Precision Experiments / Data Analysis (I)

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School on Amplitude Analysis in Modern Physics: from hadron spectroscopy to CP phases

2[nd] August 2011

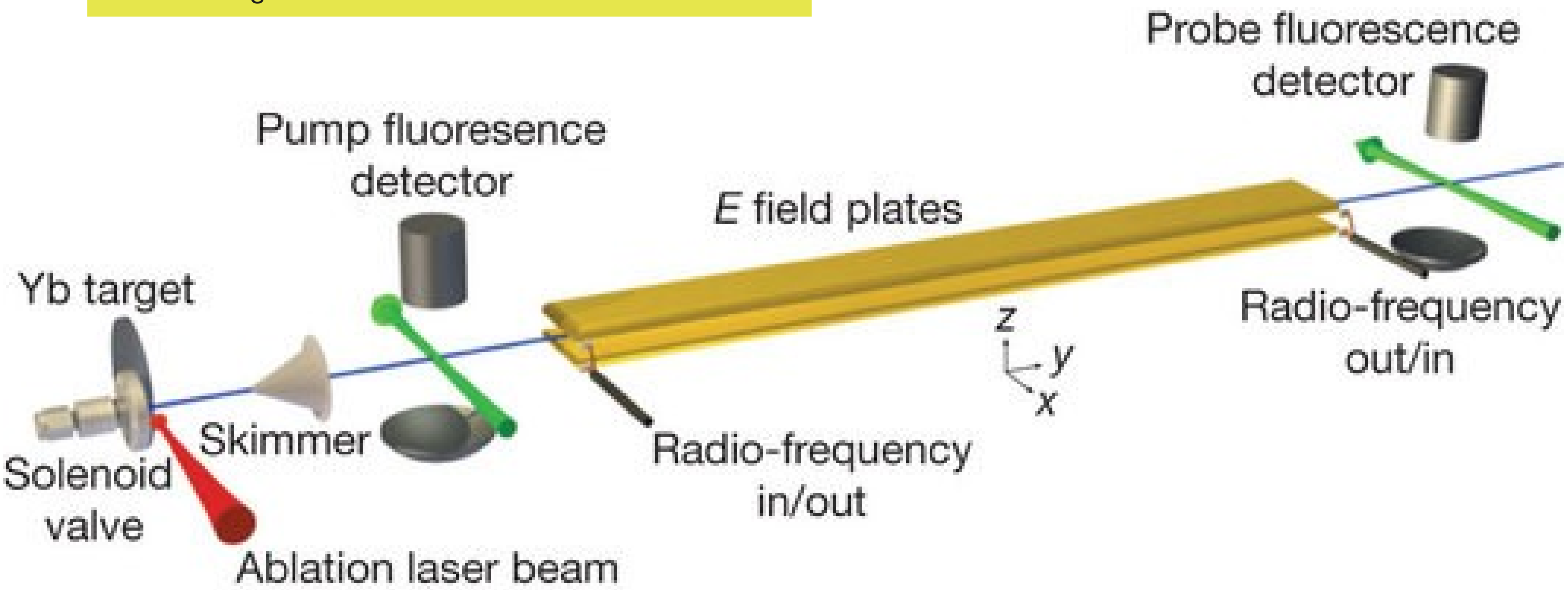
Slides available from
http://www2.warwick.ac.uk/fac/sci/physics/staff/academic/gershon/talks

“Precision Experiments”

- I will focus on methods to search for CP violation beyond the Standard Model
  - Hadronic decays of heavy flavours (mainly D, B)
- Experiments in this field are now reaching a “precision” era
  - Past: E791, FOCUS, CLEO, BESII, BaBar, Belle, ...
  - Current: CDF, D0, BESIII, LHCb
  - Future: Belle2, LHCb upgrade, SuperB
- “Precision” is relative – there are many higher precision experiments (at lower energies)
  - Studies of η, η', K, ω, etc.

How precise?

$|d_e| < 10.5 \times 10^{-28}$ e cm



Improved measurement of the shape of the electron
Nature 473, pp. 493–496 (26 May 2011)

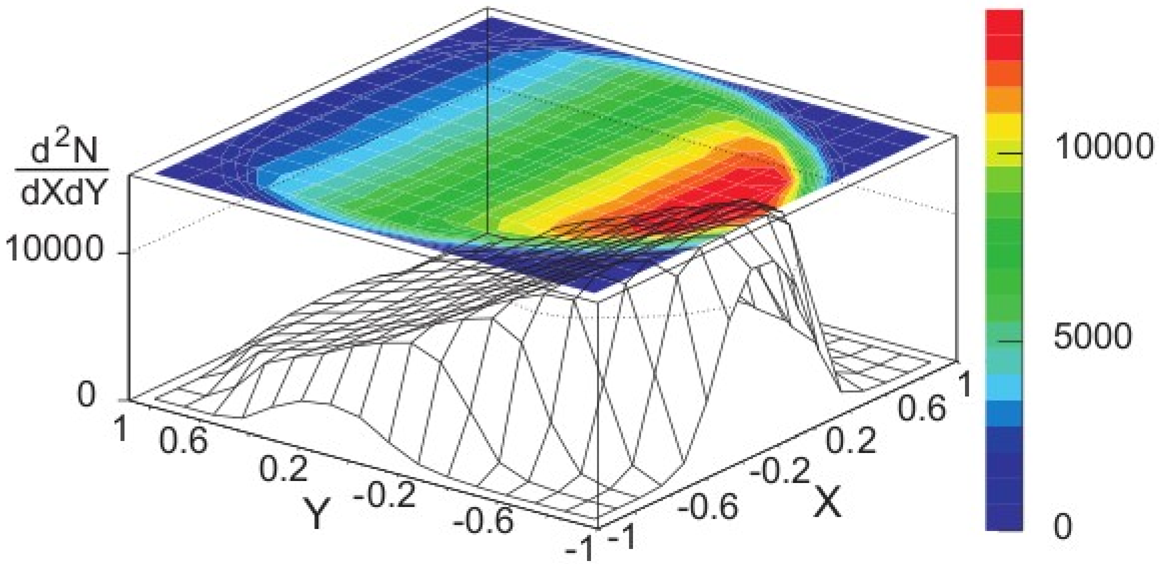
How precise?

$\eta \to \pi^+ \pi^- \pi^0$

1.34 10^6 decays

$$X = \sqrt{3}\,\frac{E_+ - E_-}{Q} = \frac{\sqrt{3}}{2m_\eta Q}(u-t)$$

$$Y = 3\,\frac{E_0 - m_0}{Q} - 1 = \frac{3}{2m_\eta Q}\left((m_\eta - m_{\pi^0})^2 - s\right) - 1$$



