

# **Introduction to Calorimetry**

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# Outline

- A short overview
- Particle shower basics
- Calorimeters
  - Sampling Calorimeters
  - Homogeneous Calorimeters
- Readout and DAQ
- Example systems
- Advanced Technologies
  - Particle Flow
  - Dual-Readout

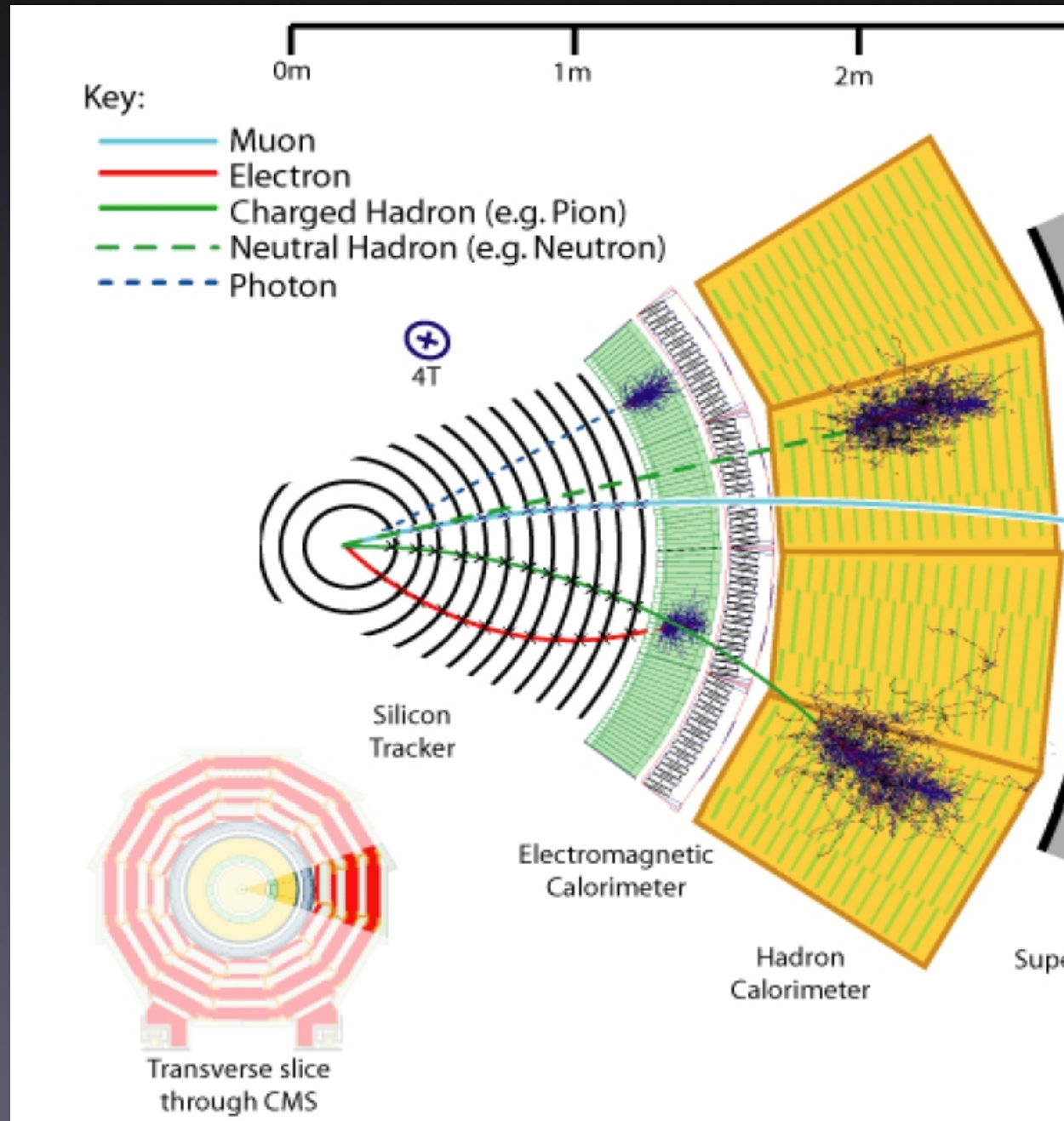
# Calorimetry -What is it?

- A calorimeter measures the energy of an incoming particle
  - Stopping the particle
  - Converting the energy into something detectable
  - Basic mechanism: electromagnetic/hadronic showers
  - The measured output is linear to the incoming energy
- It measures the location of the energy deposit
  - Allows “tracking” of neutrals, e.g. photons and neutrons
- A hermetic calorimetry is essential to measure “missing energy”
  - From all particles escaping detection
  - Neutrinos, Neutralinos and all that

# Calorimetry & Particles

- Only  $\sim 13$  Particles actually seen by a detector
  - Everything else is too short-lived
- Charged Hadrons
  - $\pi^\pm, p^\pm, K^\pm$
  - Generate hadronic Showers
- Electrons & photons
  - Generate Electromagnetic showers
- Neutral Hadrons
  - $n, K_L$
  - Generate hadronic Showers
- Muons
  - Usually only a track through the calorimeters

# As done in CMS

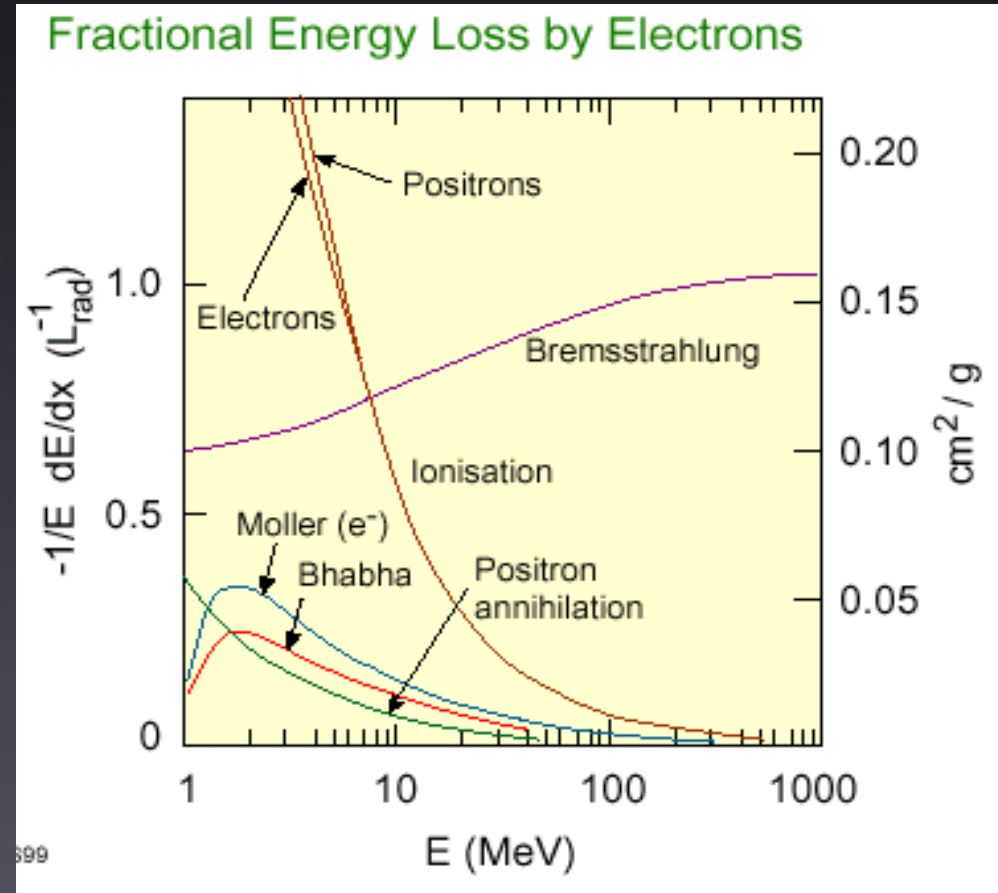


# Particle Showers

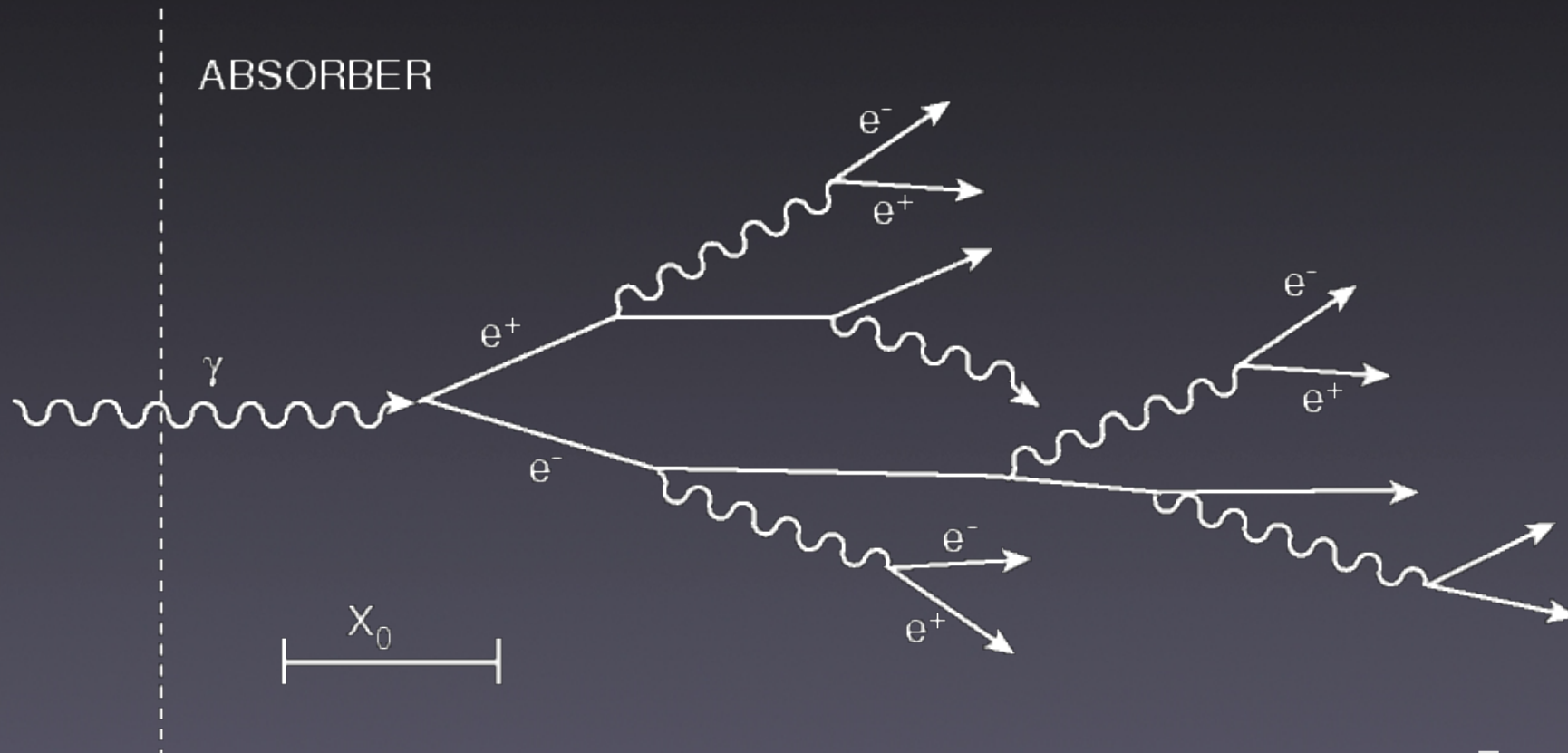
- Calorimeters stop particles by generating particle showers
- Two basic types
  - Electromagnetic showers
  - Hadronic showers
- Electromagnetic Showers
  - Driven by QED
  - Clean and simple
- Hadronic showers
  - Nuclear interactions and EM component
  - Quite complicated
  - Very difficult to model

# EM Interaction with Matter

- Electrons and photons as the main components
- Above  $\sim 1$  GeV
  - Electrons: Bremsstrahlung radiating off photons
  - Photons: Pair production
  - Increase of particles
- Below a critical energy  $E_C$ 
  - Ionization dominates
  - Shower slowly dies out
- Material dependent
  - Density  $\rho$
  - Number of Protons ( $Z$ ) and nucleons ( $A$ )



# EM shower basics



From T. Virdee



# EM Definitions

- Radiation length ( $X_0$ )

- When the energy has been reduced to  $1/e$
- Characterizes the shower depth

$$X_0 = \frac{716.4A}{Z(Z+1) \cdot \ln(287/\sqrt{Z})} \cdot \frac{1}{\rho}$$

- Critical Energy ( $E_C$ )

- Energy, where Ionization takes over

$$E_{C, \text{solid/liquid}} = \frac{610 \text{ MeV}}{Z + 1.24}$$

$$E_{C, \text{gas}} = \frac{710 \text{ MeV}}{Z + 0.92}$$

- Moliere Radius ( $r_{\text{Moliere}}$ )

- Radius which contains 90 % of the shower
- Characterizes the width of the shower

$$r_{\text{Moliere}} = 21.2 \text{ MeV} \frac{X_0}{E_C}$$

- Shower Max(imum)

