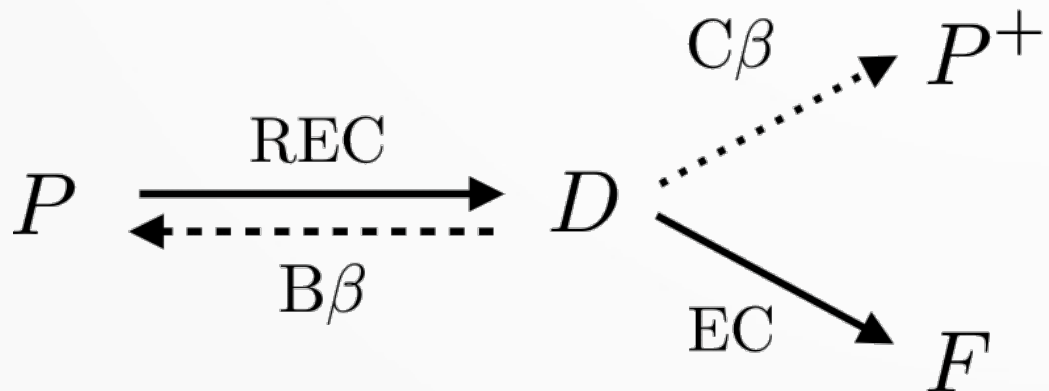
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Accelerator

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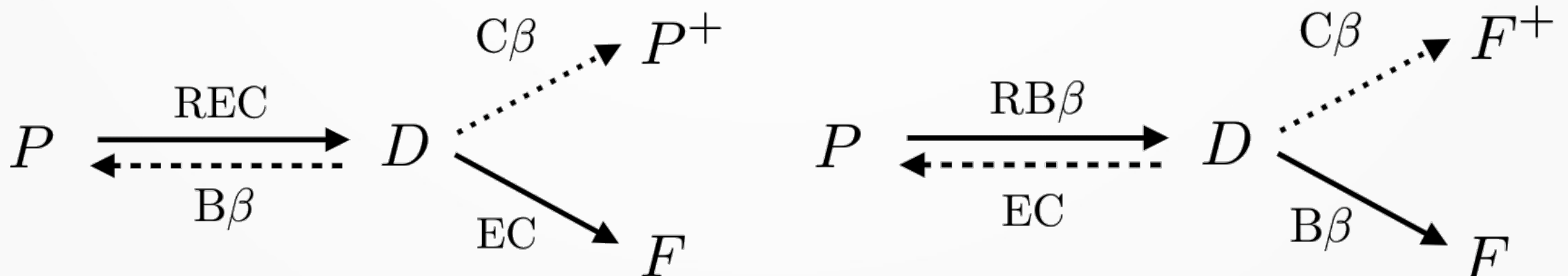
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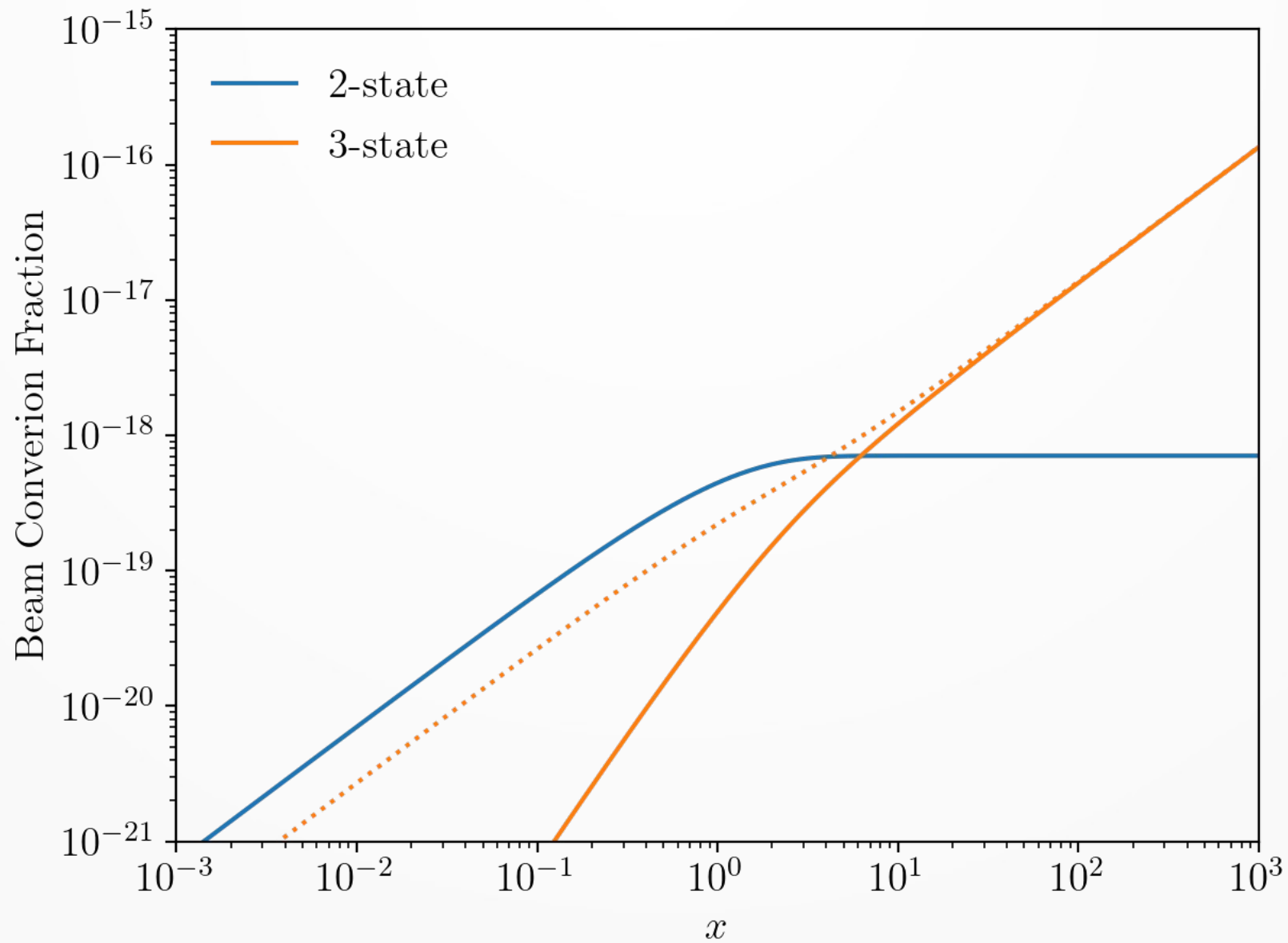


