#### Ce Zhang

University of Liverpool

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- Introduction
- Analysis
- ► Result
- Outlook & Summary

#### Introduction

- Muon g-2
- Experiment at Fermilab
- ► Analysis
- ► Result
- Outlook & Summary

- The anomalous magnetic moment of the muon:
  - Magnetic moments **precess** in a magnetic field  $\vec{\mu} = g \frac{e}{2m} \vec{S}$
  - g factor quantifies interaction strength





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- Interactions with virtual particles cause g to deviate from 2 (g > 2). Muon magnetic anomaly is defined as:

$$a_{\mu} = \frac{g-2}{2}$$







 $a_l = \frac{g_l - 2}{2} = \frac{\alpha}{2\pi} + O(\alpha^2)$ 

= 0.00116140

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$$\frac{\alpha}{2\pi}$$
JULIAN SCHWINGER
2·12·1918 — 7·16·1994
CLARICE CARROL SCHWINGER
9·23·1917 — 1·9·2011





### **Why** *g* − 2

• An experimental trick:

$$g = 2 \times (1 + a_{\mu}) \approx 2 + 0.002$$

~1000 gain by measuring  $a_{\mu}$  instead of g-factor !





### **Why Muon** *g* − 2

- Muon as a probe to New Physics:
  - For possible new physics  $a_{\mu} = a_{\mu}^{SM} + a_{\mu}^{NP}$
  - Its effects is enhanced by  $a_{\mu}^{NP} \propto (\frac{m_l}{\Lambda_{NP}})^2$





## Why Muon g - 2

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  - For possible new physics  $a_{\mu} = a_{\mu}^{SM} + a_{\mu}^{NP}$
  - Its effects is enhanced by  $a_{\mu}^{NP} \propto (\frac{m_l}{\Lambda_{MD}})^2$
  - Muon is more sensitive by a factor of  $(\frac{m_{\mu}}{m_{e}})^{2} \approx 4.3 \times 10^{4}$





## Why Muon g - 2



- Muon as a probe to New Physics
- A great tool for experimentalists
  - Can be produced copiously in proton collisions and pion decays
  - Can select momentum and polarization
  - Decays are very simple (Michel distribution due to weak decay)



## Why Muon g - 2

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Michel spectrum: highest energy positrons are aligned with muon's spin







$$\omega_{a} = -\frac{q}{m_{\mu}} \left( a_{\mu} B - \left( \frac{\gamma}{\gamma + 1} \right) (\beta B) \beta - \left( \frac{a_{\mu} - \frac{1}{\gamma^{2} - 1}}{a_{\mu} - \frac{\gamma^{2} - 1}{c}} \right)$$

$$\omega_{a} = \omega_{s} - \omega_{c}$$

$$\omega_{a} = -\frac{q}{m_{\mu}} a_{\mu} B$$



$$a_{\mu} = \frac{\omega_a}{B} \frac{m}{e}$$

1. Measure  $\omega_a^m$ : modulation of decay positron time spectrum

2. Measure *B*: proton nuclear magnetic resonance (NMR)  $\rightarrow 2\mu'_{p}B = \hbar\omega'_{p}$ (vacuum)

3. Extract  $a_{\mu}$ 

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- A real-world equation:

$$a_{\mu} = \frac{\omega_{a}^{m}}{\omega_{p}^{m}} \times \frac{(1 + C_{e} + C_{p} + C_{pa} + C_{dd} + C_{ml})}{(1 + B_{k} + B_{q})} \times \left[\frac{\mu_{p}'(T_{r})}{\mu_{e}(H)} \frac{\mu_{e}(H)}{\mu_{e}} \frac{m_{\mu}}{m_{e}} \frac{g_{e}}{2}\right]$$