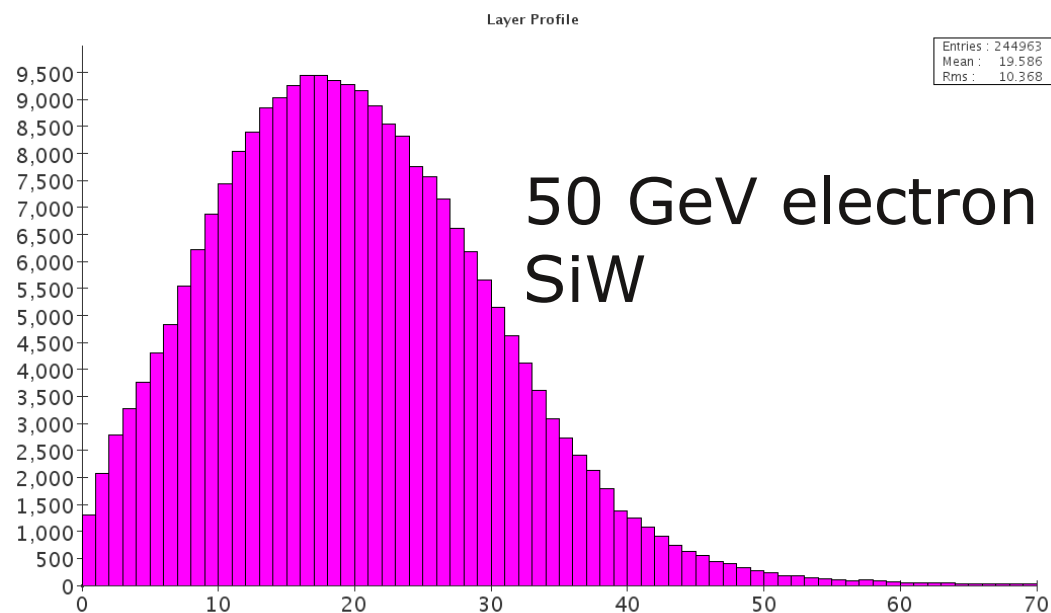
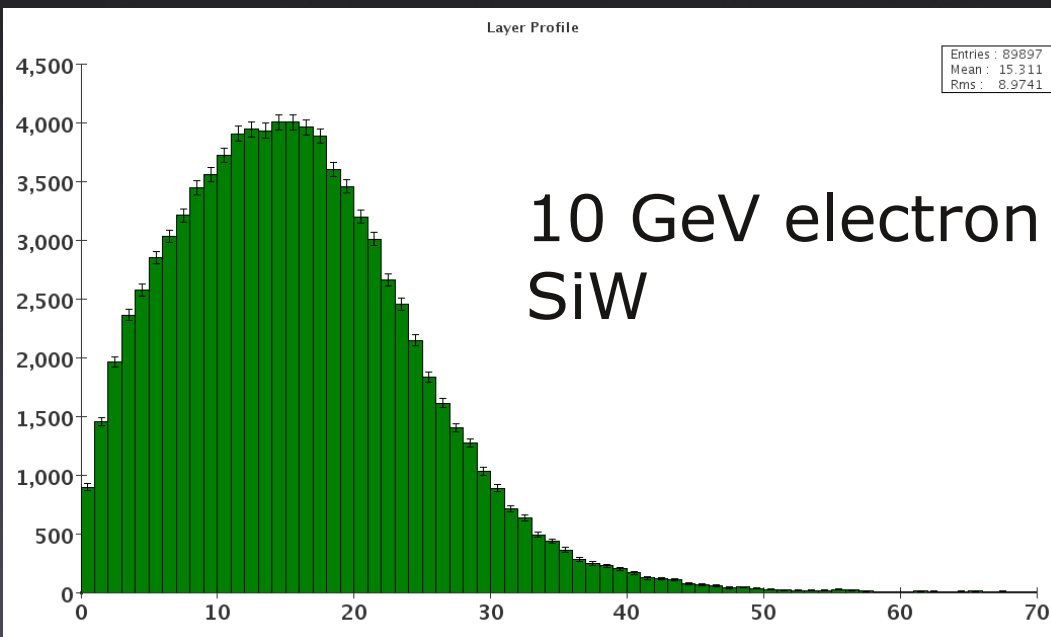
- The peak of the shower

$$S_{\text{max}} = \ln\left(\frac{E_{\text{Incoming}}}{E_C}\right)$$

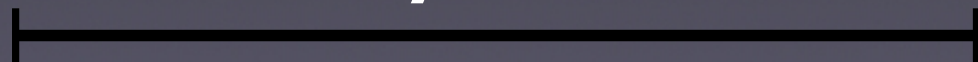
# Material Dependence

	<b>Z</b>	<b><math>\rho</math> (g/cm<sup>3</sup>)</b>	<b><math>X_0</math> (cm)</b>	<b><math>\lambda_{Int}</math> (cm)</b>
<b>C</b>	6	2.2	19	38.1
<b>Al</b>	13	2.7	8.9	39.4
<b>Fe</b>	26	7.87	1.76	16.8
<b>Cu</b>	29	8.96	1.43	15.1
<b>W</b>	74	19.3	0.35	9.6
<b>Pb</b>	82	11.35	0.56	17.1
<b>U</b>	92	18.7	0.32	10.5

# Shower Shapes



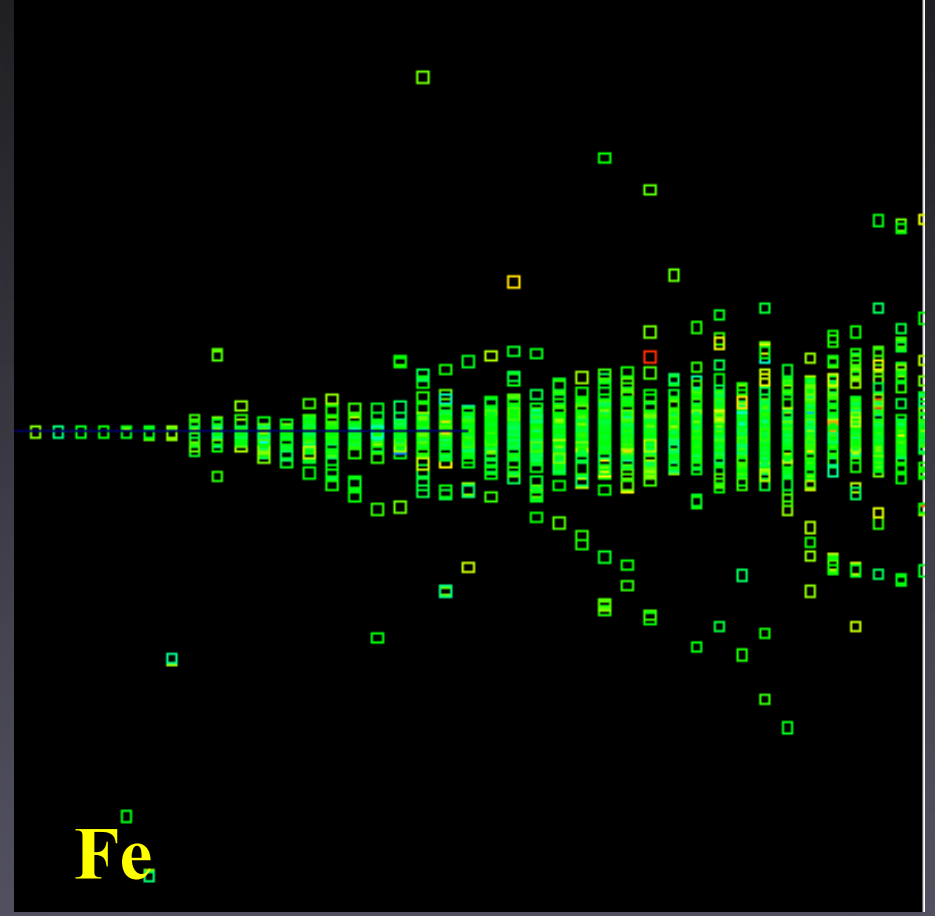
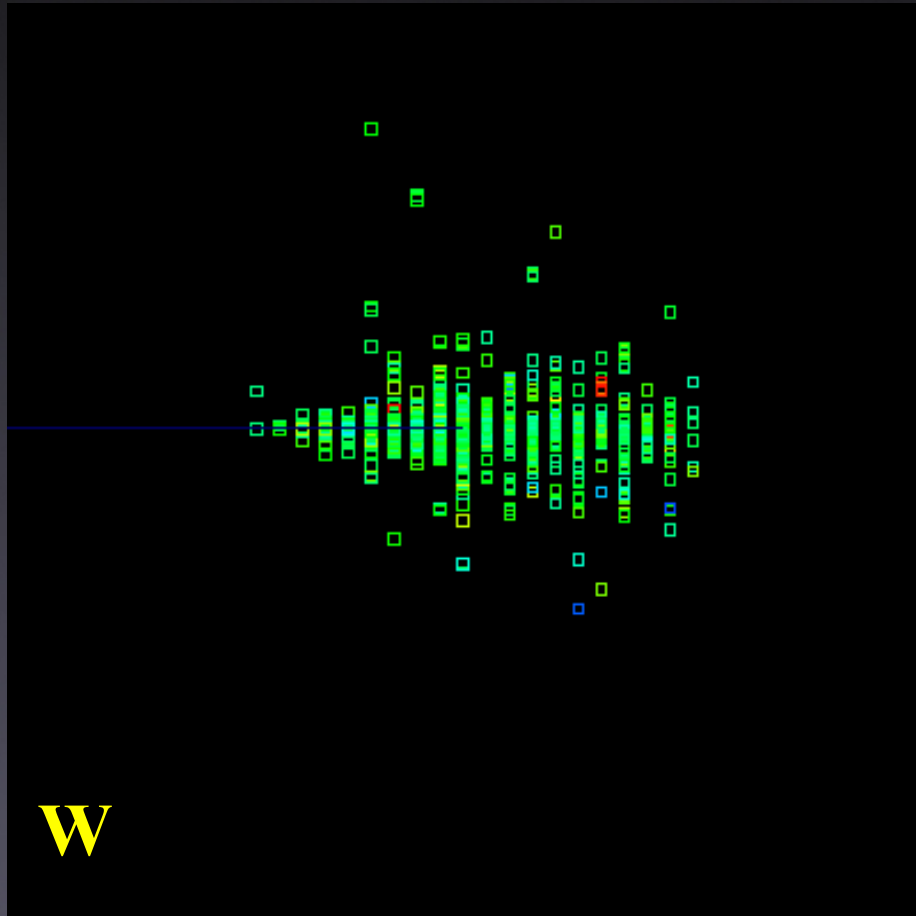
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25 cm

Layer

# EM Showers Pictures



**20 GeV electrons  
longitudinal shower profile**

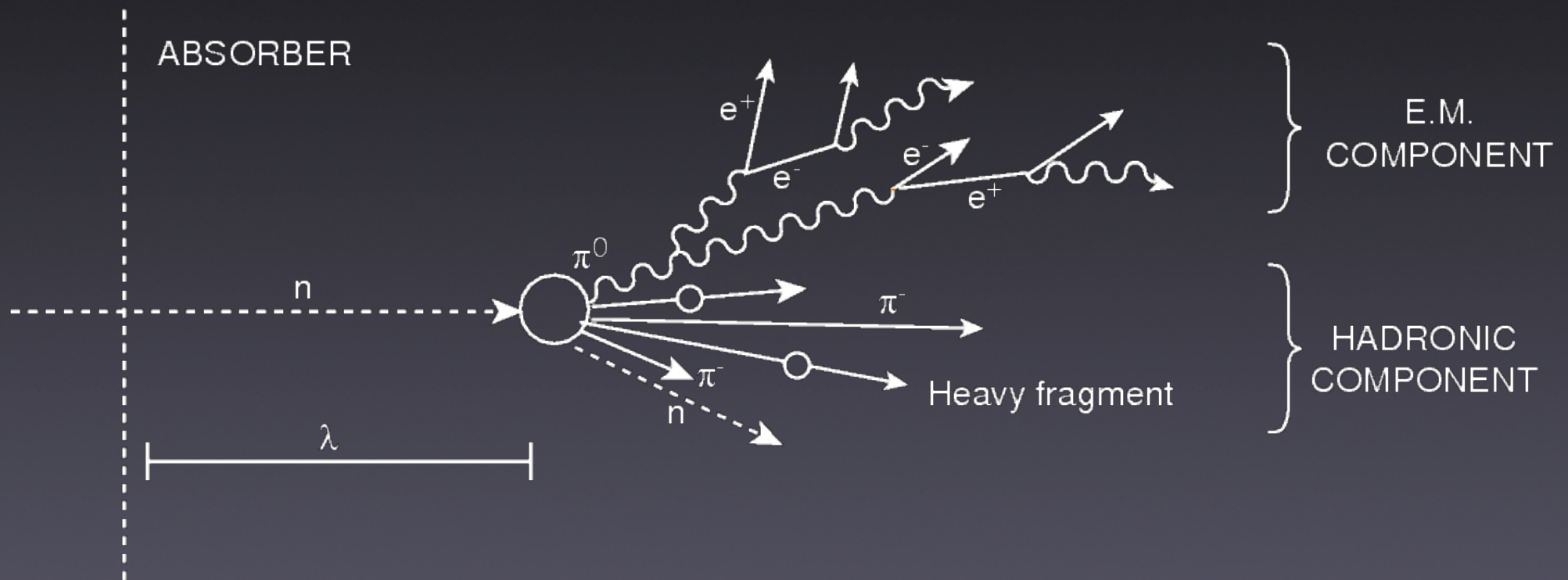
# Short Summary

- EM showers
  - dependent on density and  $Z$
- As  $Z$  increases
  - shower maximum shifts to greater depth
  - Slower decay after the Shower maximum
- The typical scale of EM showers is mm
  - A EM Calorimeter is not a very thick object
- Location of Shower max scales with  $\ln(E)$ 
  - Allows to build compact calorimeters !

# Hadronic Showers

- Hadronic showers are much more complex
- Incoming particle hits nucleus → secondaries
  - electromagnetic component (from  $\pi^0$ )
  - strong interaction component (from  $n, p, \pi^+$ )
    - fission ...
    - knock-off ...
    - Delayed photons
- Hadronic Showers are
  - much broader
  - extend deeper in the calorimeter
  - have significant event-by-event fluctuations

# Hadronic Shower basics



From T. Virdee

# Hadronic shower definitions

- Basic quantity is the nuclear interaction length

- Analog to the radiation length
- Order of magnitude larger

$$\lambda_I = \frac{A}{N_A \cdot \sigma_{Total}}$$

$$\lambda_I \sim A^{\frac{1}{3}}$$

- Only approximations for

- Shower max

$$S_{max}(\lambda_I) \sim 0.2 \cdot \ln(E) + 0.7$$

- Shower fractions

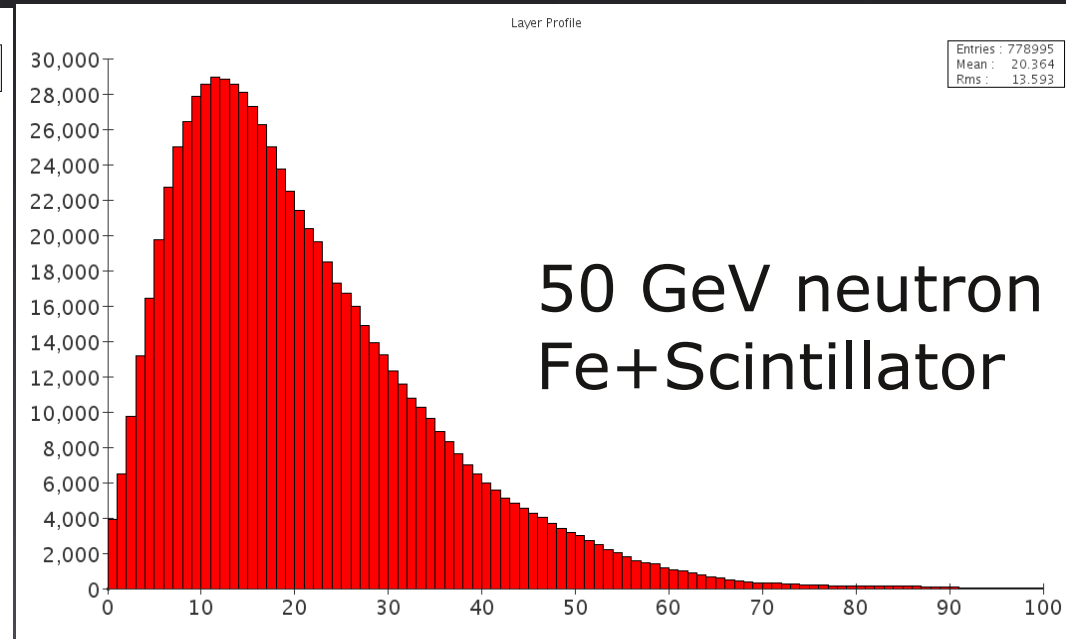
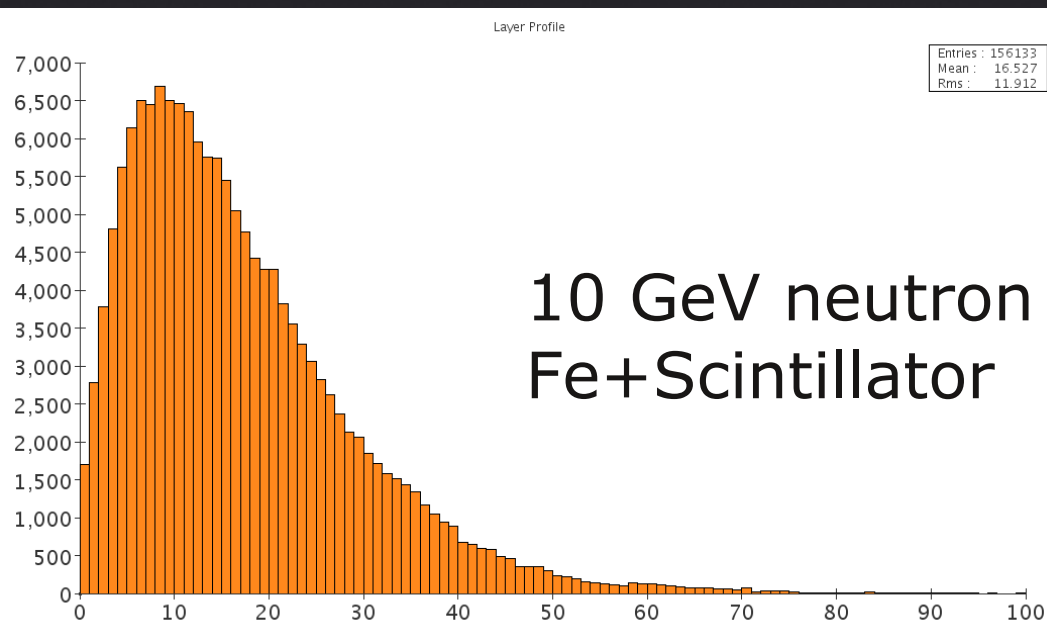
- $f_{EM}$  as electromagnetic fraction
- $f_{had}$  for the strong interaction fraction
- Generally  $f_{EM}$  increases with energy