Accelerator

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- In general:

$$N_D \sim \frac{1}{Q^7} \implies Q \sim 0.1 \text{ keV}$$

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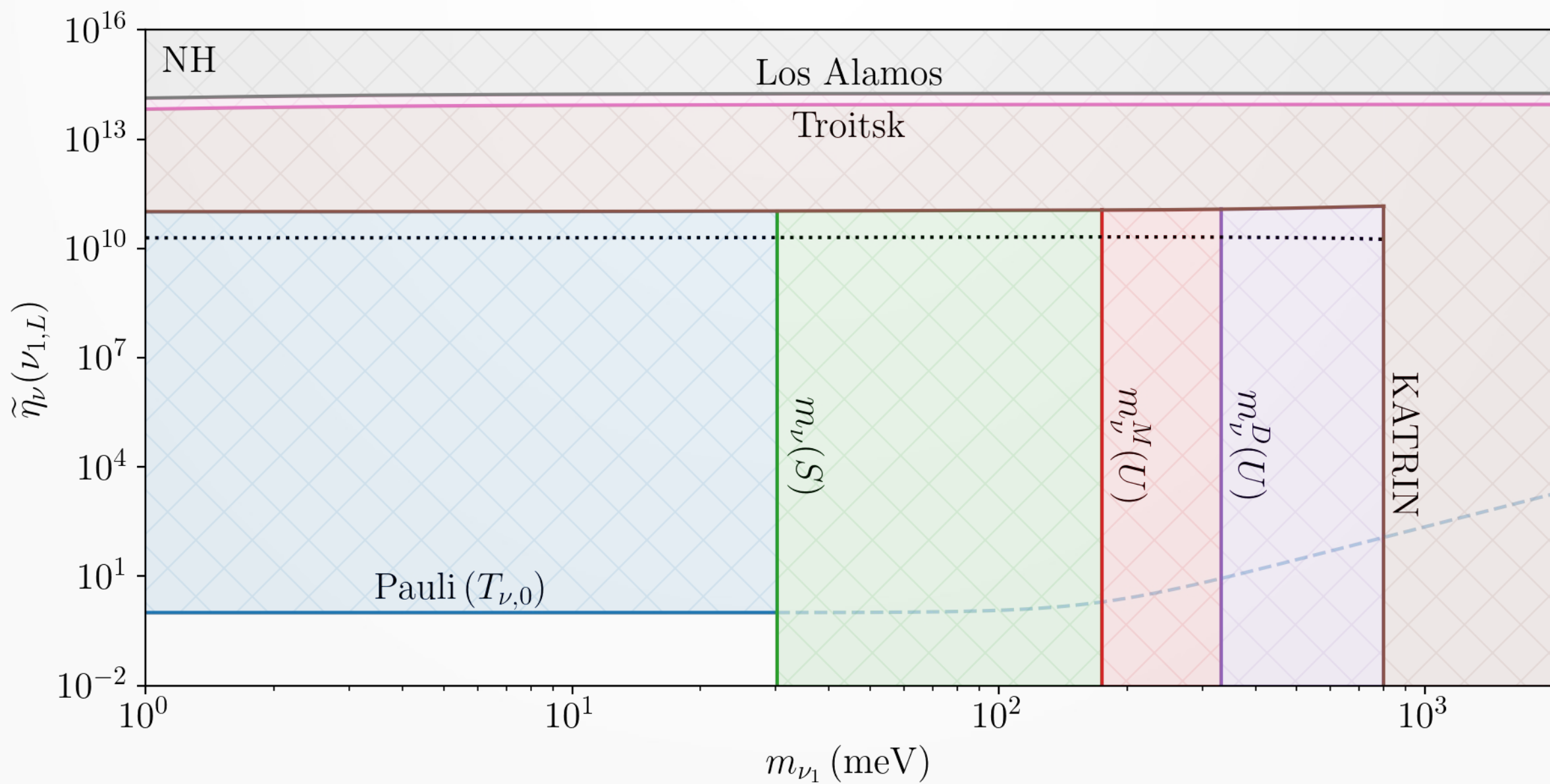