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Corrections from Magnetic Field Transient

$$a_{\mu} = \frac{\omega_a}{B} \frac{m}{e}$$

1. Measure  $\omega_a^m$ : modulation of decay positron time spectrum

- 2. Measure *B*: proton nuclear magnetic resonance (NMR)  $\rightarrow 2\mu'_p(H_20, T_r)B = \hbar\omega'_p(H_20, T_r)$
- 3. Extract  $a_{\mu}$
- A real-world equation:

$$a_{\mu} = \frac{\omega_{a}^{m}}{\omega_{p}^{m}} \times \frac{(1 + C_{e} + C_{p} + C_{pa} + C_{dd} + C_{ml})}{(1 + B_{k} + B_{q})} \times \left[\frac{\mu_{p}'(T_{r})}{\mu_{e}(H)} \frac{\mu_{e}(H)}{\mu_{e}} \frac{m_{\mu}}{m_{e}} \frac{g_{e}}{2}\right]$$
Corrections from Magnetic External constants precisely

**Field Transient** 

22

known (to 25 ppb)

• Injecting polarized muons into a storage ring



- **3.1 GeV/c**  $\mu^+$  enter the ring
- Cyclotron period: 149.2 ns
- A cycle of 16 bunches repeating every 1.4 seconds
- ~4000  $\mu^+$ /bunch in the storage ring in Run-2/3



Injecting polarized muons into a storage ring





• Inflector creates a "field-free" region





• 3 pulses magnets changes muon angle onto the good orbit (~10 mrad)



• Electrostatic Quadrupoles (ESQ) provide vertical focusing of the beam





- Quads cover 43% of azimuth
- Focus beam to a simple harmonic motion about closed orbit

• 1.45T superferric magnet shimmed to 50 ppm uniformity (~3x uniformity)





# Muon g - 2 Experiment at Fermilab Setups: Detectors

Detect decay positrons with 24 calorimeters and 2 tracker stations





PbF<sub>2</sub> crystals

### **Muon** *g* – 2 **Experiment at Fermilab** Setups: Detectors

Detect decay positrons with 24 calorimeters and 2 tracker stations





Straw tracker developed in Liverpool

#### Introduction

- Analysis
  - Precession frequency
  - Beam dynamics
  - Field
  - Blinding, combination, etc.
- ► Result
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### **Muon Precession Frequency**



• The number of detected high-energy positrons oscillating above an energy threshold is **modulated** by the anomalous precession frequency  $\omega_a$ 





Run-3a:  $\delta \omega_a(stat) = 329$  ppb, 15.3B positrons (~50% of Run-2/3)



relative size of wiggle: asymmetry  $\approx 0.35$ 



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relative size of wiggle: asymmetry  $\approx 0.35$ 

exponential decay: boosted lifetime  $\approx 64.4 \ \mu s$ 



Run-3a:  $\delta \omega_a(stat) = 329 \text{ ppb}, 15.3 \text{B}$  positrons



Simple fit to extract the frequency: an exponentially decaying oscillation at g-2  $N(t) = N_0 e^{(-t/\tau)} [1 + A\cos(\omega_a t - \phi)]$ 



Run-3a:  $\delta \omega_a(stat) = 329 \text{ ppb}, 15.3 \text{B}$  positrons



Simple fit to extract the frequency: an exponentially decaying oscillation at g-2  $N(t) = N_0 e^{(-t/\tau)} [1 + A\cos(\boldsymbol{\omega}_a t - \boldsymbol{\phi})]$ FFT Mag [arb.] 14 12 Peaks on the Fast Fourier 10 Transform (FFT) of fit residuals: simple fit is not sufficient; need a better model

2.5

3 Freq [MHz]

2

0.5

ω<sub>a</sub>

1.5


### Extra terms in the Fitting Function

 A better model must account for detector effects, beam oscillations coupled to acceptance, lost muons and fast rotations that disrupt pure exponential



Some muons are lost before they decay





### Extra terms in the Fitting Function

- A better model must account for detector effects, beam oscillations coupled to acceptance, lost muons and fast rotations that disrupt pure exponential
- I will elaborate two major systematic sources:
  - Pileup
  - Coherent betatron oscillations (CBO)



### Muon Precession Frequency Pileup

• Two or more positrons are misidentified as a single positron due to arriving too close in time/space



Two low energy positrons fake a high energy positron signal

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 Probability of pileup decreases over fill

### **Muon Precession Frequency** Pileup Correction

- Correct data with empirically determined pileup spectrum
- Improved clustering algorithm for a pileup reduction