(E_+, E_-, E_0) are pion energies in η rest frame

(s, t, u) are Mandelstam variables

$$A_{LR} = (+0.09 \pm 0.10\ {}^{+0.09}_{-0.14}) \times 10^{-2}$$

KLOE collaboration, JHEP 0805:006,2008

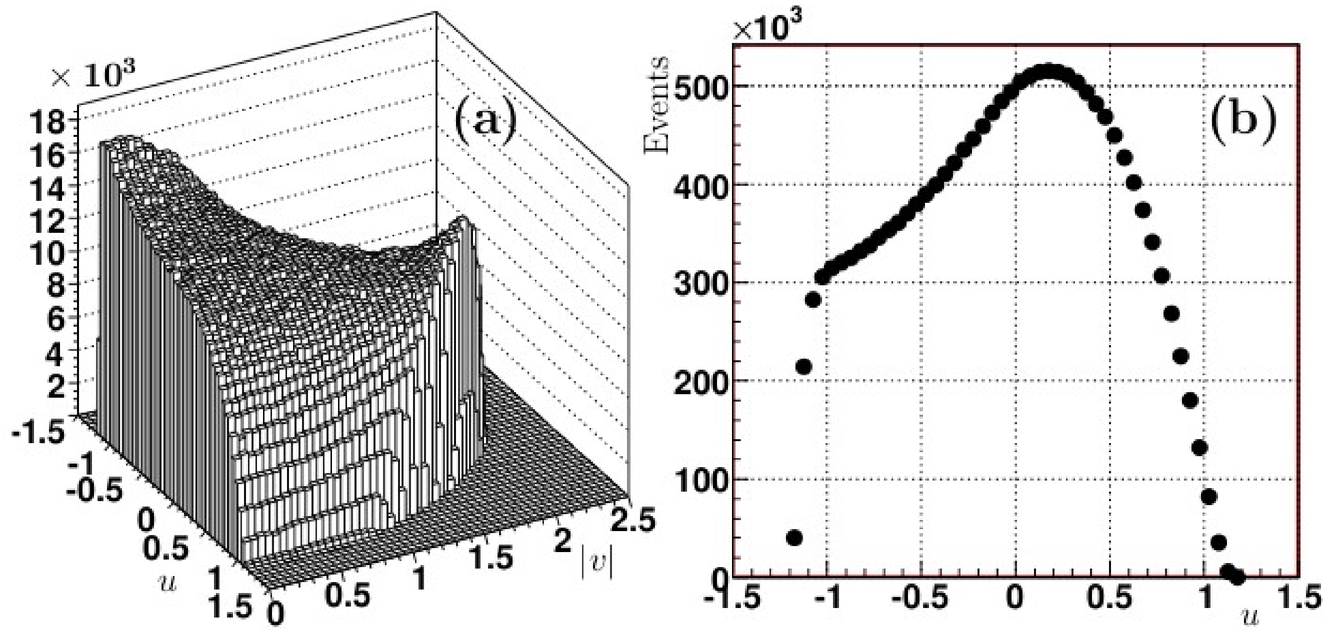
How precise?

$K^{\pm} \to \pi^{\pm}\pi^{+}\pi^{-}$

$$|M(u,v)|^2 \sim 1 + gu + hu^2 + kv^2,$$

$$u = \frac{s_3 - s_0}{m_\pi^2}, \quad v = \frac{s_2 - s_1}{m_\pi^2}, \quad s_i = (P_K - P_i)^2, \; i = 1,2,3; \quad s_0 = \frac{s_1 + s_2 + s_3}{3}.$$

3.8 10^9 decays

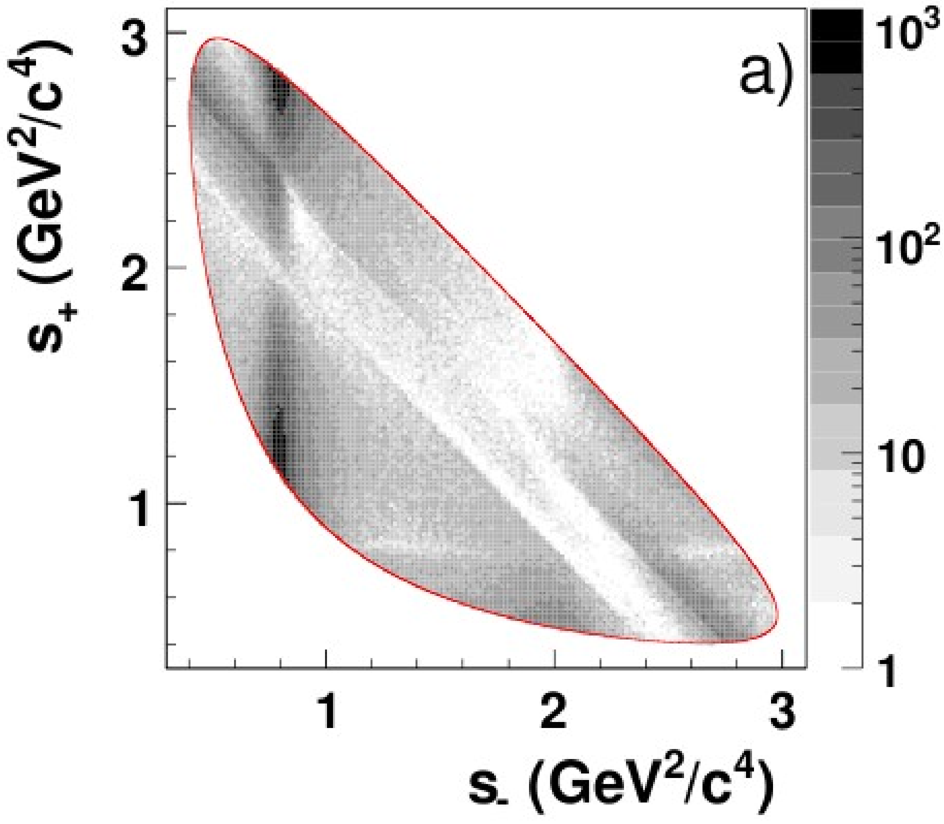


$$A_g^c = (-1.5 \pm 1.5_{stat.} \pm 0.9_{trig.} \pm 1.3_{syst.}) \times 10^{-4} = (-1.5 \pm 2.2) \times 10^{-4}.$$

NA48/2 Collaboration, Eur.Phys.J.C52:875-891,2007

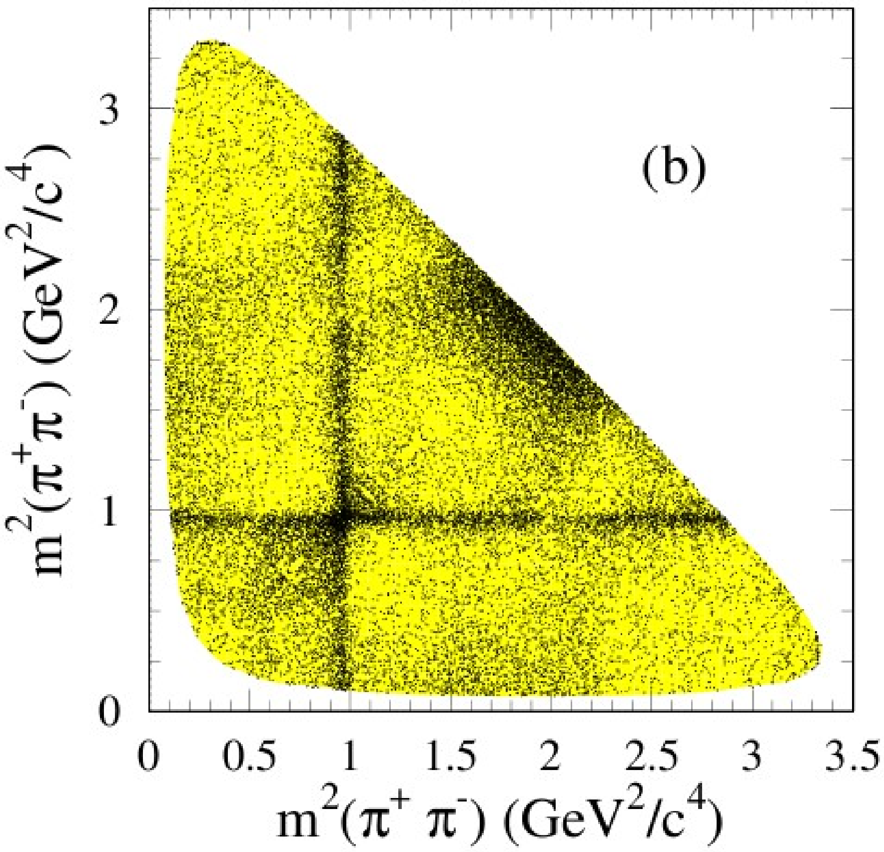
How precise?