$$f_{em} = 1 - \left(1 - \frac{1}{3}\right)^n$$

$$f_{em} = 1 - \left(\frac{E}{E_0}\right)^{(k-1)}$$



# Hadronic Shower Shapes

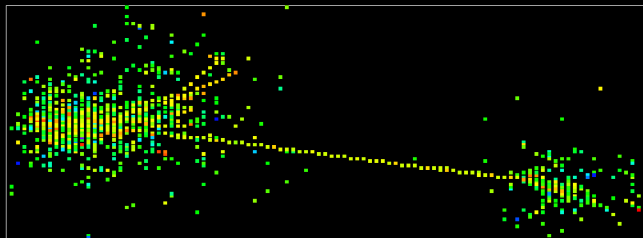
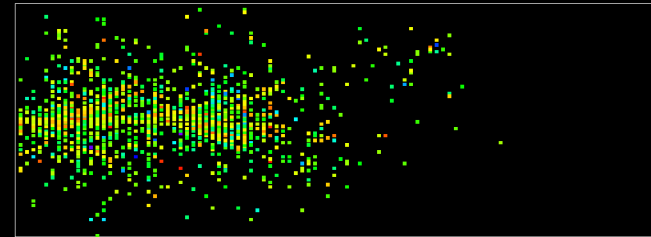
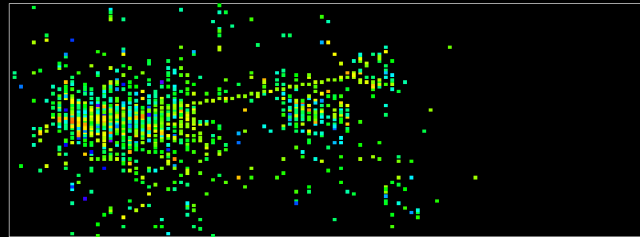
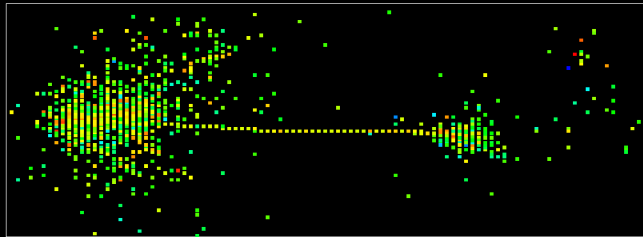
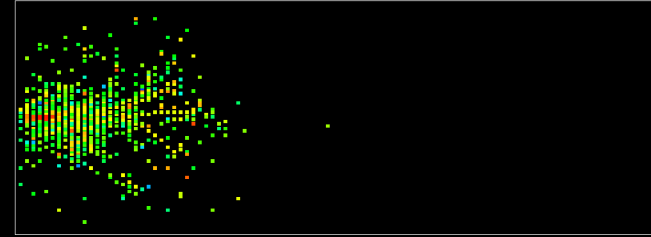
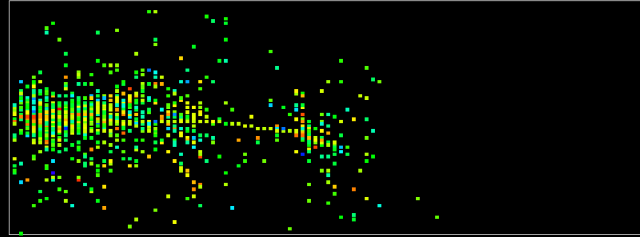
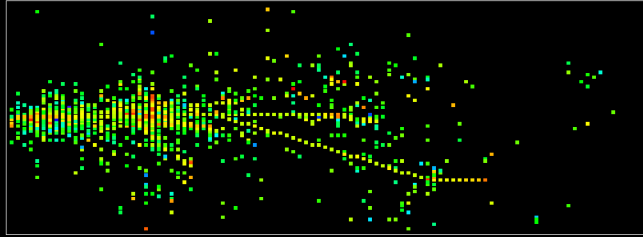


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275 cm

# Individual Showers

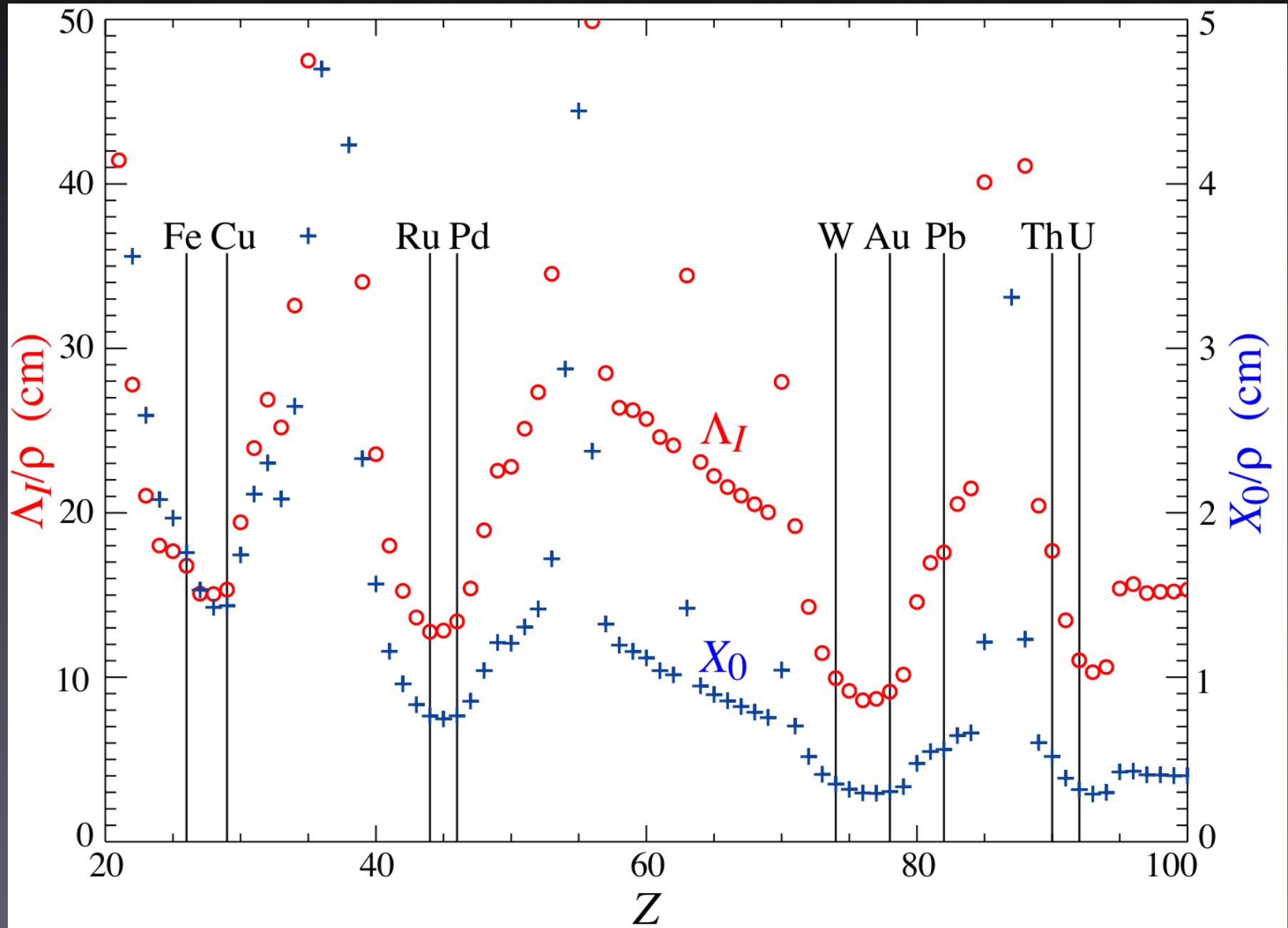


**50 GeV neutrons on  
Fe-Scintillator Stack**

# Selecting HCAL material

	<b>Z</b>	<b><math>\rho</math> (g/cm<sup>3</sup>)</b>	<b><math>X_0</math> (cm)</b>	<b><math>\lambda_{\text{Int}}</math> (cm)</b>
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# Materials again



# Compensation

- As already stated, hadronic showers have
  - electromagnetic component (e)
  - strong interaction component (h)
  - $e/h \neq 1$
- EM fraction increases with energy
  - Non-linearities
- Event by Event fluctuations
  - tend to be non-gaussian
  - Affect the resolution
- What can be done ?
  - Compensating calorimeters to achieve  $e/h=1$

# How to compensate ?

- Software-based
  - Try to reweight on a shower-by-shower basis
  - difficult
- Reduce EM-Component
  - High Z material for filtering out photo-electrons
- Boost hadronic response
  - mainly the neutron component
- Use of
  - Organic (hydrogen-rich) materials have a large neutron cross-section
  - Uranium (Nuclear fission triggered by neutrons)

# The Uranium question

- Depleted Uranium was en vogue for a while as absorber
  - Several Calorimeters, e.g. ZEUS, D0
- But compensation mainly due to
  - EM suppression
  - Boosting hadronic response
- The fission fragments carried lots of energy
  - But too slow to matter
- Uranium is a nasty material
  - Radioactive
  - Very reactive (grinds catch fire)
  - Mechanical properties
- These disadvantages made it unpopular

# Short summary

- Hadronic Showers
  - are very complex
- They have two components
  - electromagnetic
  - strong-interaction
- Electromagnetic fraction increases with energy
  - leads to non-linearity
- Compensation
  - trying to achieve  $e/h=1$



# Shower simulations

- EM Showers
  - Well-modeled using EGS4 or GEANT4 packages
  - Extensively validated using test beam data
- Hadronic showers
  - no preferred model
  - GEANT4 and FLUKA are most popular packages
  - Various compositions of models, so-called physics lists
  - One fit all doesn't exist
  - Test beam data used to tune the physics lists

# Calorimeter Resolution

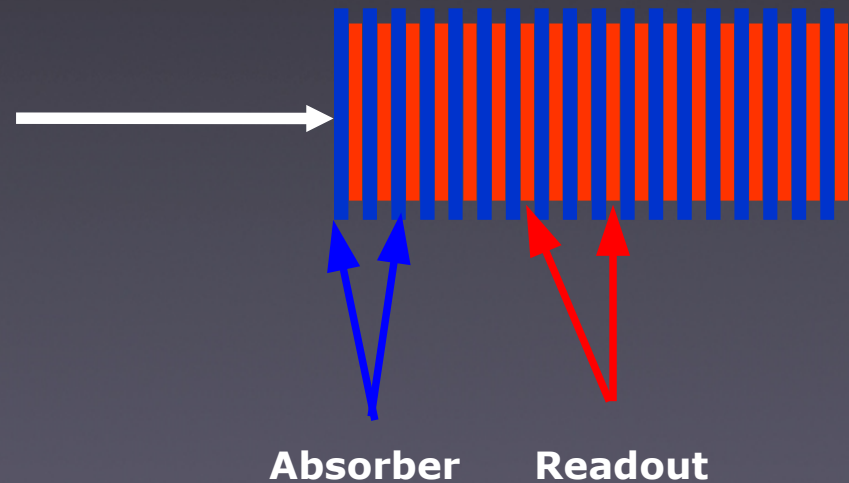
- Resolution is parametrized as

$$\frac{\sigma_E}{E} = \frac{a}{\sqrt{E}} \oplus \frac{b}{E} \oplus c$$

- a: Stochastic term
  - Fluctuations is the signal generating processes
- b: Noise Term
  - Due to read-out electronics
- c: Constant Term
  - Non-uniform detector response
  - Channel to channel inter-calibration errors
  - Fluctuations in longitudinal energy containment
  - Energy lost in dead material, before or in detector

# Calorimeter types

- Basically there are two classes
  - Homogeneous Calorimeters
  - Sampling Calorimeters
- Either type is extensively used for ECALs
- HCALs are almost exclusively sampling calorimeters
- Decision for either depends on application