Counts/50.0 MeV

10

10<sup>6</sup>

10<sup>4</sup>

10<sup>3</sup>

 $10^{2}$ 

10

10

0

Energy spectrum Reduced pileup in Run-2/3 spectrum Spectrum before/after correction 5000 Count Data Run-2 Data Original spectrum Constructed Pileup (positive) Run-1 Clustering 10<sup>8</sup> 40000 Run-2/3 Clustering Constructed Pileup (negative) Corrected spectrum Run 3a 30000  $10^{6}$ Decay 20000 endpoint :  $10^{4}$ 10000 pileup 10<sup>2</sup> only! 4500 5500 600 0 1000 2000 3000 4000 5000 6000 3000 3500 5000 4000 4000 5000 6000 7000 1000 2000 3000 8000 9000 100 Energy [MeV] Energy [MeV] Energy [MeV]







Coherent Betatron Oscillations (CBO)



- As muons circulate around the storage ring, they slowly oscillate between the plates
- Coherent betatron oscillations (CBO) horizontally couples to detector acceptance and modulate signal





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- As muons circulate around the storage ring, they slowly oscillate between the plates
- Coherent betatron oscillations (CBO) horizontally couples to detector acceptance and modulate signal





Coherent Betatron Oscillations (CBO)



• The amplitude of CBO decreases over time because of the **decoherence of muons** 



- Time-dependence is modelled
- Assess uncertainty by testing many different models



### Full Fit and Uncertainty improvements

· Modified fit function for beam dynamics effects gives good fit quality





#### Full Fit and Uncertainty improvements

• Run-2/3 uncertainty is 2.2 times smaller than Run-1

Quantity	Correction [ppb]	Uncertainty	
$(m^m \text{ (statistical)})$	[[[]	201	
$\omega_a^m$ (systematic)	-	251	
$\overline{C_e}$	451	32	
$C_p$	170	10	
$C_{pa}$	-27	13	
$\overline{C}_{dd}$	-15	17	
$C_{ml}$	0	3	
$f_{ m calib} \langle \omega_p'(\vec{r})  imes M(\vec{r})  angle$	-	46	
$B_k$	-21	13	
$B_q$	-21	20	
$\mu_p'(34.7^\circ)/\mu_e$	_	11	
$m_\mu/m_e$	_	22	
$g_e/2$		0	
Total systematic	_	70	
Total external parameters	_	25	
Totals	622	215	





 $\omega_a = -\frac{q}{m} [\dots + (a_\mu - \frac{1}{\gamma^2 - 1}) \frac{\beta \times \mathbf{E}}{c}]$ 

$$a_{\mu} = \frac{\omega_a^m}{\omega_p^m} \times \frac{(1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml})}{(1 + B_k + B_q)} \times [\dots]$$

**E-field** correction (momentum dispersion from 'magic'  $\gamma$ )



 $C_e$ 

$$\frac{\Delta p}{p_0} = (1-n)\frac{x_e}{R_0}$$

The correction depends on the muon radius distribution
 <X<sub>e</sub><sup>2</sup>> wrt the 'magic' radius. This distribution can be measured with either calo or tracker data:

$$C_e \approx 2n(1-n)\beta_0^2 \frac{\langle x_e^2 \rangle}{R_0}$$



$$a_{\mu} = \frac{\omega_{a}^{m}}{\omega_{p}^{m}} \times \frac{(1 + C_{e} + C_{p} + C_{pa} + C_{dd} + C_{ml})}{(1 + B_{k} + B_{q})} \times [\dots]$$

Pitch correction from muon's small vertical momentum component.