$D^0 \rightarrow K_s\pi^+\pi^-$
BaBar PRL 105 (2010) 081803



744 000 candidates

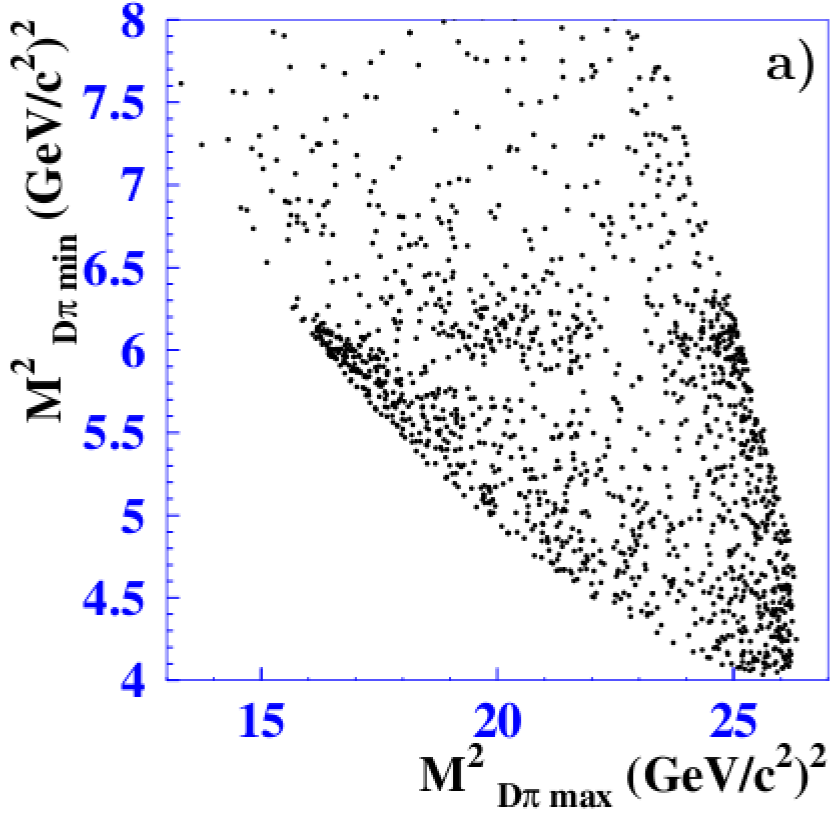
$D_s^+ \rightarrow \pi^+\pi^-\pi^+$
BaBar PRD 79 (2009) 032003



13 000 candidates

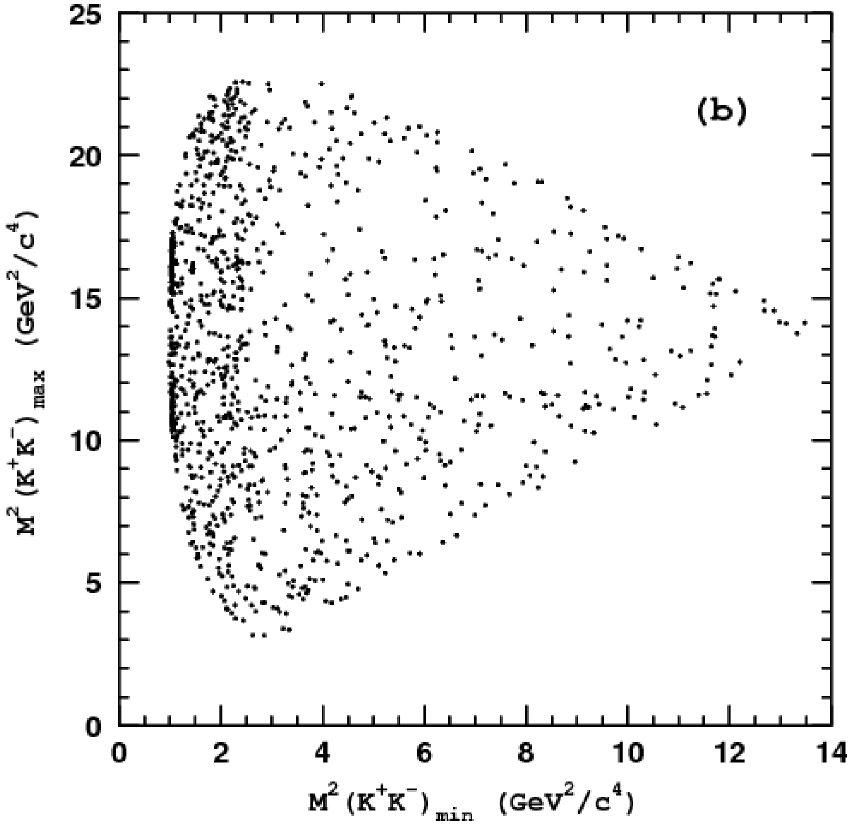
How precise?

$B^+ \rightarrow D^-\pi^+\pi^+$
Belle PRD 69 (2004) 112002



1100 candidates

$B^+ \rightarrow K^+K^+K^-$
Belle PRD 71 (2005) 092003



1100 candidates

Content of the lectures

- Why do we believe that multibody hadronic decays of heavy flavours may provide a good laboratory to search for new sources of CP violation?
- Which decays in particular should we look at?
- What methods can we use to study them?
- What are the difficulties we encounter when trying to do the analysis?

Content of the lectures

- Why do we believe that multibody hadronic decays of heavy flavours may provide a good laboratory to search for new sources of CP violation?

… see also Thomas Mannel's lectures

- Which decays in particular should we look at?

… see also Thomas Mannel's lectures

- What methods can we use to study them?

… see also Klaus Peters' lectures

- What are the difficulties we encounter when trying to do the analysis?

… main content of these lectures

Why do we believe that multibody hadronic decays of heavy flavours may provide a good laboratory to search for new sources of CP violation?

Heavy flavours & CP violation

- Studies of heavy flavours are ideal to study CP violation phenomena, since
  - In the SM, CP violation occurs only in flavour-changing weak interactions (the CKM matrix)
  - In several theories extending the SM, this remains true (to varying degrees) – weak interactions are a good place to look for new sources of CP violation
  - “New physics” can show up as deviations from precise CKM-based predictions, null or otherwise
- Aim is to make multiple, redundant measurements of the 4 independent parameters that define the CKM matrix and to find inconsistencies

The Cabibbo-Kobayashi-Maskawa Quark Mixing Matrix

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

A 3x3 unitary matrix

Described by 4 real parameters – allows CP violation

PDG (Chau-Keung) parametrisation: θ_{12}, θ_{23}, θ_{13}, δ

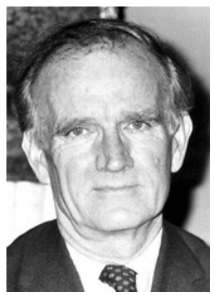
Wolfenstein parametrisation: λ, A, ρ, η

Highly predictive

Flavour oscillations, CP violation and Nobel Prizes

1964 – Discovery of CP violation in K^0 system

1980 – Nobel Prize to Cronin and Fitch



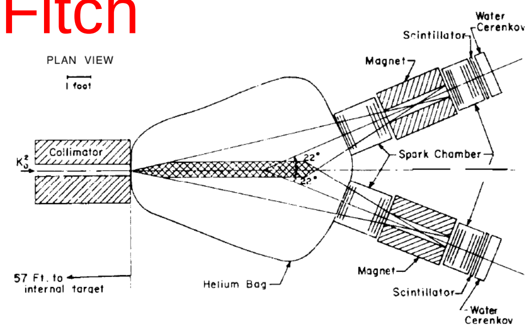


Fig. 1. Plan view of the apparatus as located at the A. G. S.

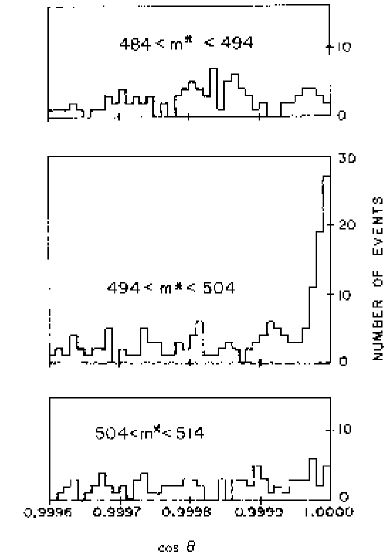


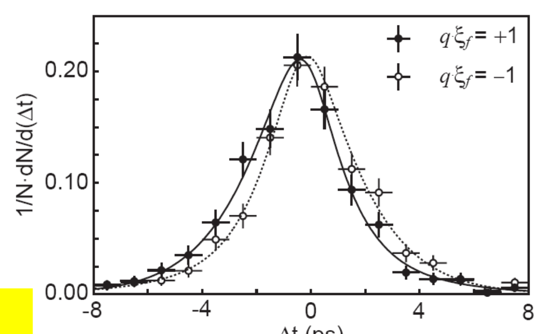
FIG. 3. Angular distribution in three mass ranges for events with cosθ > 0.9995.

