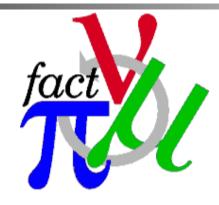
Cooling Ring Concept



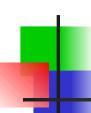
Chris Rogers,
ASTeC,
Rutherford Appleton Laboratory
April 2008



Cooling Ring Concept



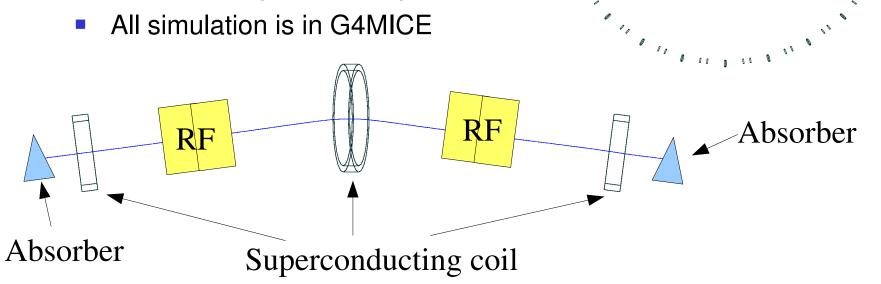
- Cooling rings using tilted solenoids have been considered for 6D cooling
 - Shown to be very effective and cheap
 - But impossible to inject/extract beam
 - Very short, tight cooling lattice
- As part of work for dogbone cooler I developed a long cooling lattice
 - More spacious
 - If I could turn this into a ring, there would be room to inject/extract
- Consider cooling ring with tilted solenoids
 - Use tilt to produce bending field
 - Conventional dipoles are awkward because of extended solenoid fringe field
 - May choose to use dipoles either by careful optics or by shielding from the solenoid fringe field
- Nb: back of envelope indicates cost of ring = cost of ISS cooling



Cooling Ring Concept



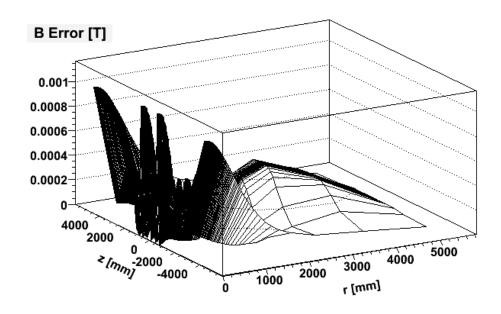
- Current work in progress
 - 24 cells
 - 15° bend
 - ~10°-15° tilt
 - Only tilting central coil
- Cooling hardware only exists in powerpoint!
 - Still sorting out lattice optics





Solenoid Mods





- Two issues with tilted solenoid ring field map
 - Tracking is sensitive to interpolation errors
 - Tracking is sensitive to extent of field map
- Constraining field map accuracy => very big field maps
- Dynamically select field map grid spacing and extent according to required field tolerance

Optics Algorithm



- Nicely automated optics algorithm to deal with full 6D coupling
 - Use minimising package e.g. minuit to find closed orbit
 - Fire particles from beginning of cell to end of cell
 - Seek to minimise phase space vector between in and out
 - Use tracking information to construct transfer map **M**

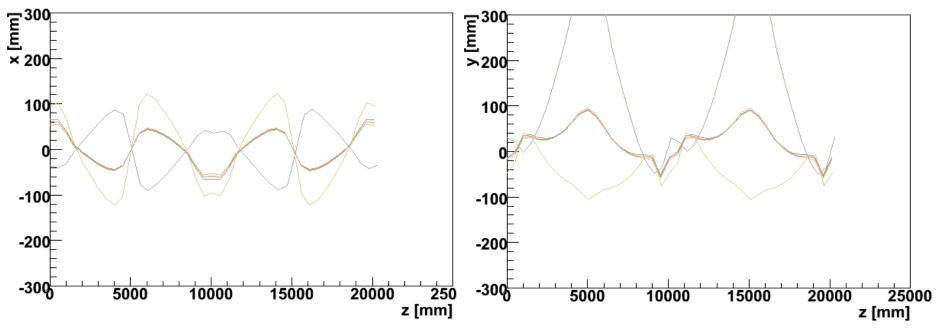
Construct matrix
$$\boldsymbol{U}$$
 from tracks like
$$\begin{vmatrix} t + \delta t \\ E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E \\ x \\ p_x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E \\ x \\ p_x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E \\ x \\ p_x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_y \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_x \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_x \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_x \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_x \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \\ p_x \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ p_x \end{vmatrix} \begin{vmatrix} t \\ E + \delta E \\ x \\ y$$