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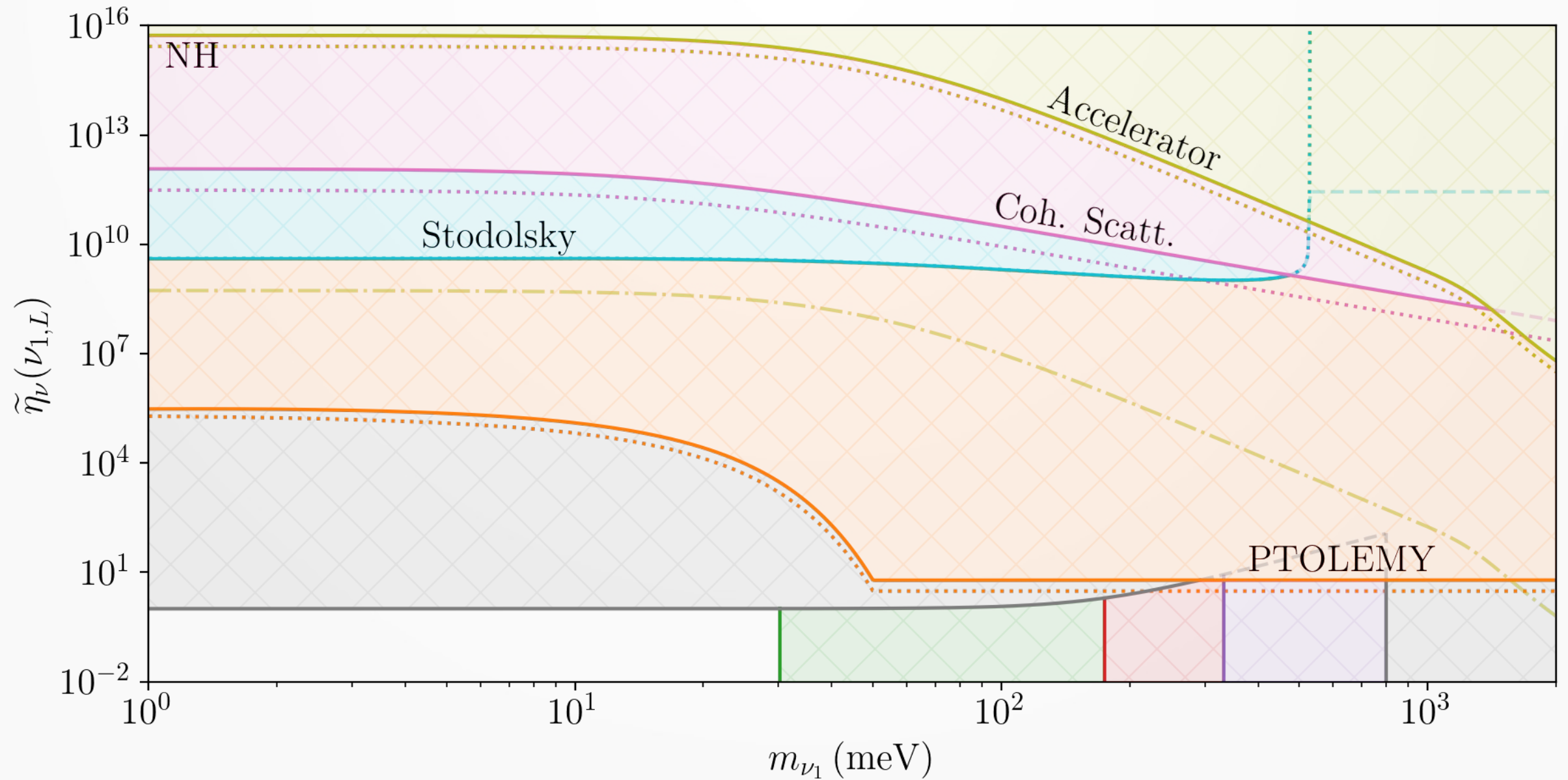
$$\eta_\nu = \frac{n_\nu}{n_{\nu,0}} \quad m_{\nu l} \quad T_\nu$$

- Mapping out the allowed parameter space lets us find the best detection proposal!