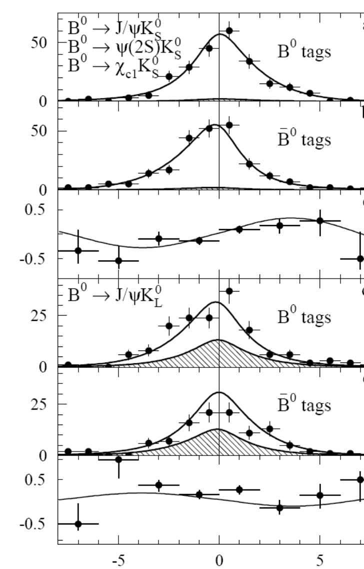
PRL 13 (1964) 138

2001 – Discovery of CP violation in B_d system

2008 – Nobel Prize to Kobayashi and Maskawa

Prog.Theor.Phys. 49 (1973) 652





Belle PRL 87 (2001) 091802

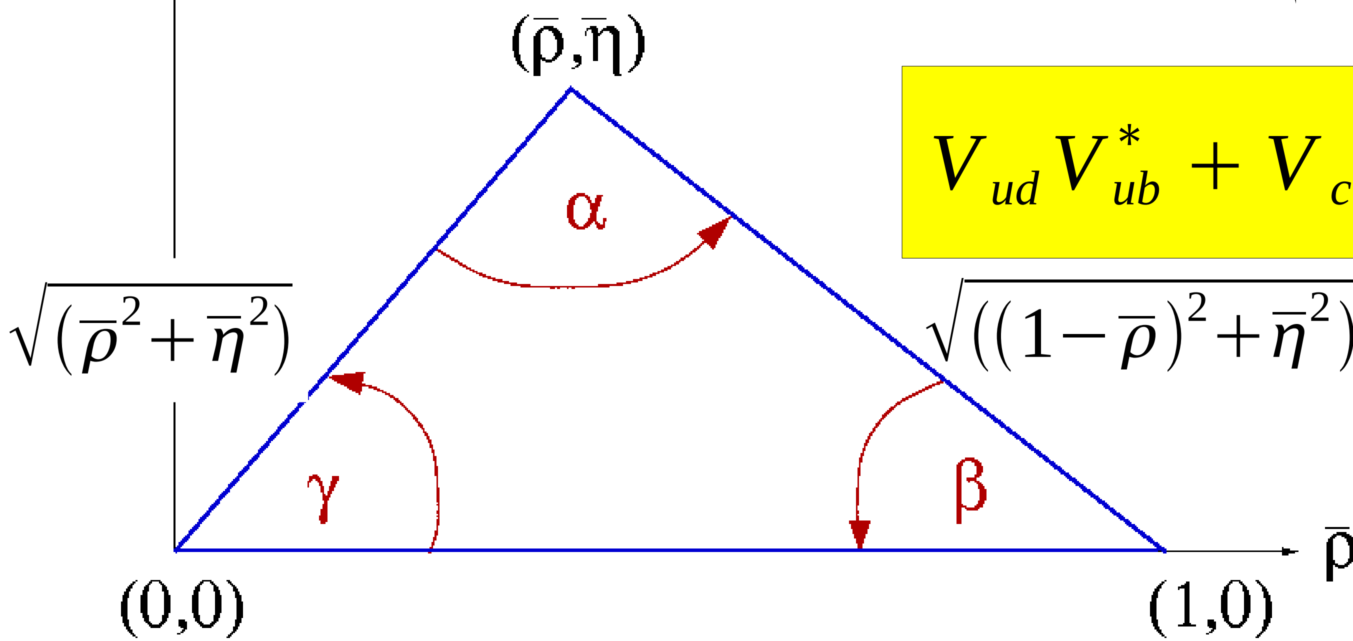
BABAR PRL 87 (2001) 091801

The Cabibbo-Kobayashi-Maskawa Matrix & The Unitarity Triangle

Quark couplings to W boson described by 3x3 unitary matrix (4 free parameters, inc. 1 phase)

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$$V_{ud}V_{ub}^{*} + V_{cd}V_{cb}^{*} + V_{td}V_{tb}^{*} = 0$$



$$\alpha \equiv \phi_2 = \arg\left[-\frac{V_{td}V_{tb}^{*}}{V_{ud}V_{ub}^{*}}\right], \quad \beta \equiv \phi_1 = \arg\left[-\frac{V_{cd}V_{cb}^{*}}{V_{td}V_{tb}^{*}}\right], \quad \gamma \equiv \phi_3 = \arg\left[-\frac{V_{ud}V_{ub}^{*}}{V_{cd}V_{cb}^{*}}\right]$$

Global fit status at EPS2011

Update from CKMfitter collaboration (talk by V. Niess)

http://indico.in2p3.fr/materialDisplay.py?contribId=392&sessionId=2&materialId=slides&confId=5116

Global Fit of the UT

Observables

$|V_{ud}|, |V_{us}|$

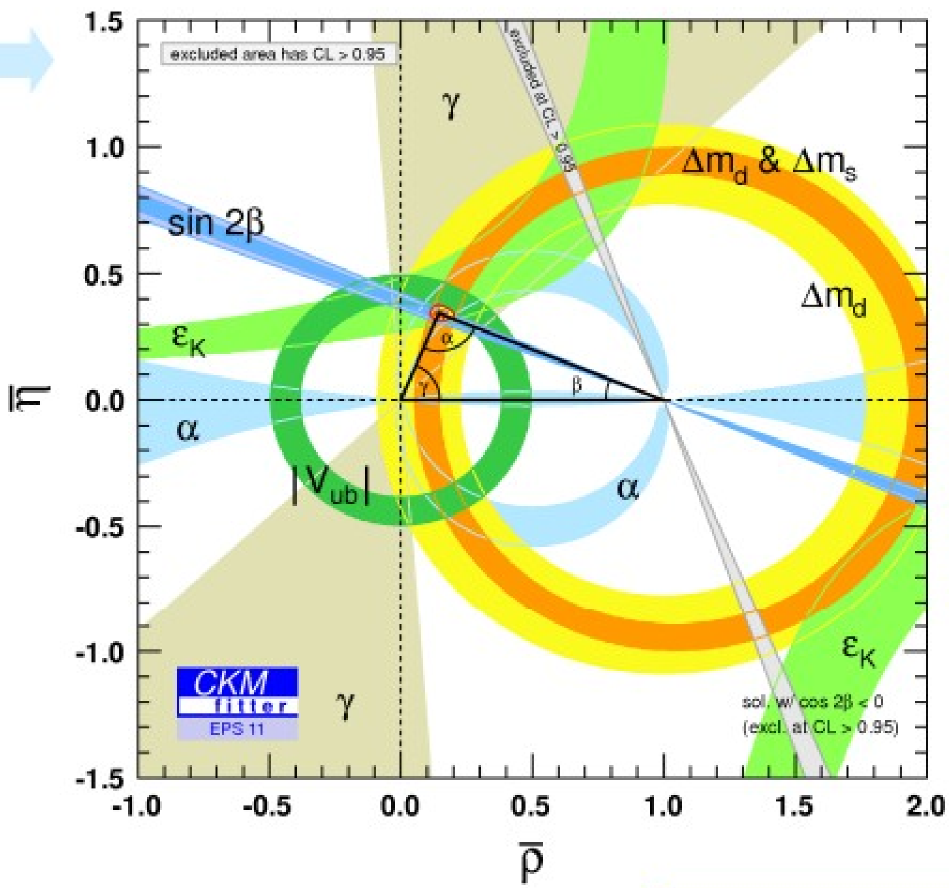
$|V_{cb}|, |V_{ub}|$

$\mathcal{B}[B \to \tau\nu]$

$\Delta m_d, \Delta m_s$

$|\varepsilon_K|$

$\alpha, \sin(2\beta_{cc}), \gamma$



Fit of UT apex is dominated by $\sin(2\beta)$, $\Delta m_d/\Delta m_s$ and α. Excellent agreement between these 3 inputs.