 $C_p$ 

$$\omega_a = -\frac{q}{m} [\dots + \frac{\gamma}{\gamma+1} (\beta \cdot B)\beta]$$

Calculated by measuring (or reconstructing) vertical position distribution:

$$C_p = \frac{1}{2} \langle \psi^2 \rangle = \frac{n}{4R_0^2} \langle A^2 \rangle = \frac{n}{2R_0^2} \langle (y - \bar{y})^2 \rangle$$



$$a_{\mu} = \frac{\omega_a^m}{\omega_p^m} \times \frac{(1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml})}{(1 + B_k + B_q)} \times [\dots]$$

 $C_{pa}$ 

Phase acceptance correction by decay-position dependence of positron phase



Early-to-late beam motion modulation leads to timedependent phase



$$a_{\mu} = \frac{\omega_a^m}{\omega_p^m} \times \frac{(1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml})}{(1 + B_k + B_q)} \times [\dots]$$

 $C_{dd}$ 

Differential decay correction as high momentum muons have longer lifetime

• Coherent **time dependence of**  $\varphi_0$  over fill could bias measured  $\omega_a$ :

$$\frac{\Delta\omega_a}{\omega_a} = -\frac{1}{\omega_a} \frac{d\phi_0}{dt}$$

• New correction in Run-2/3

$$\phi_{1}(x_{1}, x_{1}', y_{1}, y_{1}', \tau_{1}, p_{1})$$

$$\phi_{2}(x_{2}, x_{2}', y_{2}, y_{2}', \tau_{2}, p_{2})$$

$$\vdots$$

$$\phi_{n}(x_{n}, x_{n}', y_{n}, y_{n}', \tau_{n}, p_{n})$$



$$a_{\mu} = \frac{\omega_a^m}{\omega_p^m} \times \frac{(1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml})}{(1 + B_k + B_q)} \times [\dots]$$

 $C_{ml}$ 

Muon loss correction from initial phase-momentum correlation in muons



• Muons are lost in time, there is time-dependent change in phase:

$$\frac{d\phi_0}{dt} = \frac{d\phi_0}{d \frac{d d}{dt}}$$



**Uncertainty Summary** 

	Corrections [ppb]	Uncertainty [ppb]	Uncertainty in Run-1 [ppb]
C <sub>e</sub>	451	32	53
$C_p$	170	10	13
C <sub>pa</sub>	-27	13	75
C <sub>dd</sub>	-15	17	-
C <sub>ml</sub>	0	3	5
Total	580	40	93

**Uncertainty Summary** 



	Corrections [ppb]	Uncertainty [ppb]	Uncertainty in Run-1 [ppb]	• <i>C<sub>pa</sub></i> etc have been greatly reduced after fixing the 2
C <sub>e</sub>	451	32	53	Droken nv resistors in Run-1
$C_p$	170	10	13	$\overline{\omega}$ -22.2
C <sub>pa</sub>	-27	13	75	
C <sub>dd</sub>	-15	17	-	
$C_{ml}$	0	3	5	-22.4 • Run-1d
Total	580	40	93	-22.45 -22.45
				50 100 150 200 250 Time [μs]



Field in Muon Storage Region



7.112 m radius 'C'shape magnet with vertically-aligned field B = 1.45 T

- Dipole field has ppm-level uniformity (<20 ppm RMS across the full azimuth)</li>
- > Shimming devices (active and passive) minimise gradients and keep field uniform

### NMR: Trolley and Fixed Probes









- A trolley with 17 NMR probes maps the magnetic field in muon storage volume every ~3 days
- Run-1: **14** trolley maps; Run-2/3: 69 maps





#### NMR: Trolley and Fixed Probes







- 378 fixed NMR probes, above or below storage volume permanently installed ("fixed") at 72 locations around the ring (every ~5°)
- Track changes in the field continuously during muon storage



# **Magnetic Field Measurement** Field Interpolation



- Need to know the precise field at the times when muons are present in the ring
- Fixed probes don't measure storage region directly need to calibrate it with trolley measurement
- Offset driven by small changes in the field regions with low FP sensitivity



Run-2/3 uncertainty ~17 ppb



 $a_{\mu} = \frac{\omega_a^m}{<\omega_p \otimes \rho_{\mu} >} \times \cdots$ 

- Magnetic field maps weighted by muon distribution determined by trackers
- Use beam dynamics simulations to extrapolate distribution around ring





Azimuthal dependence of field moments



 $a_{\mu} = \frac{\omega_a^m}{\langle \omega_p \otimes \rho_{\mu} \rangle} \times \cdots$ 