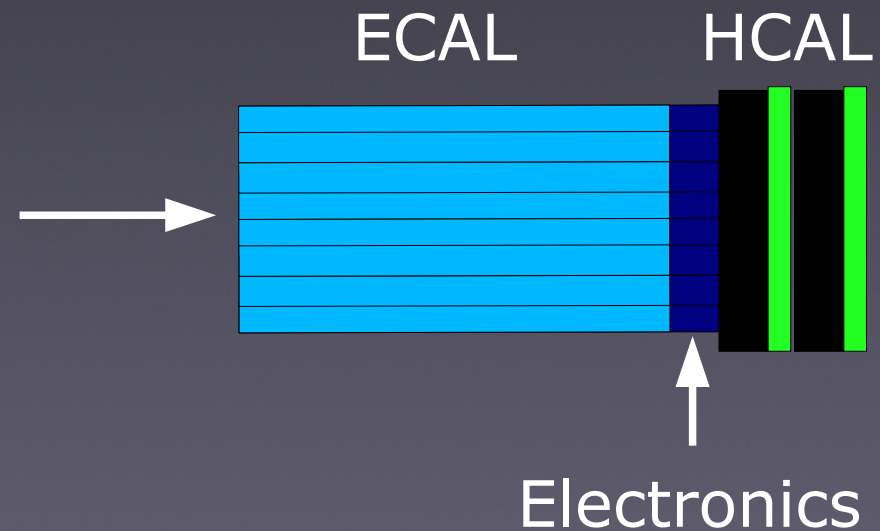
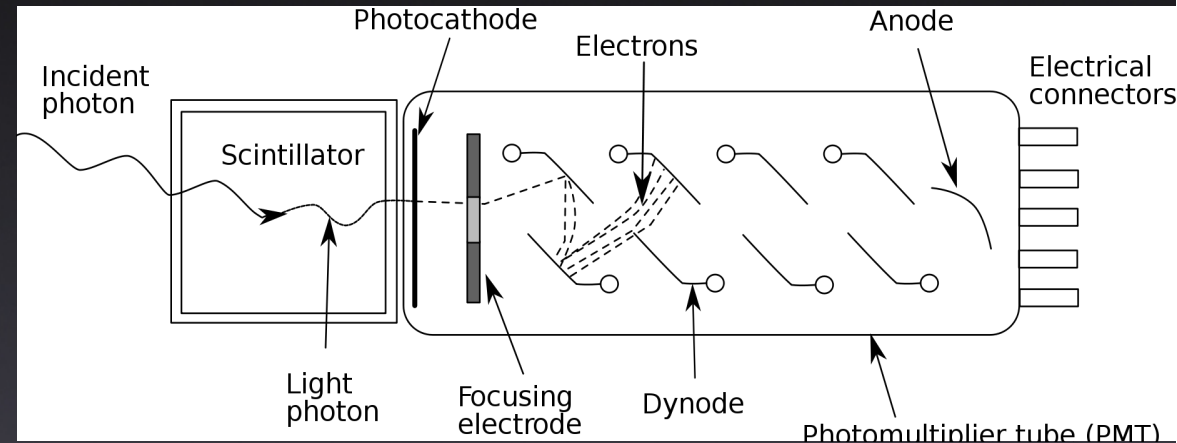
# Homogeneous Calorimeters

- Three ways to make one
  - Scintillating crystals
  - lead glass (Cerenkov light)
  - Noble gas liquids
- Either offers very good resolution
- Disadvantages
  - no direct longitudinal shower information
  - Crystals are expensive
  - very non-linear for hadrons

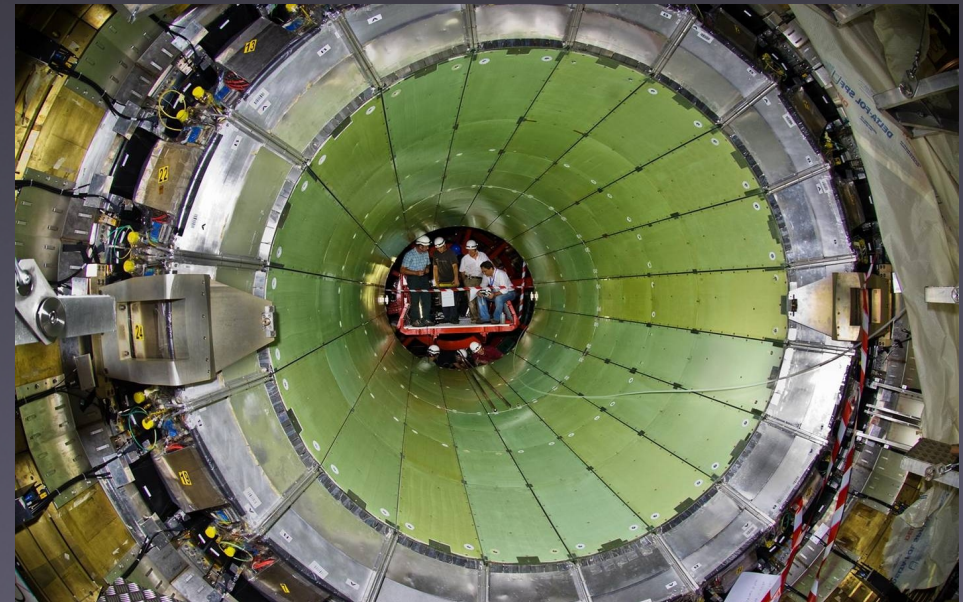
Parameter:	$\rho$	MP	$X_0^*$	$R_M^*$	$dE^*/dx$	$\lambda_I^*$	$\tau_{\text{decay}}$	$\lambda_{\text{max}}$
Units:	$\text{g/cm}^3$	$^\circ\text{C}$	cm	cm	MeV/cm	cm	ns	nm
NaI(Tl)	3.67	651	2.59	4.13	4.8	42.9	230	410
BGO	7.13	1050	1.12	2.23	9.0	22.8	300	480
BaF <sub>2</sub>	4.89	1280	2.03	3.10	6.5	30.7	630 <sup>s</sup> 0.9 <sup>f</sup>	300 <sup>s</sup> 220 <sup>f</sup>
CsI(Tl)	4.51	621	1.86	3.57	5.6	39.3	1300	560
CsI(pure)	4.51	621	1.86	3.57	5.6	39.3	35 <sup>s</sup> 6 <sup>f</sup>	420 <sup>s</sup> 310 <sup>f</sup>
PbWO <sub>4</sub>	8.3	1123	0.89	2.00	10.1	20.7	30 <sup>s</sup> 10 <sup>f</sup>	425 <sup>s</sup> 420 <sup>f</sup>
LSO(Ce)	7.40	2050	1.14	2.07	9.6	20.9	40	402
LaBr <sub>3</sub> (Ce)	5.29	788	1.88	2.85	6.9	30.4	20	356

# Read-out

- Mostly light-based
  - tends to be blue
- Classical
  - Photomultiplier
- Advanced
  - Avalanche Photo-Diodes
  - Silicon-Photo-multipliers
- Caveat
  - Readout electronics always at the end
  - highly non-linear for hadrons



# The CMS ECAL



# Target Applications

- ECAL only systems
  - e.g. B-Factories
  - generally medium energy machines
- Good ECAL is essential
  - no Jet physics at all
- Examples
  - BaBar, Belle
  - KTeV
- ECAL+ HCAL
  - If ultimate ECAL resolution is needed
  - e.g.  $H \rightarrow \gamma\gamma$
- Necessary compromise on HCAL performance
- Examples
  - CMS
  - L3

# Example systems

Technology (Experiment)	Depth	Energy resolution	Date
NaI(Tl) (Crystal Ball)	$20X_0$	$2.7\%/E^{1/4}$	1983
$\text{Bi}_4\text{Ge}_3\text{O}_{12}$ (BGO) (L3)	$22X_0$	$2\%/\sqrt{E} \oplus 0.7\%$	1993
CsI (KTeV)	$27X_0$	$2\%/\sqrt{E} \oplus 0.45\%$	1996
CsI(Tl) (BaBar)	$16\text{--}18X_0$	$2.3\%/E^{1/4} \oplus 1.4\%$	1999
CsI(Tl) (BELLE)	$16X_0$	1.7% for $E_\gamma > 3.5$ GeV	1998
$\text{PbWO}_4$ (PWO) (CMS)	$25X_0$	$3\%/\sqrt{E} \oplus 0.5\% \oplus 0.2/E$	1997
Lead glass (OPAL)	$20.5X_0$	$5\%/\sqrt{E}$	1990
Liquid Kr (NA48)	$27X_0$	$3.2\%/\sqrt{E} \oplus 0.42\% \oplus 0.09/E$	1998
Scintillator/depleted U (ZEUS)	$20\text{--}30X_0$	$18\%/\sqrt{E}$	1988
Scintillator/Pb (CDF)	$18X_0$	$13.5\%/\sqrt{E}$	1988
Scintillator fiber/Pb spaghetti (KLOE)	$15X_0$	$5.7\%/\sqrt{E} \oplus 0.6\%$	1995
Liquid Ar/Pb (NA31)	$27X_0$	$7.5\%/\sqrt{E} \oplus 0.5\% \oplus 0.1/E$	1988
Liquid Ar/Pb (SLD)	$21X_0$	$8\%/\sqrt{E}$	1993
Liquid Ar/Pb (H1)	$20\text{--}30X_0$	$12\%/\sqrt{E} \oplus 1\%$	1998
Liquid Ar/depl. U (DØ)	$20.5X_0$	$16\%/\sqrt{E} \oplus 0.3\% \oplus 0.3/E$	1993
Liquid Ar/Pb accordion (ATLAS)	$25X_0$	$10\%/\sqrt{E} \oplus 0.4\% \oplus 0.3/E$	1996



# Sampling Calorimeters

- Most Calorimeters in HEP are sampling calorimeters
- Provide high granularity both lateral and longitudinal
- Two ingredients
  - active (readout)
  - passive(absorber)

- Sampling fraction as key parameter

$$SF = \frac{\Delta E_{active}}{\Delta E_{active} + \Delta E_{passive}}$$

- May ways of building sampling Calorimeters
  - Sandwich
  - Spaghetti
  - ....
- Sandwich Calorimeters have been the most popular

# The CDF calorimeter



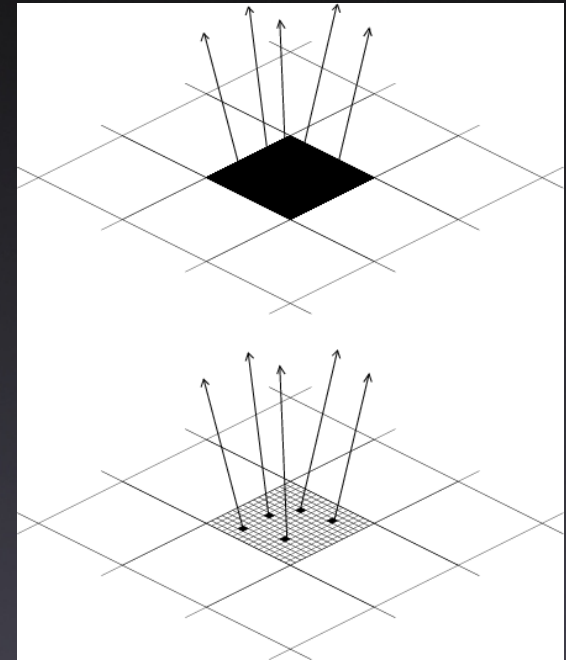
# Read-Out strategies

- Two main ideas
- Light
  - Scintillator
- Charge
  - Silicon
  - Gas detectors
  - Liquid noble gases
- Either with the benefits and disadvantages
- First question is, though
- Analog (classic) or digital (new fashion)

# Analog vs. digital readout

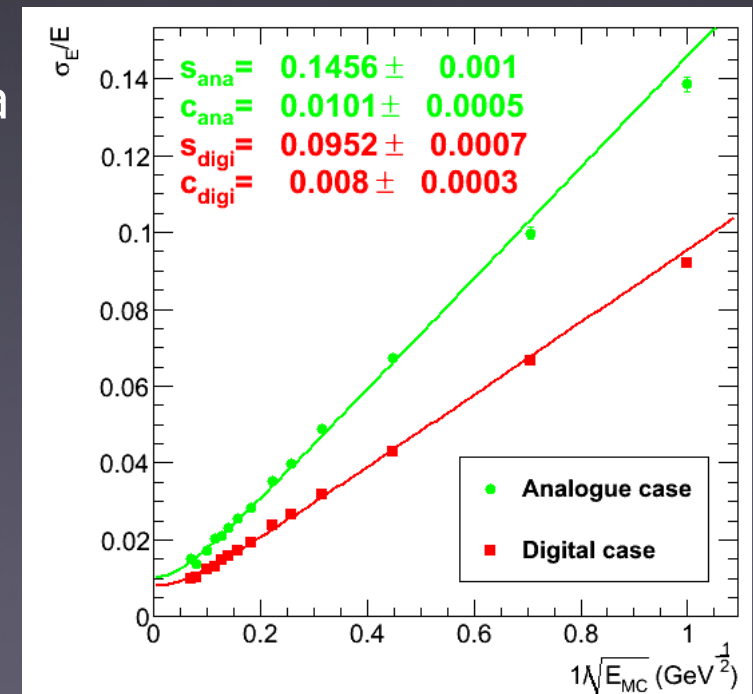
- Analog Readout

- measures the energy deposited by the shower
- Fluctuations around the average occur due to angle of incidence, velocity and Landau spread

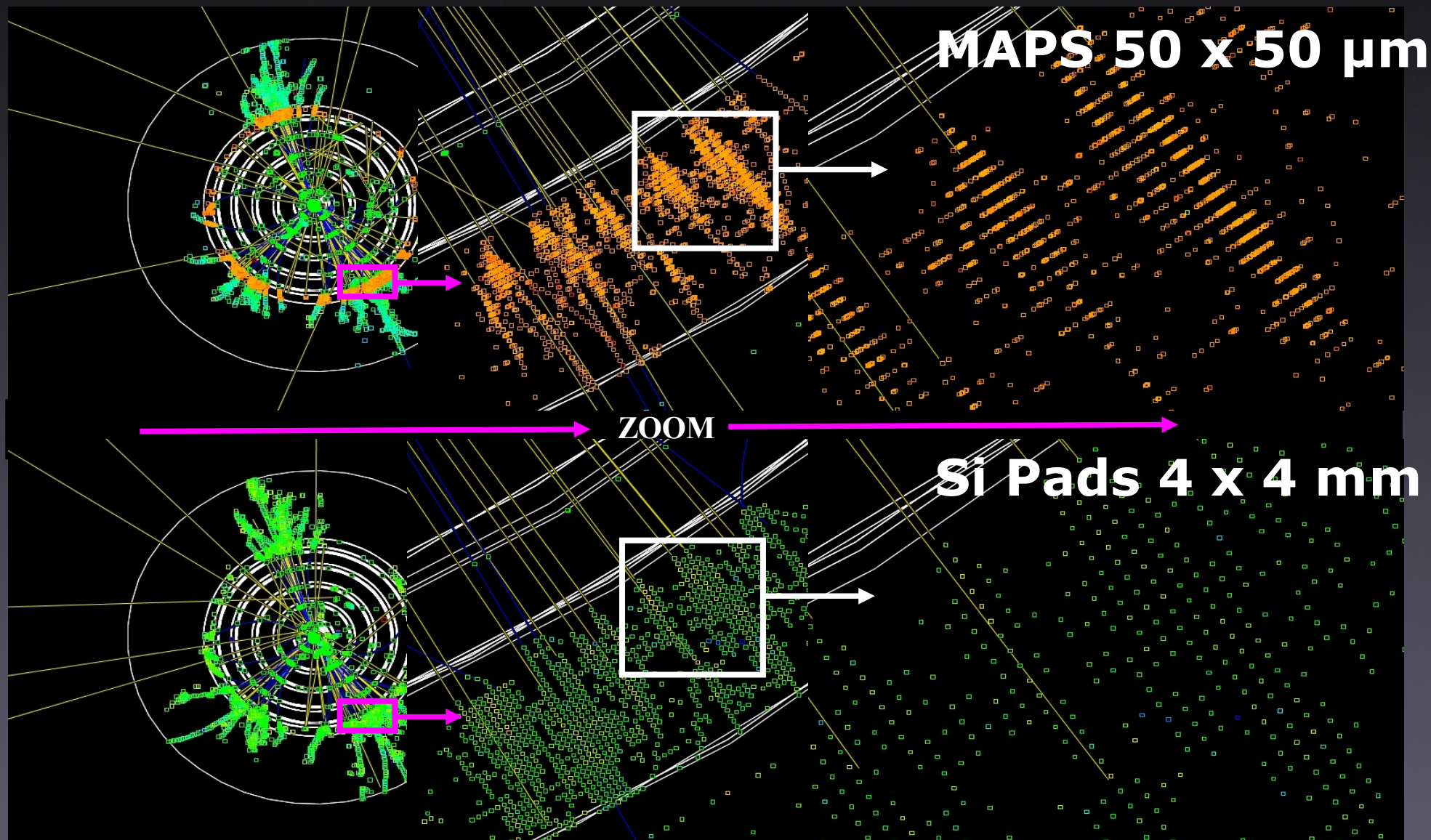


- Digital Readout

- counts the number of particles in a shower
- Number of charged particles is an intrinsically better measure than the energy deposited
- Needs very high granularity otherwise limited by multiple hits per cell