Overall consistent picture

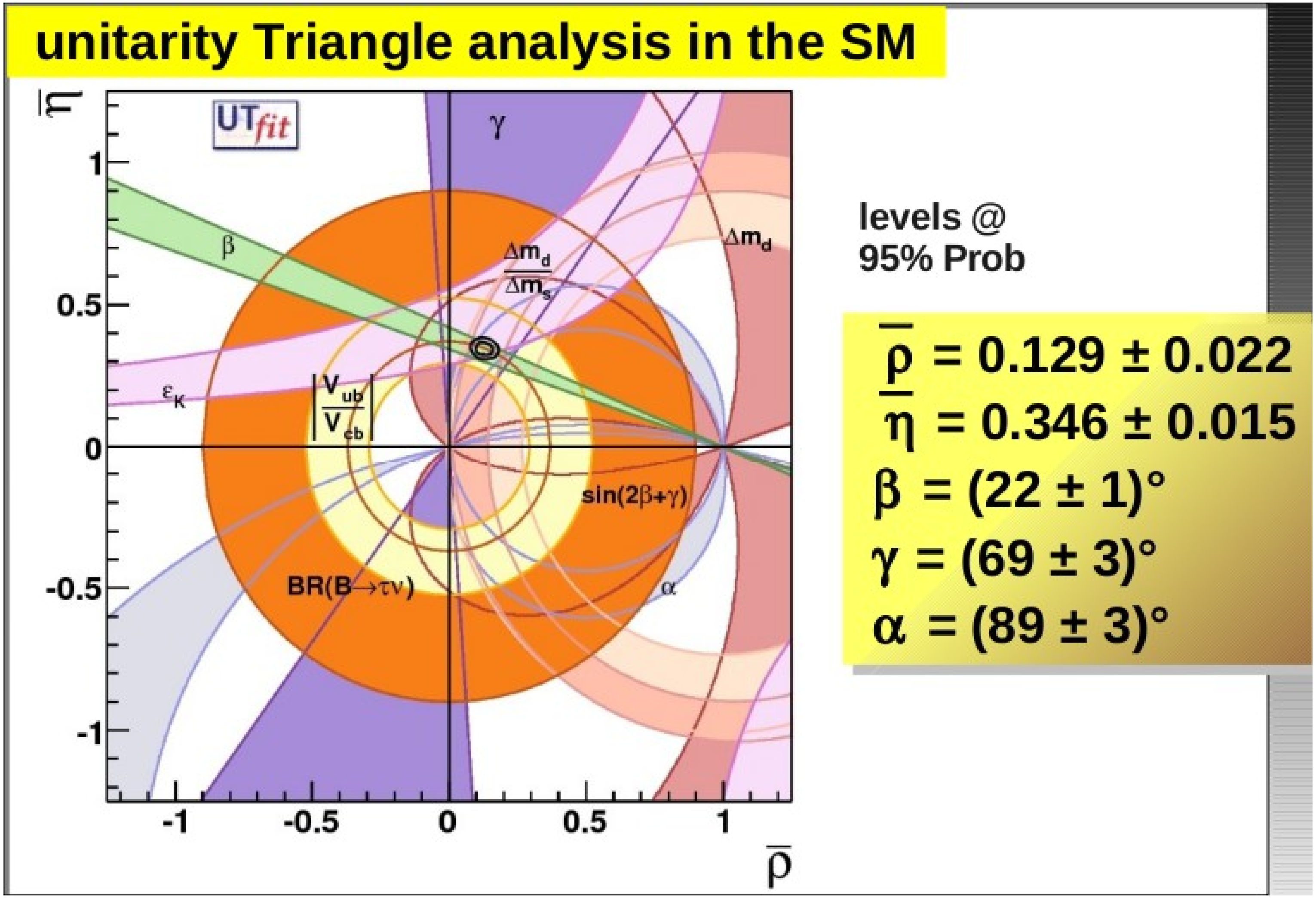
The KM mechanism is the dominant source of CP in B's

$\bar{\rho} = 0.144^{+0.027}_{-0.018}, \quad \bar{\eta} = 0.343^{+0.014}_{-0.014}$

(1 σ interval)

Global fit status at EPS2011

Update from UTfit collaboration (talk by M. Bona)
http://indico.in2p3.fr/materialDisplay.py?contribId=424&sessionId=2&materialId=slides&confId=5116



CKM Matrix – Phases

P.Harrison *et al.*,
PLB 680 (2009) 328

Can form a matrix of angles between pairs of CKM matrix elements

Φ_{ij} = phase between remaining elements when row i and column j removed

unitarity implies sum of phases in any row or column = 180°

$$\Phi = \begin{array}{c} \\ u \\ c \\ t \end{array} \begin{array}{c} \begin{array}{ccc} d & s & b \end{array} \\ \begin{pmatrix} \Phi_{ud} & \Phi_{us} & \Phi_{ub} \\ \Phi_{cd} & \Phi_{cs} & \Phi_{cb} \\ \Phi_{td} & \Phi_{ts} & \Phi_{tb} \end{pmatrix} \end{array} \simeq \begin{array}{c} \\ u \\ c \\ t \end{array} \begin{array}{c} \begin{array}{ccc} d & s & b \end{array} \\ \begin{pmatrix} 1^o & 22^o & 157^o \\ 67^o & 90^o & 23^o \\ 112^o & 68^o & 0^o \end{pmatrix} \end{array}$$

$\beta \equiv \varphi_1$

$\alpha \equiv \varphi_2$

$\gamma \equiv \varphi_3$

"The Unitarity Triangle"

OK, but why do we believe that *multibody* hadronic decays of heavy flavours may provide a good laboratory to search for new sources of CP violation?

Direct CP violation in B → Kπ

- Direct CP violation in B → Kπ sensitive to γ

too many hadronic parameters ⇒ need theory input

NB. interesting deviation from naïve expectation

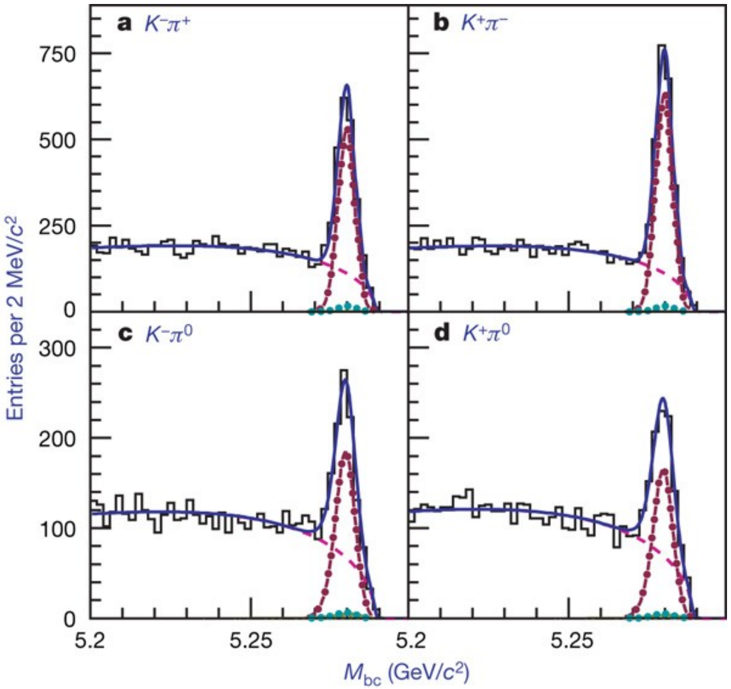
"Kπ puzzle"

$$A_{CP}(K^-\pi^+) = (-9.8^{+1.2}_{-1.1})\% \quad A_{CP}(K^-\pi^0) = (5.0 \pm 2.5)\%$$
$$\Delta(A_{CP}) = (-14.8 \pm 2.8)\%$$

HFAG averages
BABAR PRD 76 (2007) 091102 & arXiv:0807.4226; also CDF

and now LHCb!
(results not in average yet)

Belle Nature 452 (2008) 332



Could be a sign of new physics …
… but need to rule out possibility of larger than expected QCD corrections

Latest results (EPS2011) on B→Kπ

Updated Belle results (talk of P. Chang)