- Magnetic field maps weighted by muon distribution determined by trackers
- Use beam dynamics simulations to extrapolate distribution around ring
- Improvement in Run-2/3: better centred beam







Quad Transient Fields Correction:  $B_k$ 



 $a_{\mu} = \frac{\omega_a^m}{\langle \omega_n^m \rangle} \times \frac{(1 + C_e + \cdots)}{(1 + B_k + B_a)} \times \cdots$ 



- Run-2/3 has lower vibration noise vs. Run-1
- Uncertainty reduces from 37 ppb to 13 ppb



Quad Transient Fields Correction:  $B_q$ 



Pulsing **quads' plates vibrate** ⇒ **oscillating magnetic fields** Measured with a **new NMR probe** housed in insulator ٠ ESQ3 ESQ4 ESQ2 ransient (ppb Field Change [ppb] 400 400⊦ 200 **Run-1 Measurement** 200 Locations -200 -200 -400 Muon, fills -400 20 80 40 60 100 0 100 200 -100 0 Time (ms) Azimuth (deg)

- For Run-1 analysis, we had limited measurement positions
- Largest Run-1 systematic: 92 ppb

Release talk by James Mott, 10th August 2023



Quad Transient Fields Correction:  $B_q$ 

$$a_{\mu} = \frac{\omega_a^m}{\langle \omega_p^m \rangle} \times \frac{(1 + C_e + \cdots)}{(1 + B_k + B_q)} \times \cdots$$

For Run-2/3 analysis, probe runs on the trolley rails •

Allows **full mapping** of all quad stations:





Uncertainty is reduced to **20 ppb** 

on trolley rail train



### **Uncertainty Summary**



- Main reduction in the uncertainty comes from better understanding of the transient field effects (B<sub>k</sub> and B<sub>q</sub>)
- Interpolation uncertainty also reduced with increased trolley runs
- TDR goal already achieved

### **Consistency Check**



• We perform many consistency checks: fit residual FFTs, fit start time scans, fits by calorimeter, fits by positron energy, etc.



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### **Datasets and Combination**



- Three datasets based on different running configurations (Run-2; Run-3a; Run-3b)
- 7 analysis groups for a total of 19 analysis methods (results)
  - Final combination only considers 6 of them (asymmetry-weighted methods)
- Assuming 100% correlated systematics across datasets

dataset	quad HV [kV]	index n	kicker HV [kV]	$\begin{array}{l} \mathrm{beam} < x > \\ \mathrm{[mm]} \end{array}$	magnet temp, $\Delta T$		$\omega_a$ statistical uncertainty [ppm]
Run 2 Run 3a Run 3b	$18.3 \\ 18.2 \\ 18.2$	$0.108 \\ 0.107 \\ 0.107$	$142 \\ 142 \\ 165$	5-6 4-5 0-1	$\sim 3 \ ^oC$ $\sim 0.2 \ ^oC$ $\sim 0.2 \ ^oC$	$     18 \\     33 \\     12   $	$0.34 \\ 0.29 \\ 0.47$

### **Datasets and Combination**



66

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### **Blinding Analysis**



### Locked Clock Panel



$$\frac{\omega_{a}}{\tilde{\omega_{p}'}} = \frac{f_{\text{clock}} \ \omega_{a,\text{meas}} \ (1 + c_{e} + c_{p} + c_{ml} + c_{pa})}{f_{\text{field}} \ \left\langle \omega_{p} \bigotimes \rho_{\mu} \right\rangle \ (1 + B_{qt} + B_{kick})}$$

- Perform analysis with software & hardware blinding
- Hardware blind comes from altering our clock frequency
  - Non-collaborators set frequency to  $(40 \epsilon)$  MHz
- Clock is locked and value kept secret until analysis completed

## New Results from the Muon g - 2 Experiment at Fermilab

- Introduction
- ► Analysis

#### Result

- Unblinding
- Discrepancies with SM prediction(s)
- Outlook & Summary

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### **Unblinding** 24th of July, 2023

- Muon g-2 analysis has software & hardware blinding
- Unblinding meeting in Liverpool:





Photo credits: McCoy Wynne

- Unanimous vote from all collaborators to unblind!
- Secret envelopes were finally opened to reveal the hidden clock frequencies and the result...