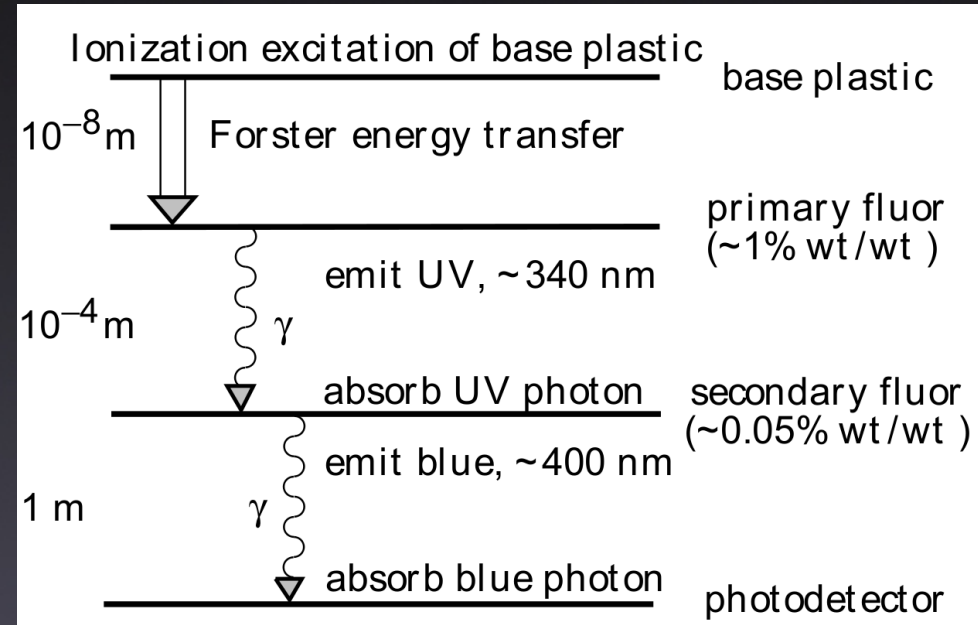


# An Example



# Scintillator-based readout

- Usually talking about
  - organic scintillators
  - aka plastic
- Wave-length shifting to improve light detection
- Fibers to connect the read-out
  - read out same as for e.g. crystals
- Easy to build calorimeter towers
- Lots of experience already with this technology



# However

- A word of warning (R. Wigmans, Calorimetry)
  - The detector is inherently non-uniform
  - The detector is inherently unstable
- Reasons
  - Scintillation is very sensitive to the environment
  - Moving light to the readout is necessarily non-uniform
  - Aging ...
  - PMTs, Silicon-PMs etc are all temperature dependent
- This means careful monitoring and calibration

# Other approaches

- Silicon-Pads
  - analog to a Silicon tracker
  - See Giulio Villani's talk
- Liquid Noble Gases
  - Argon is most popular
- Micro-Pattern Gas detectors
  - RPC
  - GEM
  - Micromegas
  - Most of them suited as digital counters



# RPC

- Resistive Plate Chambers

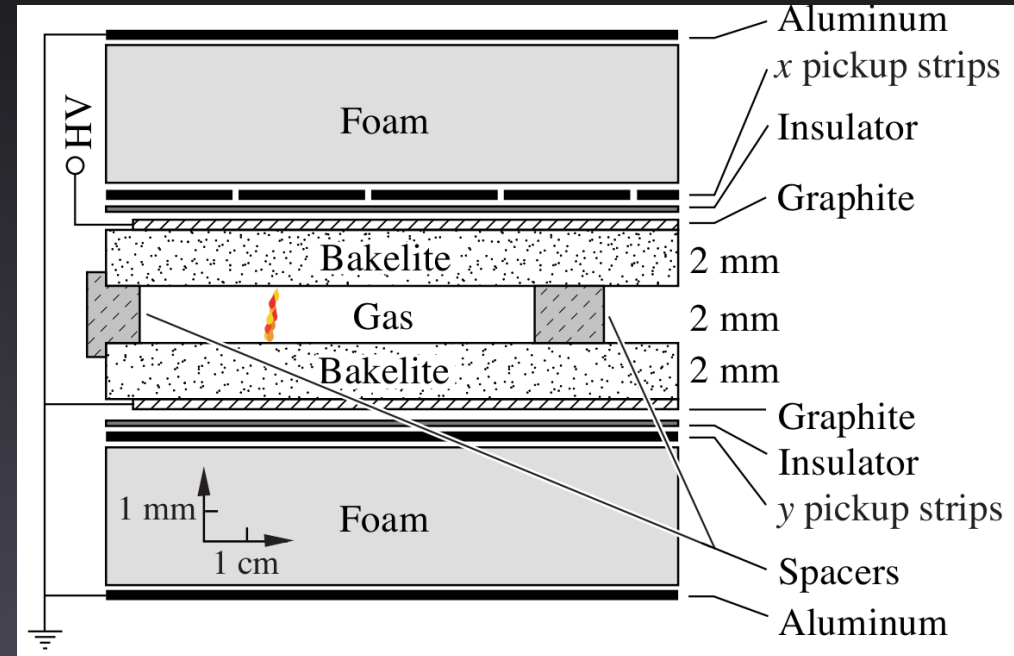
- cheap alternative to scintillators

- Idea

- 2 high resistivity plates with gas in between
- Particle triggers discharge
- Self-resetting

- Signal readout capacitive coupling

- Very high segmentation is possible



# GEM & Micromegas

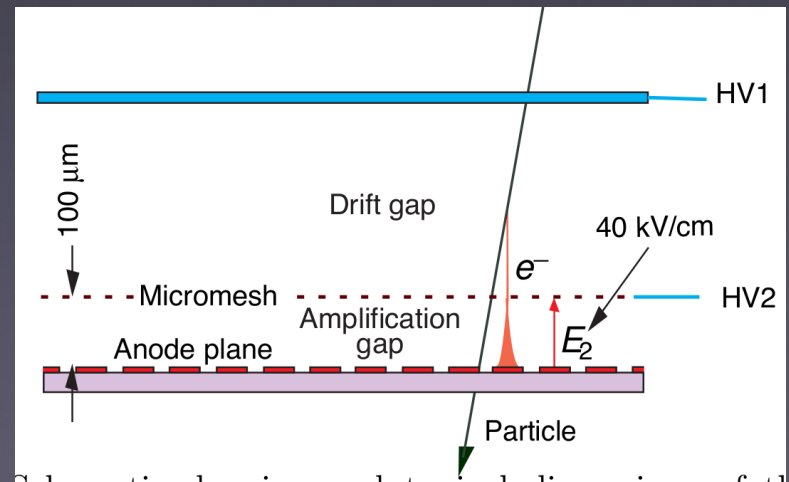
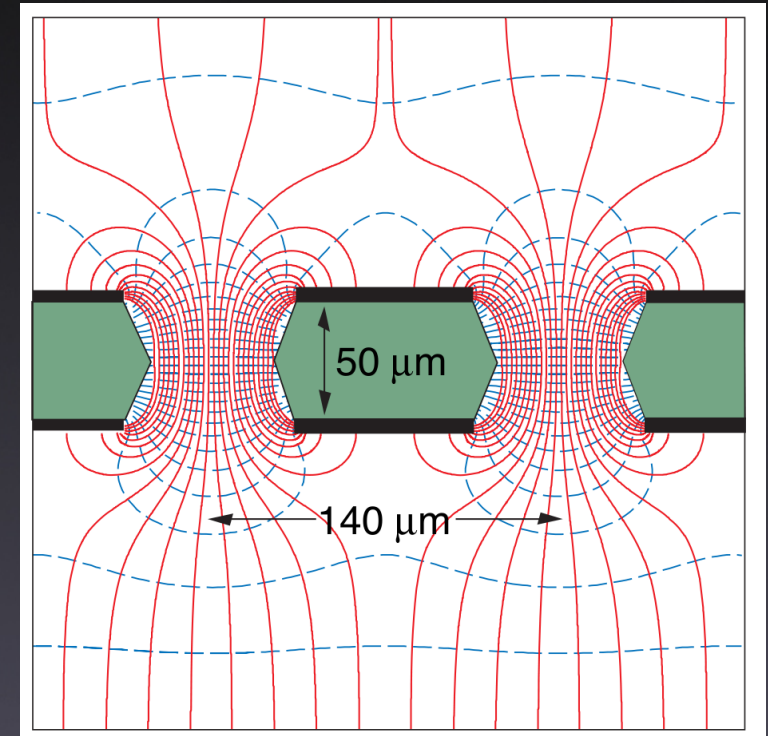
- GEM

- perforated copper-kapton foil with field
- pitch  $\sim 100 \mu\text{m}$
- Charge amplification in the holes

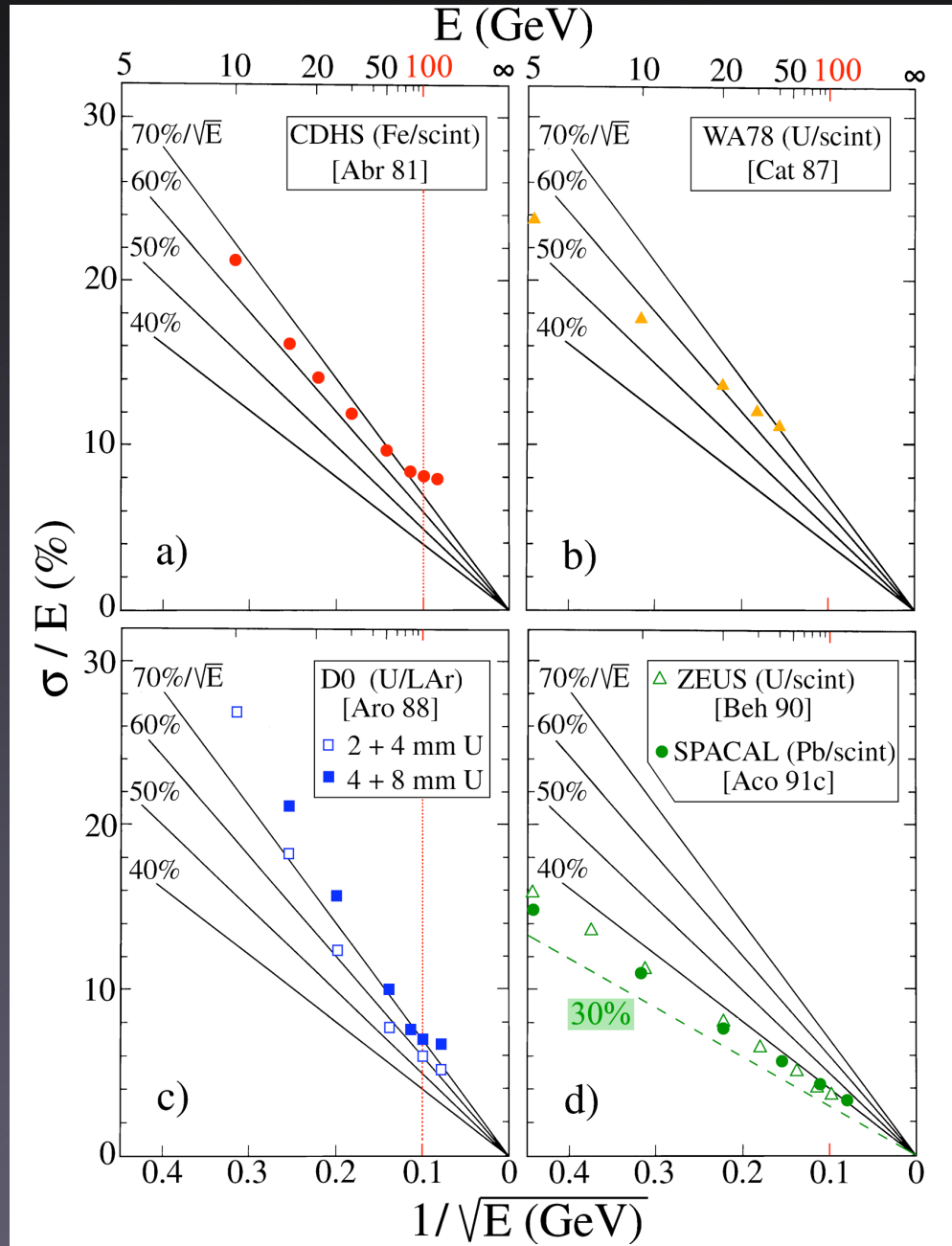
- MicroMegas

- large Drift region
- small amplification region
- small metal mesh as separator

- Both of high-rate and fast signals



# Typical HCAL performance



# Short summary

- Two types of calorimeter
  - homogeneous
  - sampling
- Each with the unique advantages
- Readout can be realized in many ways
  - light collection
  - charge collection
- The target application drives the technology choice

# System design

- So far only talked about “the building blocks”
- A complete system is a different matter
- Various constraints
  - Space
  - Channel count
  - Services
  - Costs
- and derived parameters
  - Depth & Leakage
  - Segmentation
  - Dead areas