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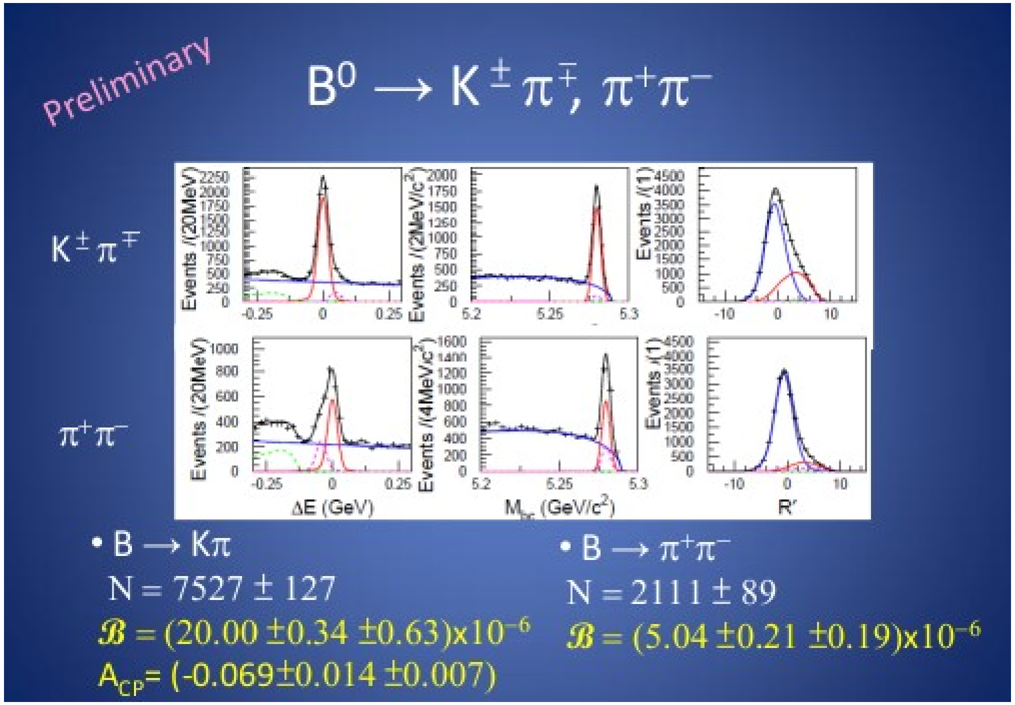

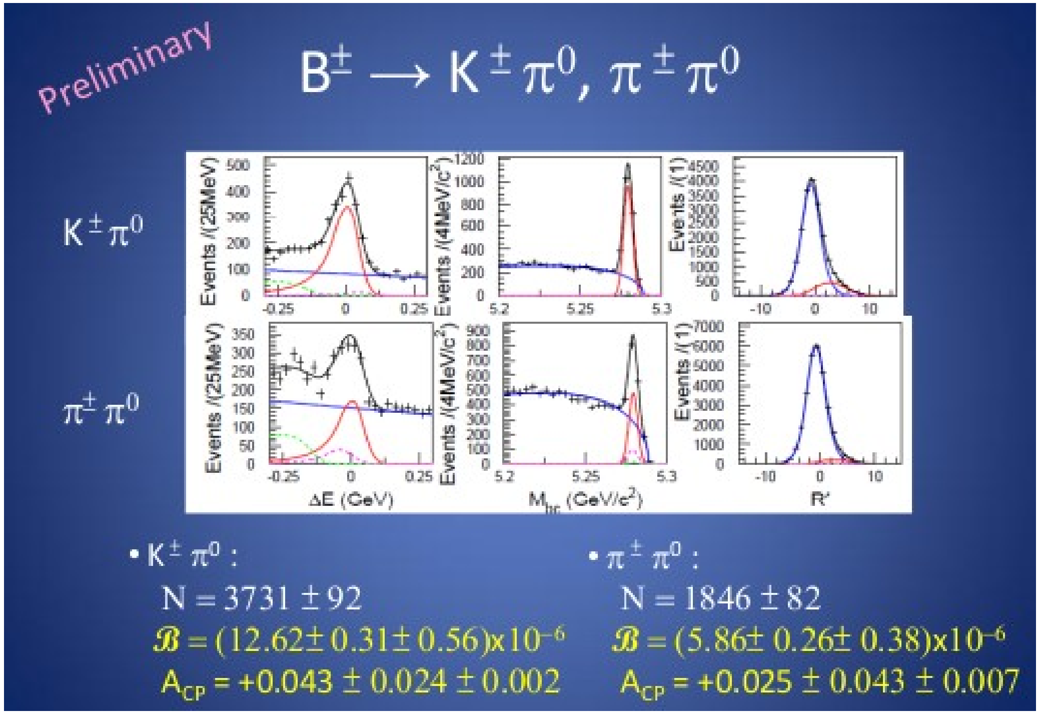

Latest results (EPS2011) on B→Kπ

Updated LHCb results (talk of A. Carbone)

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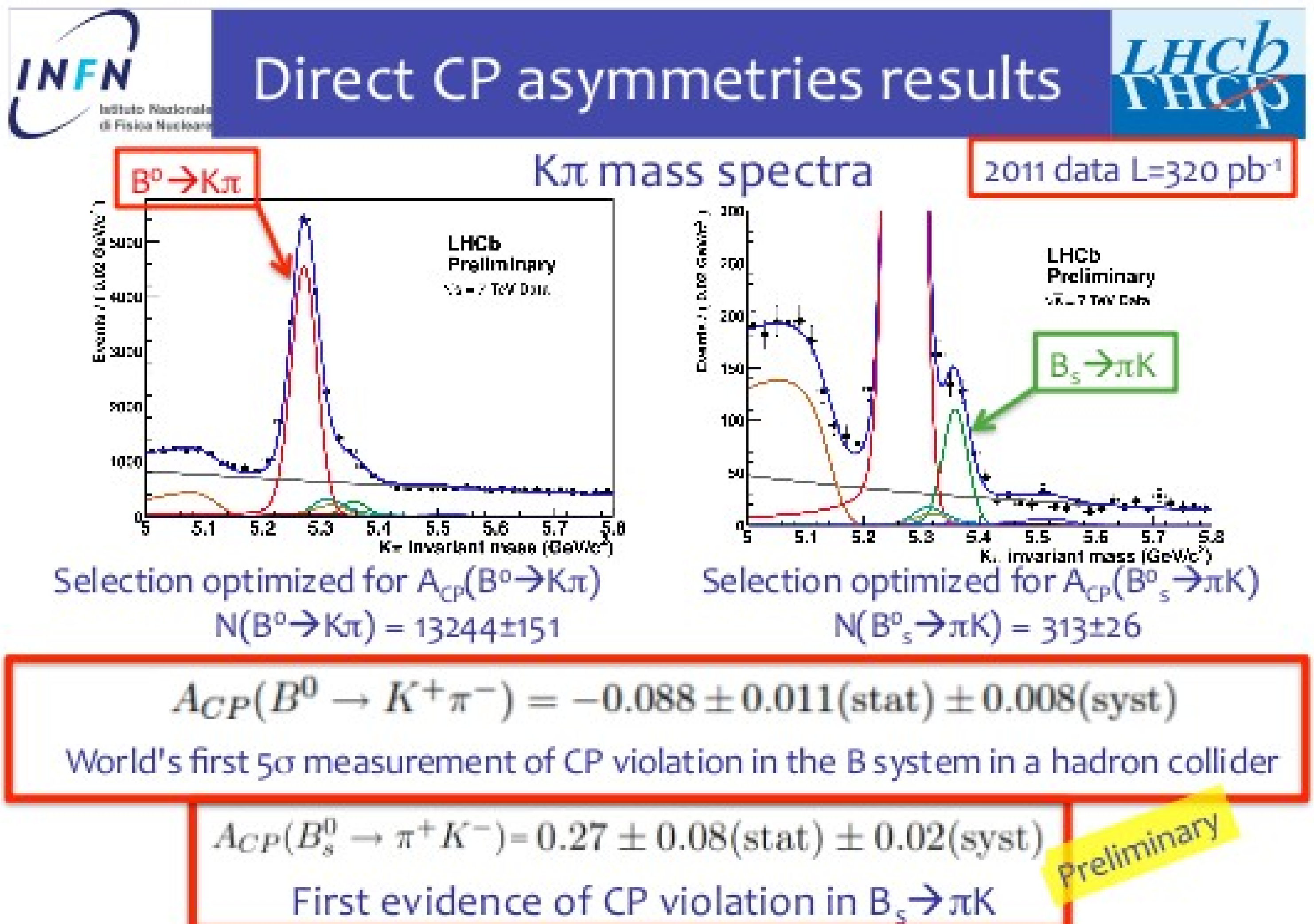