### **New Result**

### Released on 10<sup>th</sup> of Aug 2023

• PRL (...) has been accepted





FNAL Run-1 (2021) confirmed BNL (Brookhaven, 2004) measurement



### **New Result**

### Released on 10<sup>th</sup> of Aug 2023

• PRL (...) has been accepted







- FNAL Run-1 (2021) confirmed BNL (Brookhaven, 2004) measurement
- FNAL (2023): **Excellent agreement** with BNL and Run-1; Uncertainty more than halved to **215 ppb**

### **New Result**

### Released on 10<sup>th</sup> of Aug 2023

• PRL (...) has been accepted







- Combined FNAL result uncertainty: 203 ppb
- Combined world average uncertainty is **190 ppb**
- Average is **dominated by FNAL** value


### **Discrepancy between Experiments & Theories**



• New experimental average with SM prediction (WP-2020) gives >  $5\sigma$ 



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- Since then, two important developments on SM prediction:
  - Lattice QCD from the BMW (2020)



### **Discrepancy between Experiments & Theories**



- New experimental average with SM prediction (WP-2020) gives >  $5\sigma$
- Since then, two important developments on SM prediction:
  - Lattice QCD from the BMW (2020)
  - New  $e^+e^- \rightarrow \pi^+\pi^-$  cross section from CMD-3 (2023)

**Disclaimer:** 

The CMD-3 point is a visual exercise. It is not a fully updated SM prediction!

- TI White Paper result has been substituted by CMD-3 only for 0.33 → 1.0 GeV.
- The NLO HVP has not been updated.
- It is purely for demonstration purposes → should not be taken as final!



### Standard Model (SM) predictions

• The uncertainty in the SM prediction of  $a_{\mu}$  is **entirely limited** by our knowledge of the hadronic leading order contribution  $a_{\mu}^{\text{HLO}}$  ( $a_{\mu}^{\text{HVP,LO}}$ )



Standard Model (SM) predictions

- The uncertainty in the SM prediction of  $a_{\mu}$  is **entirely limited** by our knowledge of the hadronic leading order contribution  $a_{\mu}^{\text{HLO}}$  ( $a_{\mu}^{\text{HVP,LO}}$ )
- Approaches (at low-E; pQCD doesn't work):
  - 1) Lattice QCD Method: Ab-initio calculation on lattice
  - 2) Dispersive Method: using  $\sigma(e^+e^- \rightarrow hadrons)$  data











### Dispersive Method Using Collider Data

•  $e^+e^- \rightarrow \pi^+\pi^-$  channel is the major source of uncertainty





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### **Dispersive Method Using Collider Data**

•  $e^+e^- \rightarrow \pi^+\pi^-$  channel is the major source of uncertainty



A **recent CMD-3 result** is different from all the previous data  $\rightarrow$  more puzzles!

### Outlook



- Towards solving SM prediction ( $a_{\mu}^{HVP,LO}$ ) inconsistencies:
  - KLOE & BABAR discrepancy (MC generator, ...)
  - Outstanding CMD-3 result
  - **MUonE** to better understand  $a_{\mu}^{HVP,LO}$

### Outlook



- Towards solving SM prediction ( $a_{\mu}^{HVP,LO}$ ) inconsistencies:
  - KLOE & BABAR discrepancy (MC generator, ...)
  - Outstanding CMD-3 result
  - **MUonE** to better understand  $a_{\mu}^{HVP,LO}$
- Experimental updates:
  - Final result from Fermilab (Run-4/5/6)
  - New Muon g 2/EDM experiment at J-PARC

### **Outlook** Final Result from Fermilab (Run-4/5/6)





- With data in Runs 4,5,6, we can double our sensitivity again and likely surpass our goal of 140ppm total uncertainty
- Expected ~ 2025

### Outlook



### Muon g - 2/EDM Experiment at J-PARC

#### **Features:**

#### **Muon cooling**

- Surface muon (3.4 MeV, large emittance)
- → thermal muon (0.2 eV, low emittance)