- Fire tracks through cooling cell
- Solve M U_{in} = U_{out} to get M
- Solve transport equation to extract matched 6D covariance matrix **V**
 - Solve $M^T V_{in} M = V_{out}$ with $V_{out} = V_{in}$
- Repeat over a range of momenta to get chromatic aberrations
- I might like to extract spherical aberrations as well at some point
- Takes about 1 minute for each step
 - Next: put this into an optimiser to optimise lattice



Closed Orbit vs Path Length



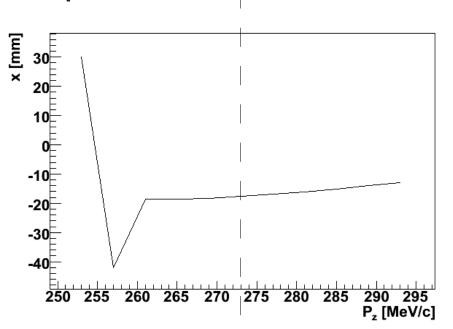


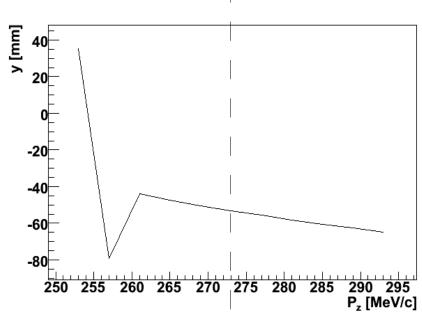
- Closed orbits for momenta between 250 290 MeV/c
 - Quite tightly bunched for momenta 260 290 MeV/c
 - Unstable below 260 MeV/c



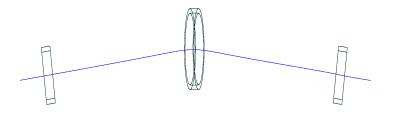
Closed Orbit vs Momentum

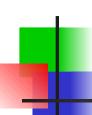






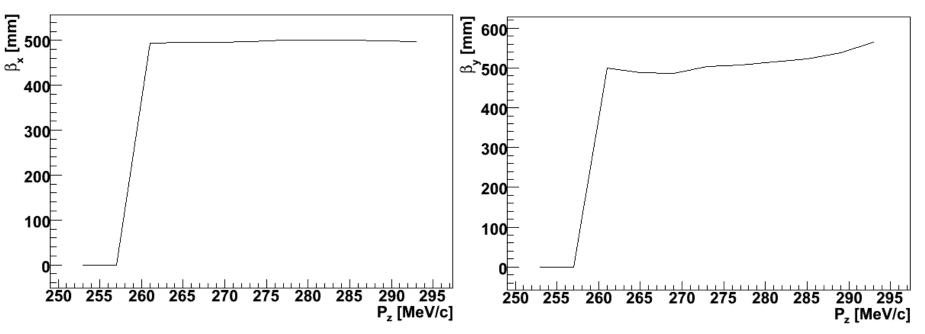
- Closed orbit at absorber moves by only ~20 mm over 30 MeV/c
 - If I want to put wedges in, I need to increase the dispersion here
 - At the moment I am tilting centre coil
 - May choose to tilt end coil
- Instability below ~ 260 MeV/c





Transverse optics





- Transverse optics looks quite reasonable
 - Quite achromatic above the instability
 - β ~ 500 is very reasonable for cooling
 - Momentum acceptance ~ 30 MeV/c is a little smaller than I would like

Continuing Work...



- An interesting candidate for a high energy cooling ring
 - Optics seems to be quite achromatic
 - I have not looked for spherical aberrations
- This has potential to make a cheap but efficient cooling channel
 - Very challenging to get a high emittance beam through
 - A kicker for this device would still be tough
- Would like to simulate full beam
- Would like to pursue aggressive optimisation