We have excellent data, in clear disagreement with “the naïve Standard Model prediction” on $B \to K\pi$ …

... but can't be sure that corrections to the SM prediction aren't larger than expected …

… need methods that provide more observables to help control uncertainties

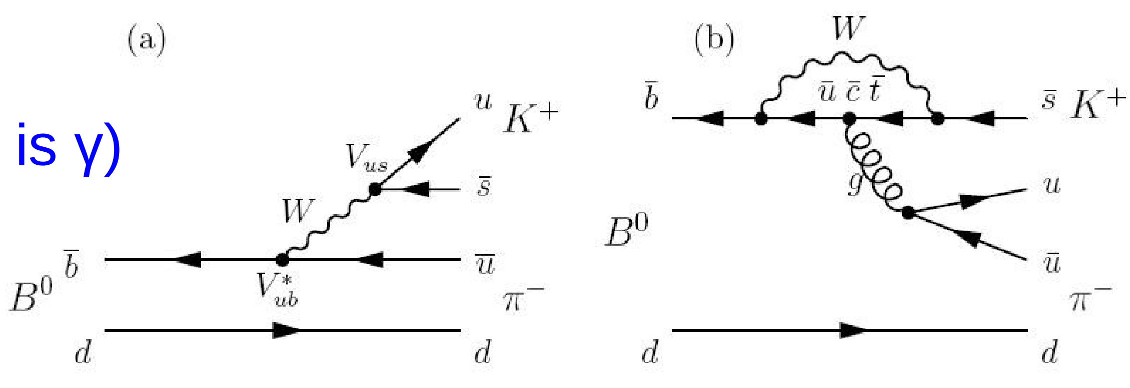
Why are we so interested in Dalitz plots?

- Condition for DCPV: $|\bar{A}/A| \neq 1$
- Need $\bar{A}$ and A to consist of (at least) two parts
  - with different weak (φ) and strong (δ) phases
- Often realised by “tree” and “penguin” diagrams

$$A = |T| e^{i(\delta_T - \phi_T)} + |P| e^{i(\delta_P - \phi_P)} \qquad \bar{A} = |T| e^{i(\delta_T + \phi_T)} + |P| e^{i(\delta_P + \phi_P)}$$

$$A_{CP} = \frac{|\bar{A}|^2 - |A|^2}{|\bar{A}|^2 + |A|^2} = \frac{2\,|T||P| \sin(\delta_T - \delta_P) \sin(\phi_T - \phi_P)}{|T|^2 + |P|^2 + 2\,|T||P| \cos(\delta_T - \delta_P) \cos(\phi_T - \phi_P)}$$

Example: B→Kπ
(weak phase difference is γ)



Feynman tree (a) and penguin (b) diagrams for the $B^0_d \to K^+\pi^-$ decay

Why are we so interested in Dalitz plots?

- Condition for DCPV: $|\bar{A}/A| \neq 1$

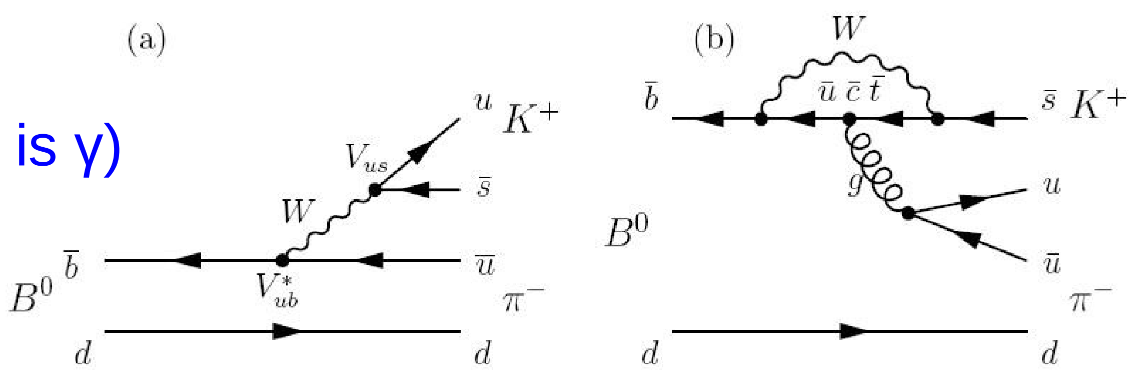
Problem with two-body decays:

- 2 observables (B, A_{CP})
- 4 unknowns ($|T|$, $|P|$, $\delta_T - \delta_P$, $\varphi_T - \varphi_P$)

$$A_{CP} = \frac{|\bar{A}|^2 - |A|^2}{|\bar{A}|^2 + |A|^2} = \frac{2\,|T||P|\sin(\delta_T - \delta_P)\sin(\phi_T - \phi_P)}{|T|^2 + |P|^2 + 2\,|T||P|\cos(\delta_T - \delta_P)\cos(\phi_T - \phi_P)}$$

Example: B→Kπ

(weak phase difference is γ)



Feynman tree (a) and penguin (b) diagrams for the $B^0_d \to K^+\pi^-$ decay

What Is a Dalitz Plot?

- Visual representation of
  - the phase-space of a three-body decay
    - involving only spin-0 particles
    - (term often abused to refer to phase-space of any multibody decay)
  - Named after it's inventor, Richard Dalitz (1925–2006):
  - “On the analysis of tau-meson data and the nature of the tau-meson.”
    - R.H. Dalitz, Phil. Mag. 44 (1953) 1068
    - (historical reminder: tau meson = charged kaon)
  - For scientific obituary, see
    - I.J.R. Aitchison, F.E. Close, A. Gal, D.J. Millener,
    - Nucl.Phys.A771:8-25,2006

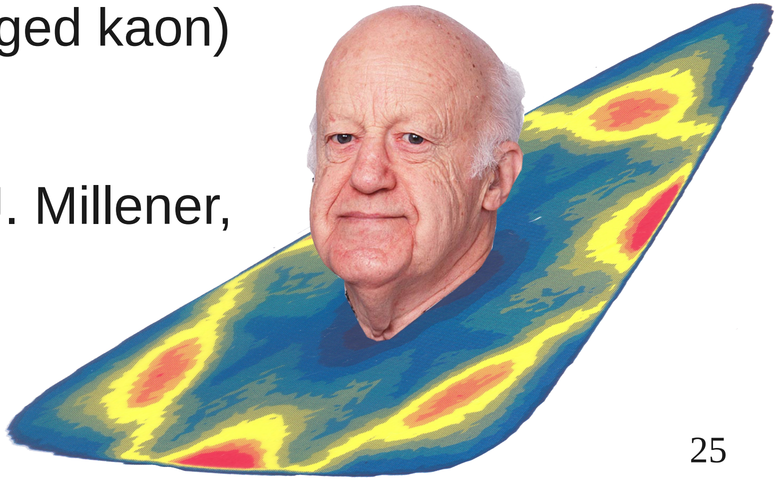
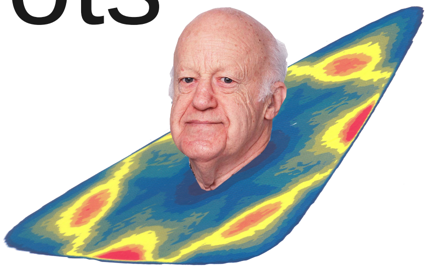