# The ideal calorimeter

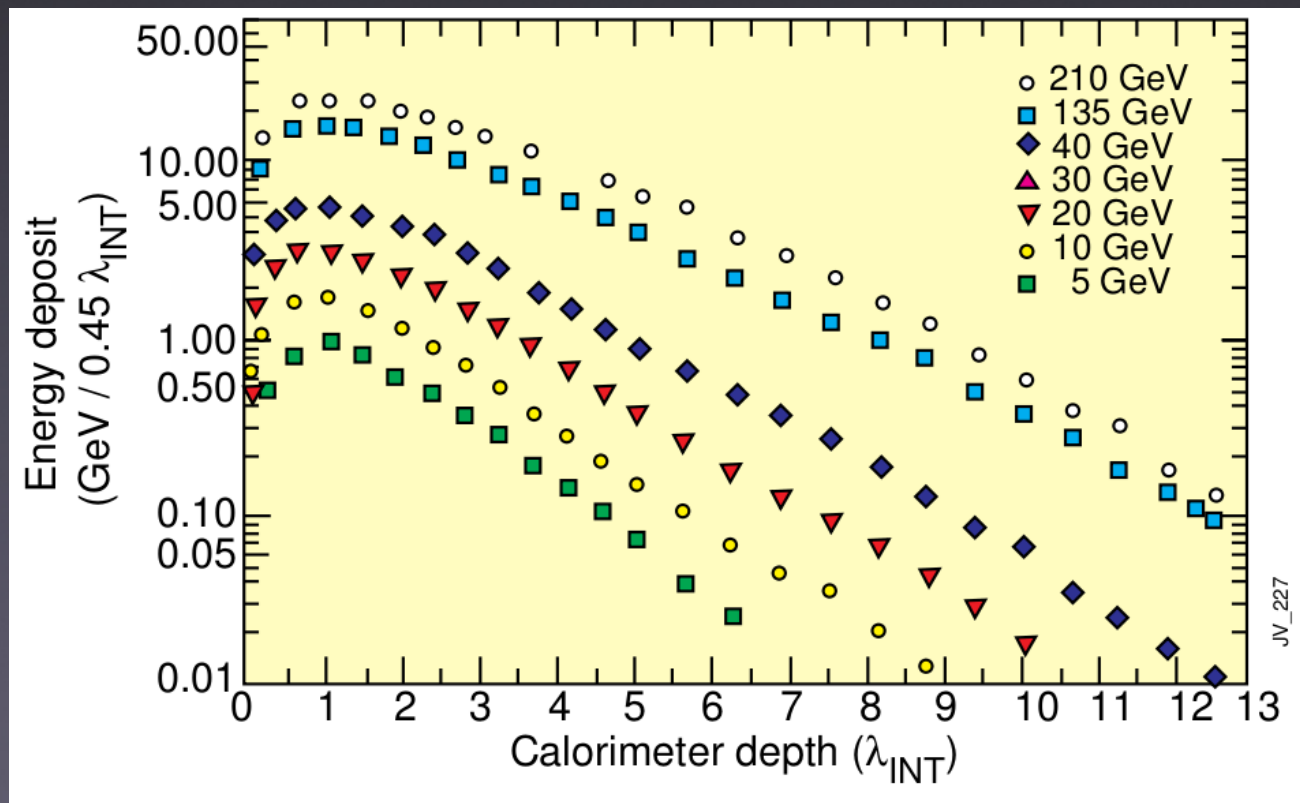
- Is infinitively deep
  - no leakage
- if infinitely fine segmented
  - and has no cracks
- needs no power or readout
  - hence no services
- Weighs nothing
  - no mechanical support

# Space Constraints

- Calorimeter sits
  - either between tracker and coil
  - or is located (partially) outside the coil
- In the first case, the coil limit the size
  - of both tracker and calorimeter
  - Limiting factor are coil forces and cost
- This forces the choice of very dense material
  - like e.g. Tungsten or Steel
- Locating the calorimeter outside
  - impacts the physics as well
  - Coil is dead material

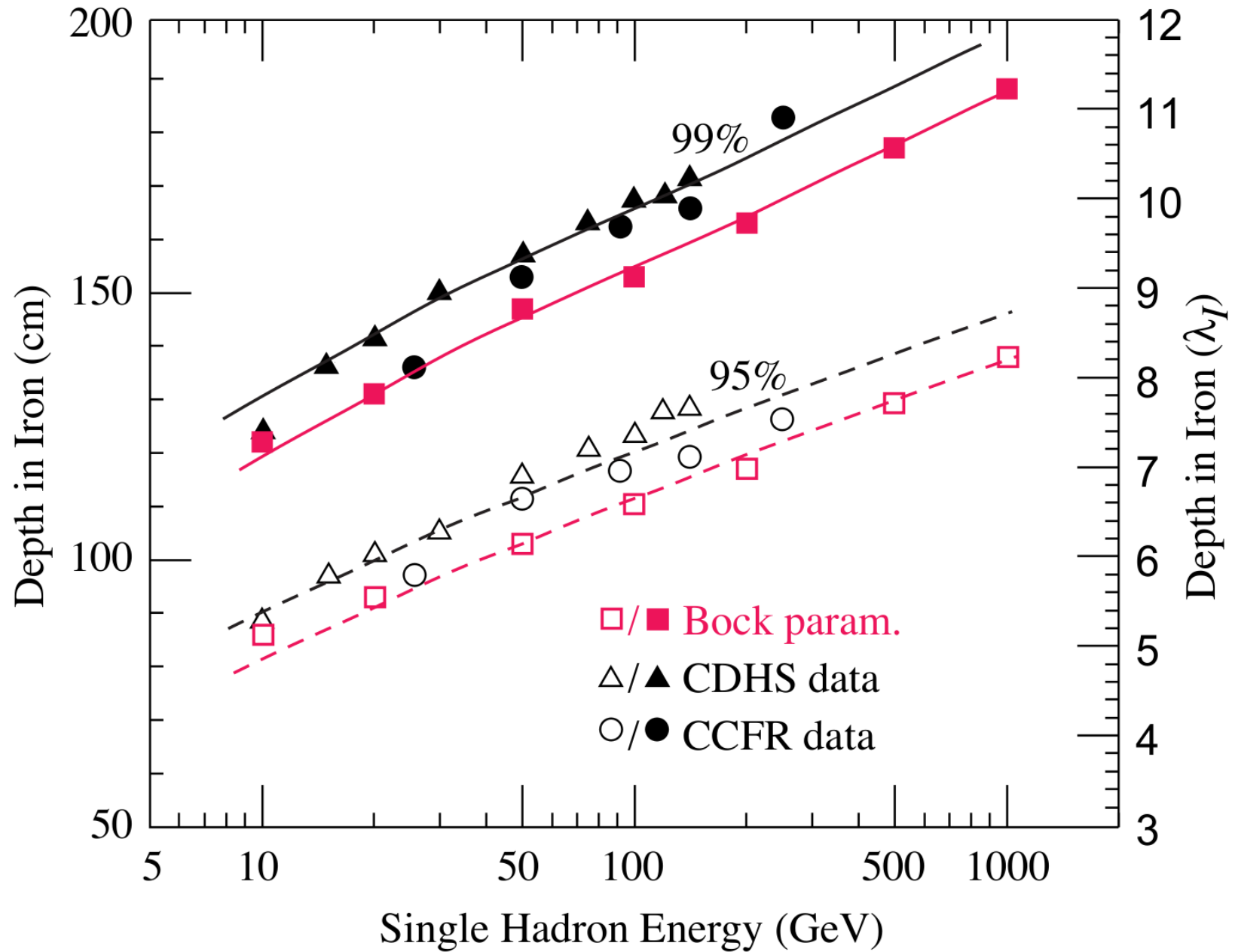
# Leakage

- Can't make a calorimeter infinitely deep
  - So need a compromise
- Adding radiation length is expensive ...
  - Solid physics case required





# Cont'd



# Mechanics and Services

- Given the materials, Calorimeters are massive objects
  - CMS ECAL Barrel 68 t ( $\text{PbWO}_4$  crystals)
  - ZEUS Calorimeter (Uranium) 700 t
- Mechanical support becomes crucial design feature
- Power consumption is equally impressive
  - Single channel  $\sim$  a few 10 mW
  - But  $10^6$  channels so, 10 kW
- Cables
  - Running cables & fibers leads to cracks
  - Impact on performance

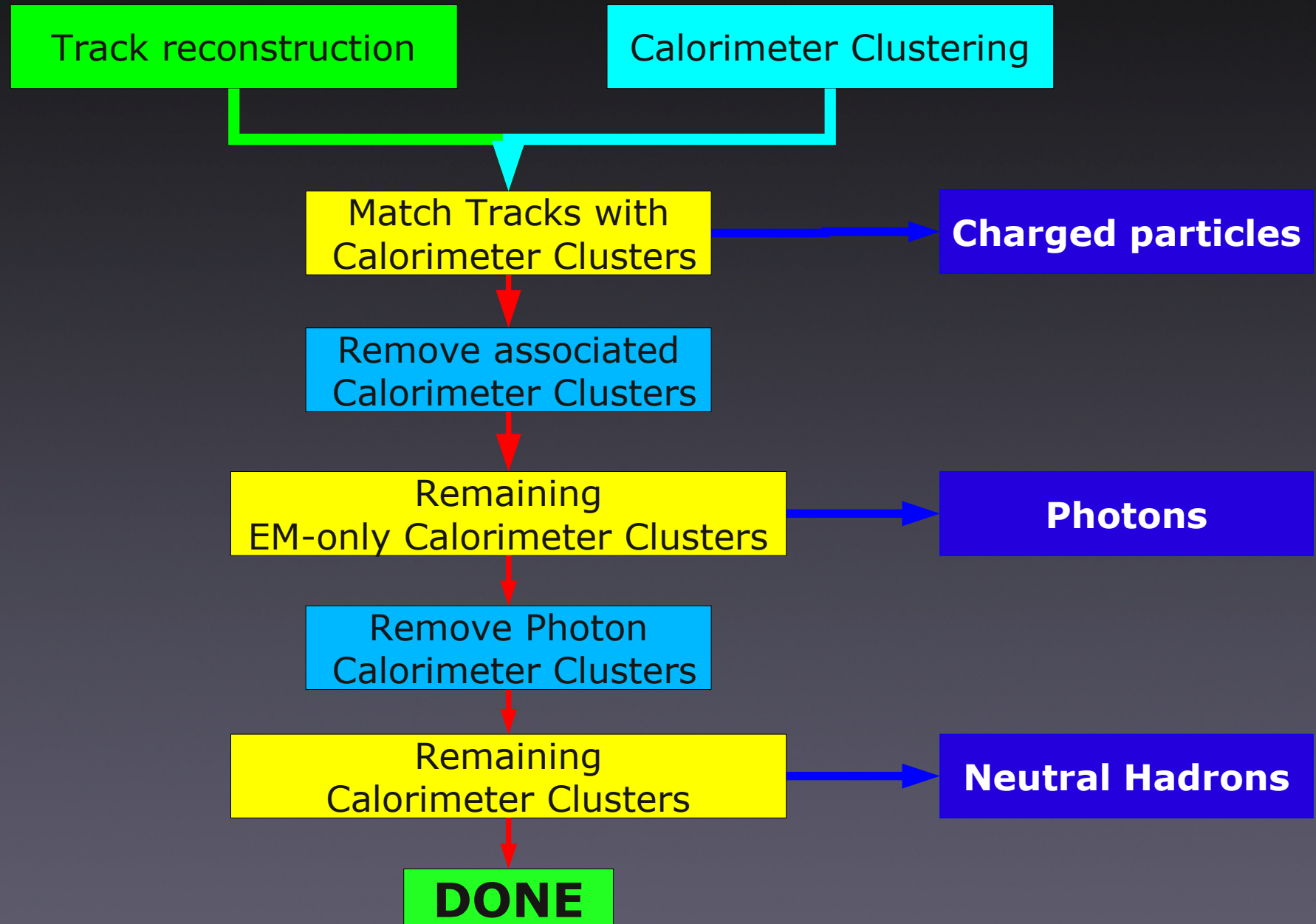
# Advanced ideas

- Calorimetry R&D is an active field
- Advances in both electronics and material
  - Dealing with large amount of channels
  - new crystal materials
  - Silicon Photomultiplier & Large Area Silicon Detectors
- These allows exploring new ideas
  - Particle Flow Algorithms
  - Dual Readout Calorimetry

# Particle Flow Algorithms

- Observation : Track measurements much better than calorimetric ones
  - Usually true up to several 100 GeV
  - Average particle momentum is more  $O(10 \text{ GeV})$
- So use Tracker to measure the energy
  - Assuming all charged hadronic tracks are pions
  - Lepton-ID for electrons, muons
- Use Calorimeter only for
  - Neutral hadrons and photons
- Remove Calorimetry from the energy measurement

# PFA in a nutshell



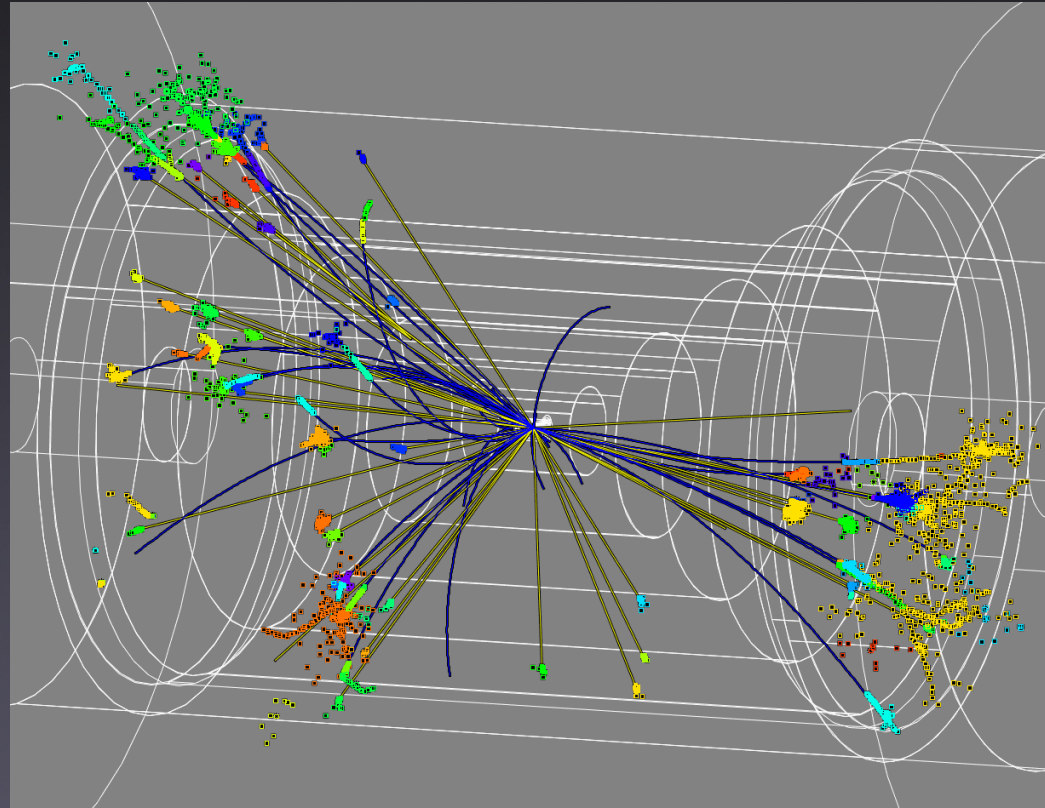
# Jet Resolutions

Particle Class	SubDetector	Jet energy fraction	Particle Resolution	Jet Energy Resolution
Charged	Tracking	60%	$10^{-4} \sqrt{E}_{\text{charged}}$	neg.
Photons	ECAL	30%	11 % $\sqrt{E}_{\text{EM}}$	6 % $\sqrt{E}_{\text{jet}}$
Neutral Hadrons	HCAL (+ECAL)	10%	40 % $\sqrt{E}_{\text{hadronic}}$	13 % $\sqrt{E}_{\text{jet}}$

- Energy resolution about 14% (driven by HCAL)
- Confusion terms have bigger impact
  - $\sigma_{\text{jet}}^2 = \sigma_{\text{charged}}^2 + \sigma_{\text{EM}}^2 + \sigma_{\text{hadronic}}^2 + \sigma_{\text{confusion}}^2 + \sigma_{\text{threshold}}^2 + \dots$
- Performance not limited by Calorimetry
  - Need high granularity to reduce confusion !