#### Muon LINAC

Muon acceleration to 212 MeV

#### **3D spiral injection**

- Large kick angle within a few ns
- Good injection efficiency

#### Storage ring

- Compact storage ring
- Tracking detector



### Outlook



### Muon g - 2/EDM Experiment at J-PARC

#### **Goals:**

#### $a_{\mu}$ (statistically limited)

- 0.45 ppm (phase-1, ~ BNL/FNAL Run-1)
- 0.10 ppm (phase-2, ~ FNAL Final)

#### Muon EDM (sensitivity)

•  $1.5 \times 10^{-21} \ e \cdot cm$  (×70 better)

#### **Schedule:**

#### First data taking phase

- Start from 2028 and beyond
- Running time of 2 × 10<sup>7</sup>s (240 days)







#### Muon g - 2 Experiment at Fermilab

Better than 200 ppb precision achieved in Run-2/3

Precession Frequency Beam Dynamics Corrections Magnetic Field
Consistency Check; Blinding; Combination etc.





#### Muon g - 2 Experiment at Fermilab

Better than 200 ppb precision achieved in Run-2/3

Precession Frequency Beam Dynamics Corrections Magnetic Field
Consistency Check; Blinding; Combination etc.

#### SM prediction(s)

Data-driven method (WP2020) conflicts with the LQCD

Discrepancies within the data-driven method:

- KLOE BABAR
- CMD-3 with all previous results





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Up to 5-sigma discrepancy

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# Summary



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#### Future experimental results

- Final result (Run-4/5/6) from Fermilab (~2025)
- New Experiment at J-PARC (2028)

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**Beam Dynamics Corrections** Precession Frequency Magnetic Field

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#### **Future experimental results**

- Final result (Run-4/5/6) from Fermilab (~2025)
- New Experiment at J-PARC (2028) •

#### Future SM update

- The Muon g 2 Theory Initiative is coordinating • the SM prediction update
- **MUonE Project** at CERN to directly measure HVP •

# Thank you!

### Acknowledgements

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- MSIP, NRF and IBS-R017-D1 (Republic of Korea)



### Backup



#### **Muon g-2 Collaboration**





- Boston
- Cornell
- Illinois
- James Madison
- Kentucky
- Massachusetts
- Michigan
- Michigan State
- Mississippi
- North Central
- Northern Illinois
- Regis
- Virginia
- Washington

#### **USA National Labs**

- Argonne
- Brookhaven
- Fermilab

# 181 collaborators33 Institutions7 countries



Shanghai Jiao Tong

#### Germany







- Frascati
- Molise
- Naples
- Pisa
- Roma Tor Vergata



Juline – Udine



CAPP/IBS





 $\searrow$ 

- Duurenniovosiniisk
- JINR Dubna

#### United Kingdom

- Lancaster/Cockcroft
- Liverpool
- Manchester
- University College London

#### Muon g-2 Collaboration

7 countries, 33 institutions, 181 collaborators





Muon g-2 Collaboration Meeting @ Elba, May 2019





# **Muon Precession Frequency UNIVERSITY OF LIVERSITY OF Fast Rotation Effect**

- Each individual detector can only sample the muon beam at a particular phase of the cyclotron period.
- In terms of the debunching effect, this sampling implies that the positron data will contain a modulation at the cyclotron period (149 ns << 4.3 us) that decoheres over the measurement period.





5 900 800 700 600 500 400 300 40 41 42 43 44 45 46 47 Time (μs)

(a) Fast rotation signal in the positron data for calorimeter 1, at early times when the signal is strong.

(b) Fast rotation signal in the positron data for calorimeter 1, at later times when the signal is reduced.