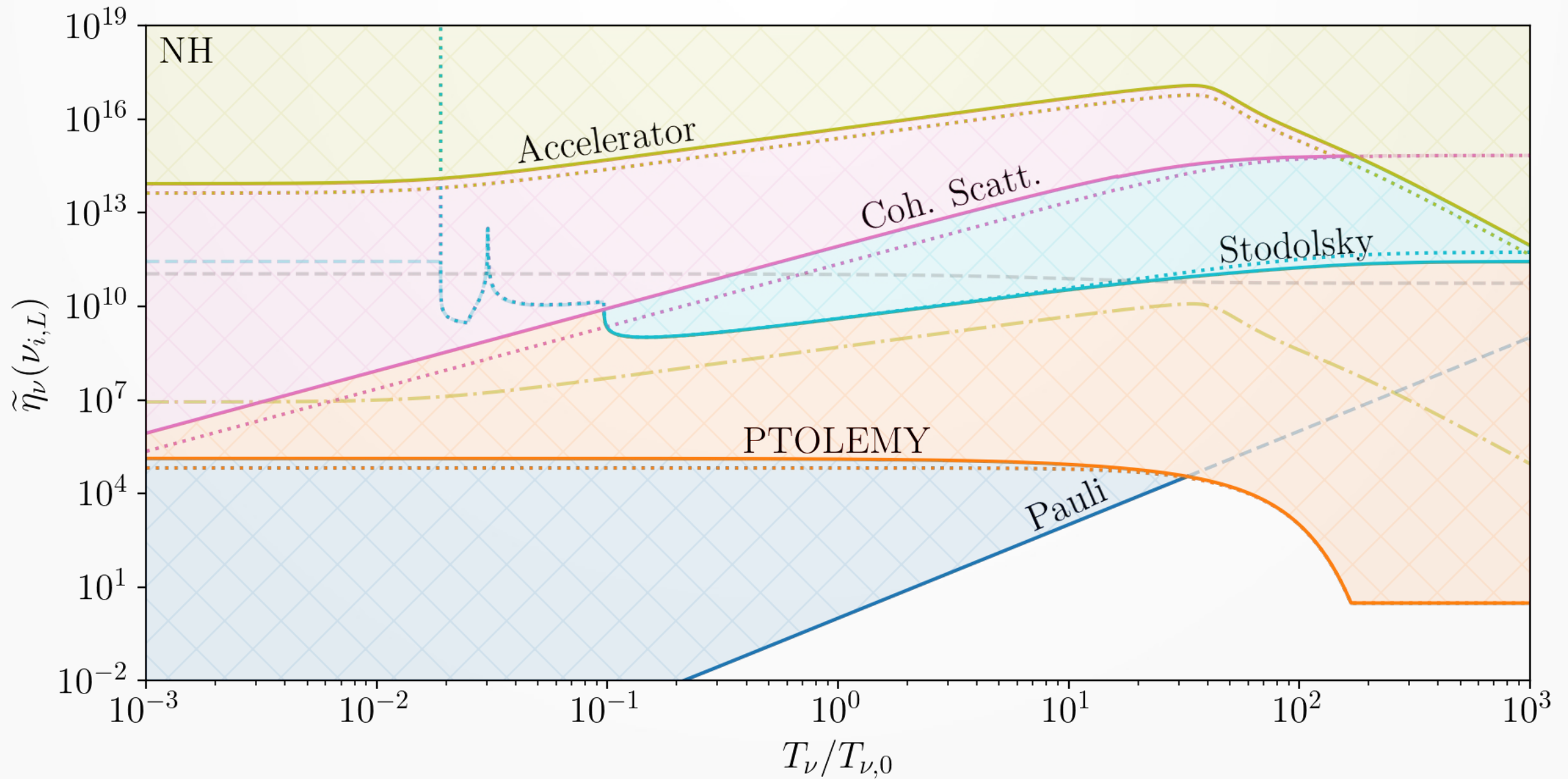
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- Detecting the $C\nu B$ could reveal a wealth of new physics
- Detection made difficult by neutrino properties
- Many exciting proposals to detect the $C\nu B$!

Thank you!
Questions?