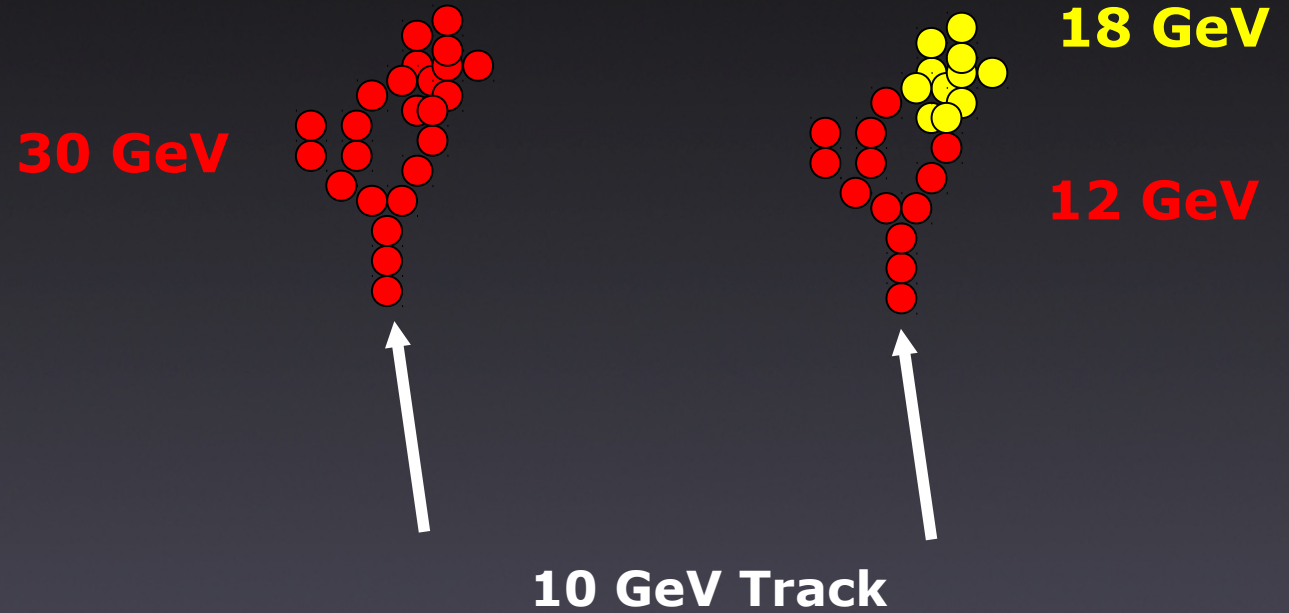
# Sounds easy

- Associating showers to tracks
  - showers can overlap
  - track ambiguities
  - leakage
- Hadronic showers are very difficult
  - As you already know

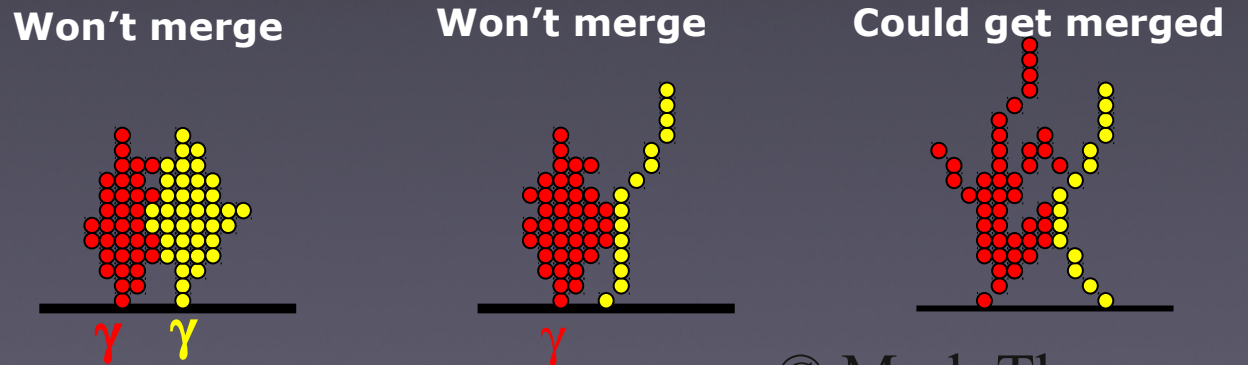


# Matching problems

## Shower matching



## Shower merging



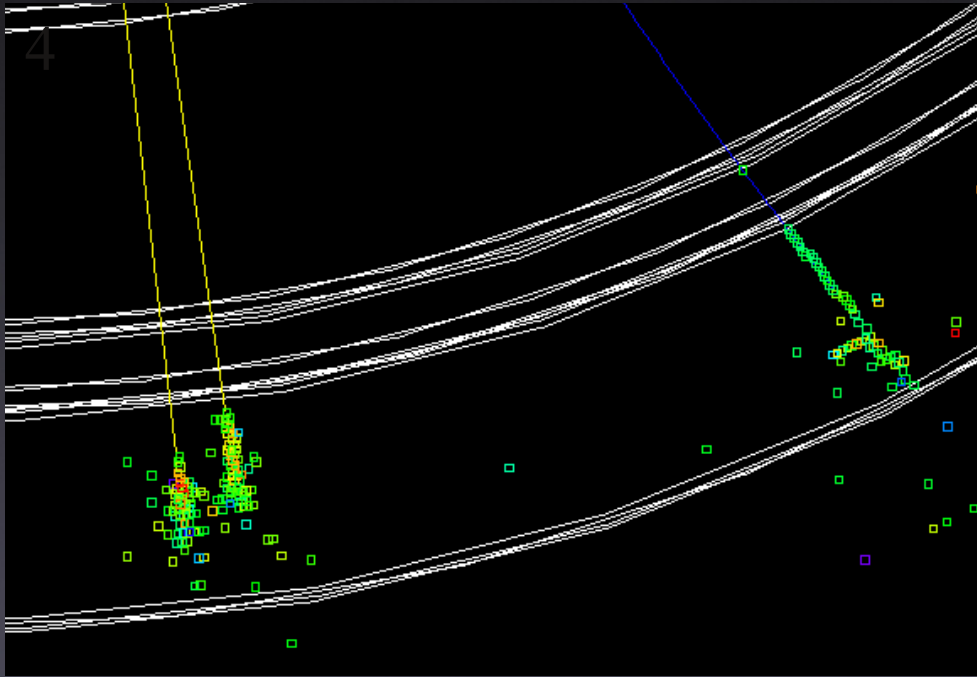
© Mark Thomson



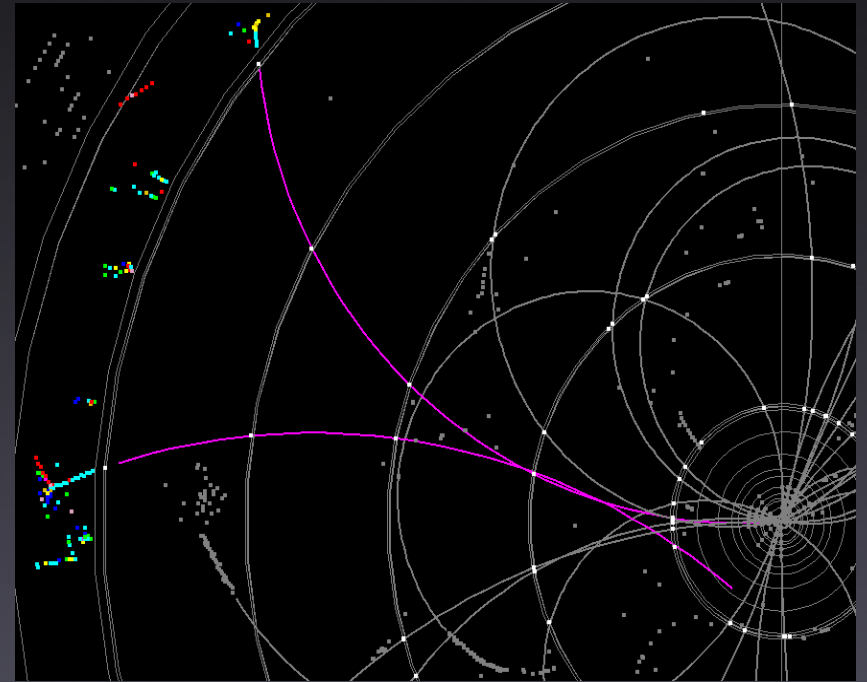
# PFA design considerations

- Highly granular
  - For Shower separation and matching
  - mm for ECAL, cm for HCAL
- Sampling Calorimeters with decent energy resolution
  - containment is an issue
- Minimize dead material
  - Fit inside the coil
  - Compact
- Calorimetry must also
  - Pass engineering constraints
  - Affordable

# Other benefits

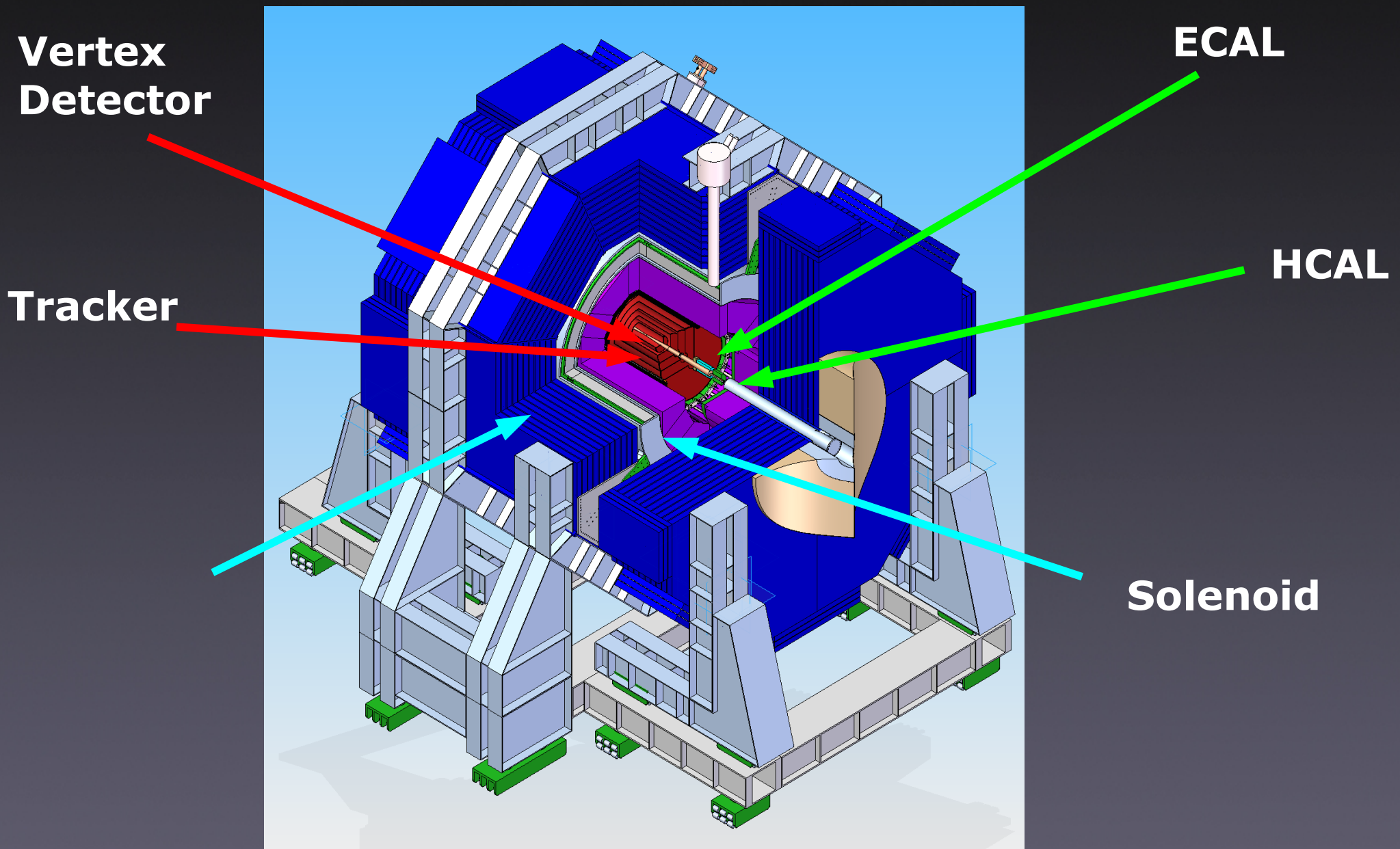


$\tau^+ \rightarrow \rho^+ \nu$  ( $\pi^+ \pi^0 \nu$ )