# **Magnetic Field Measurement**



- > Trolley and fixed NMR probes use petroleum jelly as the proton sample low volatility
- > Need to measure protons in  $H_20$  (measurement standard)  $\rightarrow$  calibration
- Trolley and cylindrical H<sub>2</sub>0 calibration probe switch places to repeatedly measure the same field in the same place. Calibration performed ~once per year.
   Cylindrical H<sub>2</sub>0 probe









EPS talk by Saskia Charity, 21st August 2023

UNIVERSITY OF

LIVERPOOL

Cross-check with spherical probes Uncertainty: 9 ppb

### **Muon** *g* – 2 **Experiment at Fermilab** Experimental Principle

$$a_{\mu} = \frac{\omega_a}{B} \frac{m}{e}$$

1. Measure  $\omega_a^m$ : modulation of decay positron time spectrum

2. Measure *B*: proton nuclear magnetic resonance (NMR)  $\rightarrow B = \frac{\hbar \omega_p}{2} \cdot \frac{\mu_e(H)}{\mu'_n(H_2 0)} \cdot \frac{\mu_e}{\mu_e(H)} \cdot \frac{1}{\mu_e}$ 

3. Extract  $a_{\mu}$ 

$$a_{\mu} = \frac{\omega_a^m}{\omega_p^m} \times \frac{(1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml})}{(1 + B_k + B_q)} \times \left[\frac{g_e}{2} \frac{\mu_p'(\mathsf{H}_2\mathsf{O})}{\mu_e(\mathsf{H})} \frac{\mu_e(\mathsf{H})}{\mu_e} \frac{m_\mu}{m_e}\right]$$

Corrections from Magnetic Field Transient External constants precisely known (to 25 ppb)

# Why Muon g - 2



- Muon as a probe to New Physics
  - For any new physics  $a_{\mu} = a_{\mu}^{SM} + a_{\mu}^{NP}$ ?
  - Its effects is enhanced by  $a_{\mu}^{NP} \propto (\frac{m_l}{\Lambda_{NP}})^2$
  - Muon is more sensitive by a factor of  $(\frac{m_{\mu}}{m_{e}})^{2} \approx 4.3 \times 10^{4}$



Trapped electrons allow the most precise measurement of g-2

 $\mu$ 

A factor of 40 improved measurements on (g-2)<sub>e</sub> is needed to provide a compatible crosscheck with the muon (with a factor of 2 improved α measurement)

# Beam Dynamic Corrections



$$a_{\mu} = \frac{\omega_a^m}{\omega_p^m} \times \frac{(1 + C_e + C_p + C_{pa} + C_{dd} + C_{ml})}{(1 + B_k + B_q)} \times [\dots]$$

C <sub>e</sub>	<b>E-field</b> correction ( <b>momentum dispersion</b> from magic $\gamma$ )
$C_p$	Pitch correction from muon's small vertical momentum component
$C_{pa}$	Phase acceptance correction by decay-position dependence of positron phase
$C_{dd}$	Differential decay correction as high momentum muons have longer lifetime
$C_{ml}$	Muon loss correction from initial phase-momentum correlation in muons



A New Approach towards  $a_{\mu}^{\text{HVP}}$  with running of  $\Delta \alpha_{\text{had}}$ 

• The dispersive approach to compute  $a_{\mu}^{\text{HVP,LO}}$  is via the time-like formula:

$$\int_{\mu}^{\gamma} \int_{\mu}^{\mu} a_{\mu}^{\text{Horos}} = \left(\frac{\alpha m_{\mu}}{3\pi}\right)^2 \int_{m_{\pi^0}}^{\infty} ds \, \frac{R_{\text{had}}(s)K(s)}{s^2}, \quad K(s) = \int_{0}^{1} dx \, \frac{x^2(1-x)}{x^2 + (1-x)(s/m_{\mu}^2)}$$

• Alternatively, exchanging the x and s integrations  $\rightarrow$  space-like formula:



Running of  $\Delta \alpha_{had}$ : Time-like vs Space-like





 $\Delta \alpha_{had}$  via Muon-electron Scattering





 $\Delta \alpha_{had}$  via Muon-electron Scattering





### $\Delta \alpha_{had}$ via Muon-electron Scattering





### $\Delta \alpha_{had}$ via Muon-electron Scattering















- Correlation between muon and electron angles allows to select elastic events and reject background ( $\mu N \rightarrow \mu N e^+e^-$ ).
- Boosted kinematics:
  - Single detector to cover full acceptance
  - $\theta_{\mu} < 5 \text{ mrad}, \theta_{e} < 32 \text{ mrad}.$