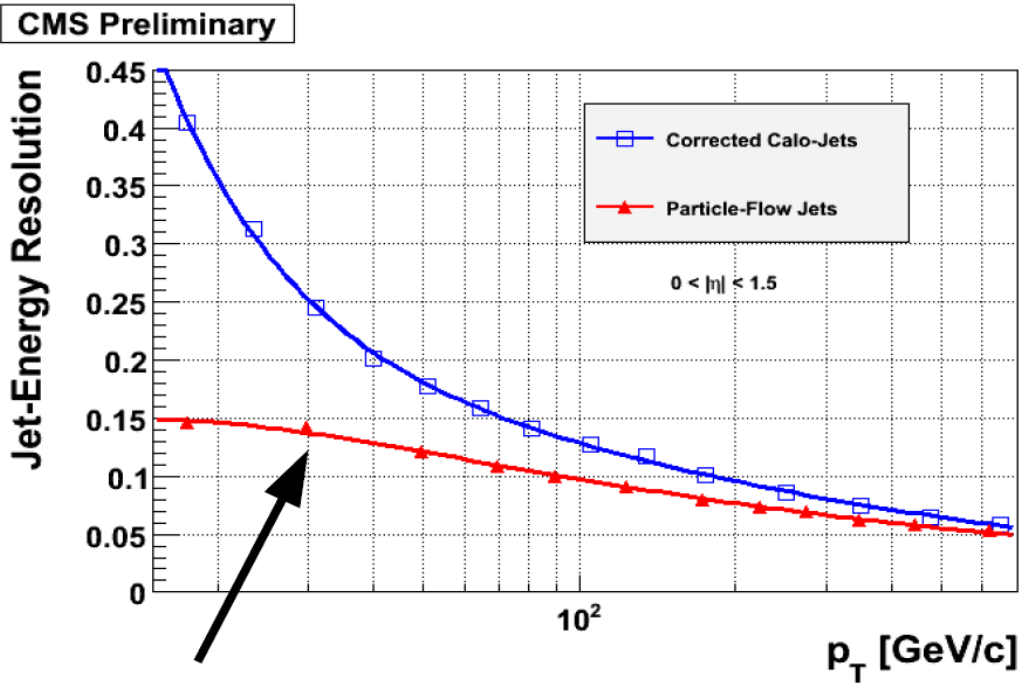


**Calorimeter Aided Tracking**  
 **$V^0$  finder**

# A PFA Detector

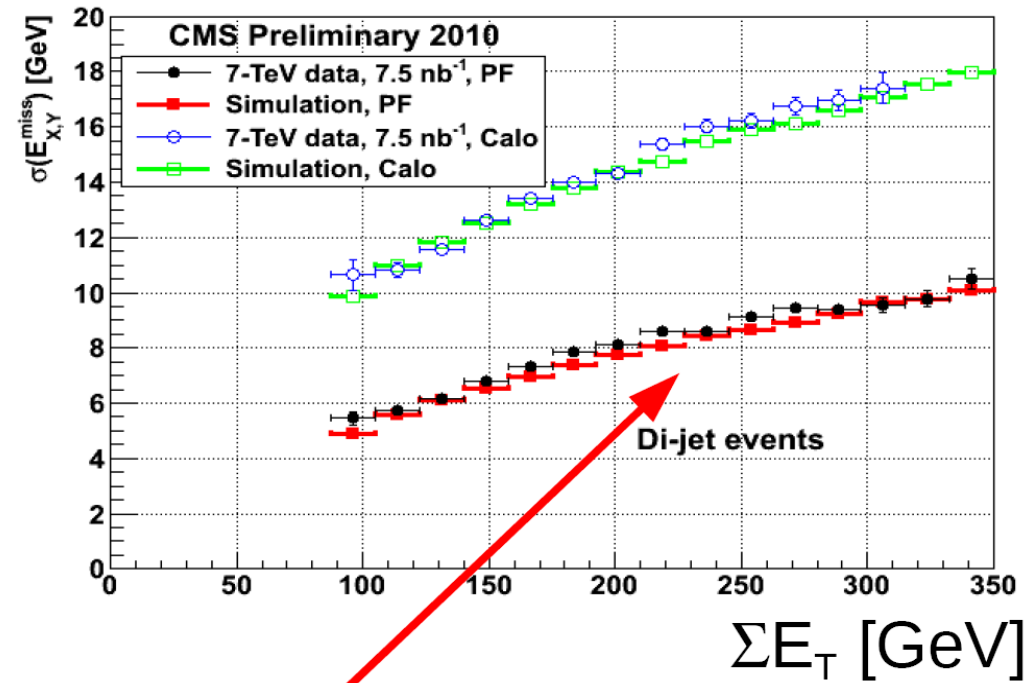


# PFA at CMS



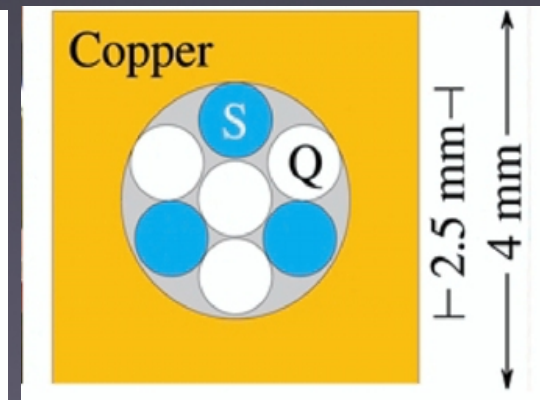
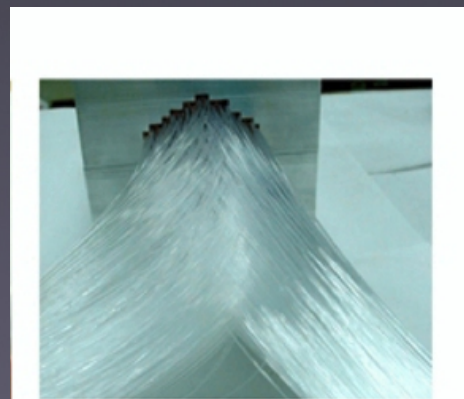
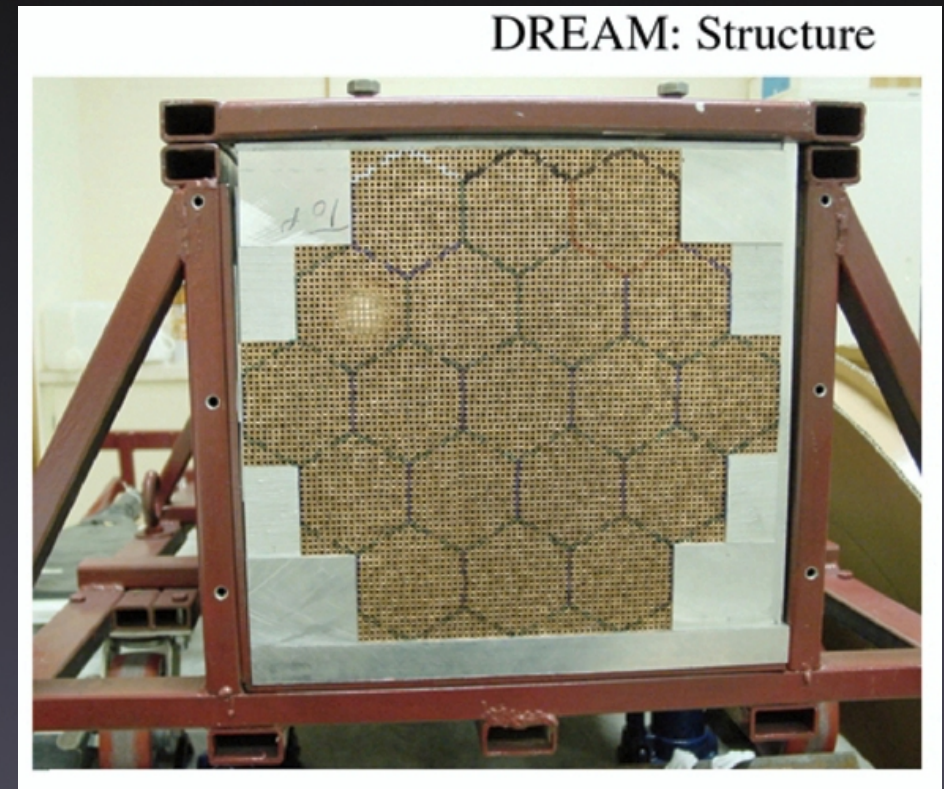
Jet energy resolution  
Simulated QCD-multijet events in the  
CMS barrel

Missing  $E_T$  resolution for Di-jet events



# Dual-Readout Calorimetry

- As already mentioned
  - Two components in hadronic showers
- Dual Readout Idea
  - Two active media
  - Scintillating Fibers measure visible energy
  - Quartz Fibers measure Cerenkov light from em component
- Implemented in the DREAM calorimeter



# Dual Readout in Detail

- Scintillation signal (S) and Cerenkov signal:

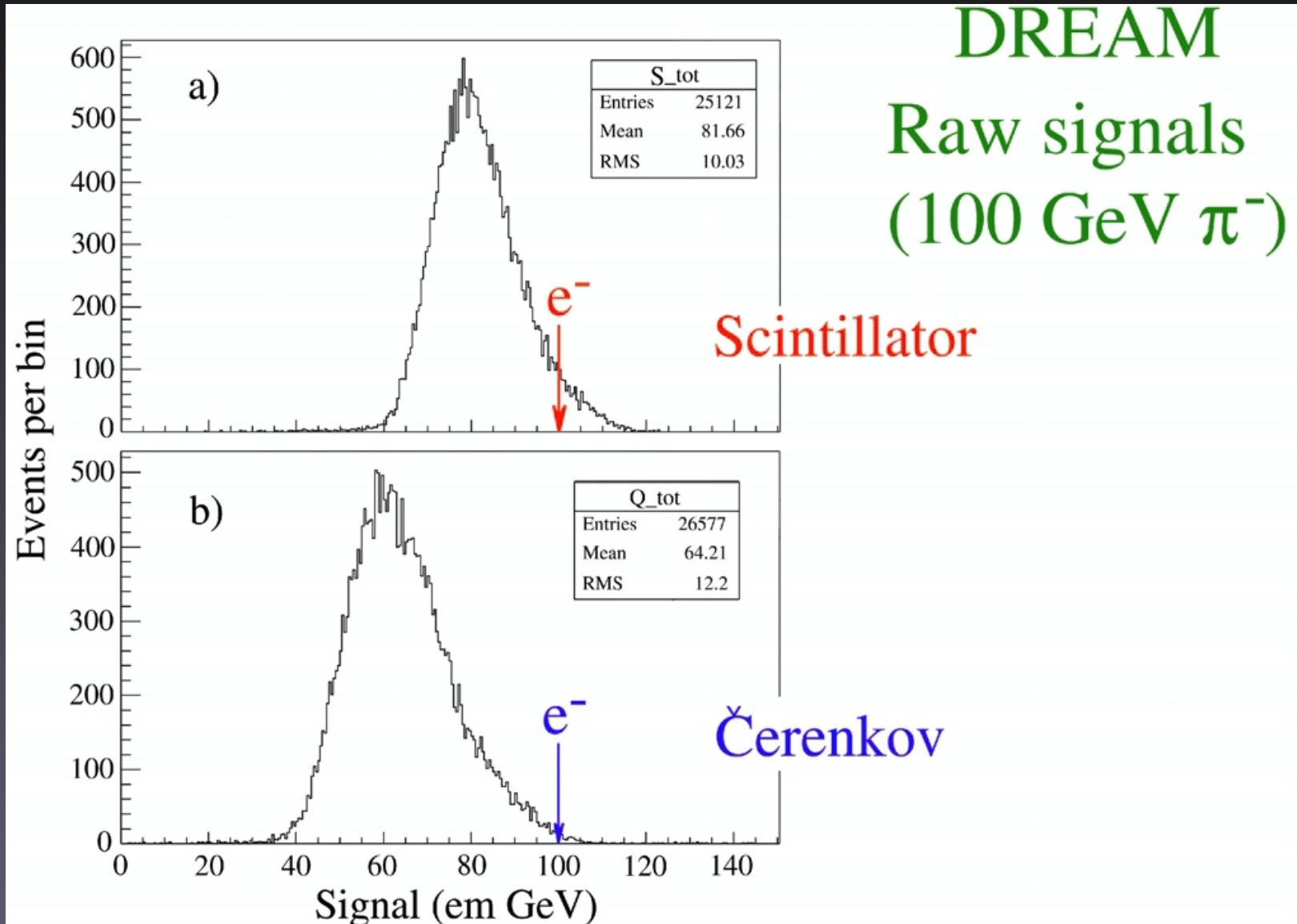
$$Q = E(f_{em} + h/e_Q(1 - f_{em}))$$
$$S = E(f_{em} + h/e_S(1 - f_{em}))$$

- This can be written as

$$E = \frac{RS - Q}{R - 1}$$
$$R = \frac{1 - h/e_Q}{1 - h/e_S}$$

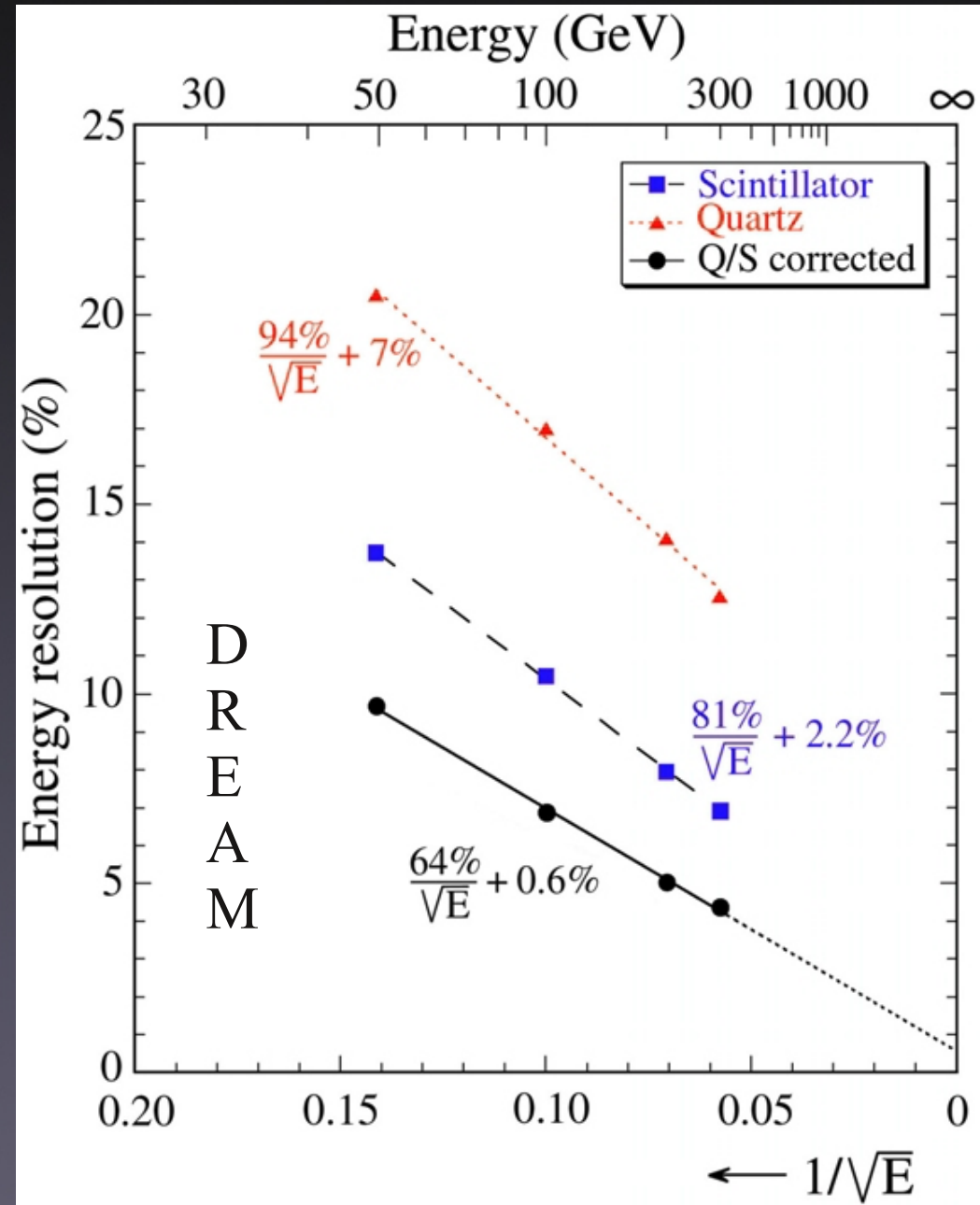
- R will be taken from calibrations

# Some plots



# Energy Resolution

- DREAM prototype
  - Achieves linear hadronic response
  - Dual readout demonstration
- Limitations
  - Size of prototype (leakage)
  - Light yield
  - Fluctuations in visible energy
- Principle can be applied to other calorimeters with optical readout





# Summary

- Calorimeters are not black magic
  - Hope you got an idea, how they work
- Lots of things I couldn't cover
  - Material for several lectures
- Calorimeter R&D is an active field
  - CALICE, DREAM ...
- Recommended Literature
  - R. Wigmans : Calorimetry
  - Review of Particle Physics 2009
  - T. Virdee : Experimental Techniques