Image credit: Mike Pennington

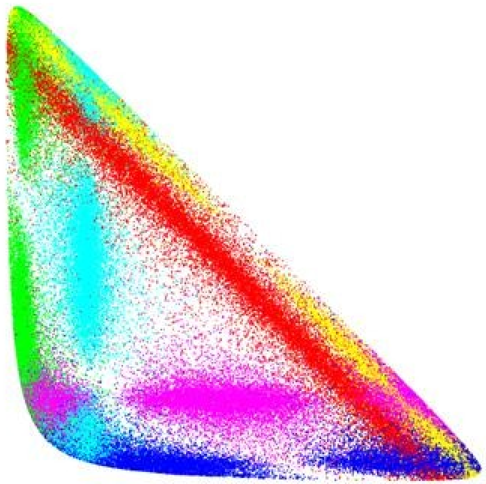
Dalitz plot analysis

- Amplitude analysis to extract directly information related to the phase at each Dalitz plot position
- Most commonly performed in the "isobar model"
  - sum of interfering resonances
  - each described by Breit-Wigner (or similar) lineshapes, spin terms, etc.
  - fit can be unbinned, but has inherent model dependence
- Alternative approaches aiming to avoid model dependence usually involve binning

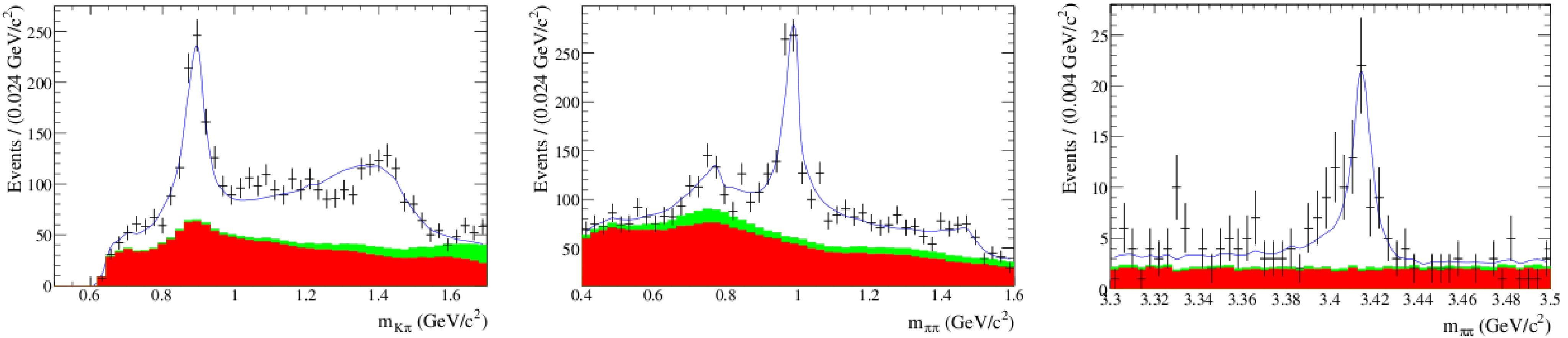
Pros and cons of Dalitz plots



- Pros
  - More observables (B & A_{CP} at each Dalitz plot point)
  - Using isobar formalism, can express total amplitude as coherent sum of quasi-two-body contributions
    $$A(m_{12}^2, m_{23}^2) = \sum_r c_r F_r(m_{12}^2, m_{23}^2)$$
    - where c_r & F_r contain the weak and strong physics, respectively
    - n.b. each c_r is itself a sum of contributions from tree, penguin, etc.
  - Interference provides additional sensitivity to CP violation
- Cons
  - Need to understand hadronic (F_r) factors
    - lineshapes, angular terms, barrier factors, ...
  - Isobar formalism only an approximation
  - Model dependence



$B^+ \to K^+\pi^+\pi^-$



BaBar PRD 78 (2008) 012004
See also Belle PRL 96 (2006) 251803

Model includes:

- $K^{*0}(892)\pi+$, $K_2^{*0}(1430)\pi^+$
- $(K\pi)_0^*\pi^+$ (LASS lineshape)
- $\rho^0(770)K^+$, $\omega(782)K^+$, $f_0(980)K^+$, $f_2(1270)K^+$, $\chi_{c0}K^+$
- $f_X(1300)K^+$, phase-space nonresonant

$B^+ \to K^+\pi^+\pi^-$

TABLE II: Summary of measurements of branching fractions (averaged over charge conjugate states) and CP asymmetries. Note that these results are not corrected for secondary branching fractions. The first uncertainty is statistical, the second is systematic, and the third represents the model dependence. The final column is the statistical significance of direct CP violation determined as described in the text.

Mode	Fit fraction (%)	$\mathcal{B}(B^+ \to \text{Mode})(10^{-6})$	A_{CP} (%)	DCPV sig.
$K^+\pi^-\pi^+$ total		$54.4 \pm 1.1 \pm 4.5 \pm 0.7$	$2.8 \pm 2.0 \pm 2.0 \pm 1.2$	
$K^{*0}(892)\pi^+$; $K^{*0}(892) \to K^+\pi^-$	$13.3 \pm 0.7 \pm 0.7\,^{+0.4}_{-0.9}$	$7.2 \pm 0.4 \pm 0.7\,^{+0.3}_{-0.5}$	$+3.2 \pm 5.2 \pm 1.1\,^{+1.2}_{-0.7}$	0.9σ
$(K\pi)^{*0}_0\pi^+$; $(K\pi)^{*0}_0 \to K^+\pi^-$	$45.0 \pm 1.4 \pm 1.2\,^{+12.9}_{-0.2}$	$24.5 \pm 0.9 \pm 2.1\,^{+7.0}_{-1.1}$	$+3.2 \pm 3.5 \pm 2.0\,^{+2.7}_{-1.9}$	1.2σ
$\rho^0(770)K^+$; $\rho^0(770) \to \pi^+\pi^-$	$6.54 \pm 0.81 \pm 0.58\,^{+0.69}_{-0.26}$	$3.56 \pm 0.45 \pm 0.43\,^{+0.38}_{-0.15}$	$+44 \pm 10 \pm 4\,^{+5}_{-13}$	3.7σ
$f_0(980)K^+$; $f_0(980) \to \pi^+\pi^-$	$18.9 \pm 0.9 \pm 1.7\,^{+2.8}_{-0.6}$	$10.3 \pm 0.5 \pm 1.3\,^{+1.5}_{-0.4}$	$-10.6 \pm 5.0 \pm 1.1\,^{+3.4}_{-1.0}$	1.8σ
$\chi_{c0}K^+$; $\chi_{c0} \to \pi^+\pi^-$	$1.29 \pm 0.19 \pm 0.15\,^{+0.12}_{-0.03}$	$0.70 \pm 0.10 \pm 0.10\,^{+0.06}_{-0.02}$	$-14 \pm 15 \pm 3\,^{+1}_{-5}$	0.5σ
$K^+\pi^-\pi^+$ nonresonant	$4.5 \pm 0.9 \pm 2.4\,^{+0.6}_{-1.5}$	$2.4 \pm 0.5 \pm 1.3\,^{+0.3}_{-0.8}$	—	—
$K_2^{*0}(1430)\pi^+$; $K_2^{*0}(1430) \to K^+\pi^-$	$3.40 \pm 0.75 \pm 0.42\,^{+0.99}_{-0.13}$	$1.85 \pm 0.41 \pm 0.28\,^{+0.54}_{-0.08}$	$+5 \pm 23 \pm 4\,^{+18}_{-7}$	0.2σ
$\omega(782)K^+$; $\omega(782) \to \pi^+\pi^-$	$0.17 \pm 0.24 \pm 0.03\,^{+0.05}_{-0.08}$	$0.09 \pm 0.13 \pm 0.02\,^{+0.03}_{-0.04}$	—	—
$f_2(1270)K^+$; $f_2(1270) \to \pi^+\pi^-$	$0.91 \pm 0.27 \pm 0.11\,^{+0.24}_{-0.17}$	$0.50 \pm 0.15 \pm 0.07\,^{+0.13}_{-0.09}$	$-85 \pm 22 \pm 13\,^{+22}_{-2}$	3.5σ
$f_X(1300)K^+$; $f_X(1300) \to \pi^+\pi^-$	$1.33 \pm 0.38 \pm 0.86\,^{+0.04}_{-0.14}$	$0.73 \pm 0.21 \pm 0.47\,^{+0.02}_{-0.08}$	$+28 \pm 26 \pm 13\,^{+7}_{-5}$	0.6σ

- $f_X(1300)K^+$, phase-space nonresonant

BaBar PRD 78 (2008) 012004
See also Belle PRL 96 (2006) 251803

Evidence for direct CP violation
But significant model dependence

$B^+ \rightarrow K^+\pi^+\pi^-$

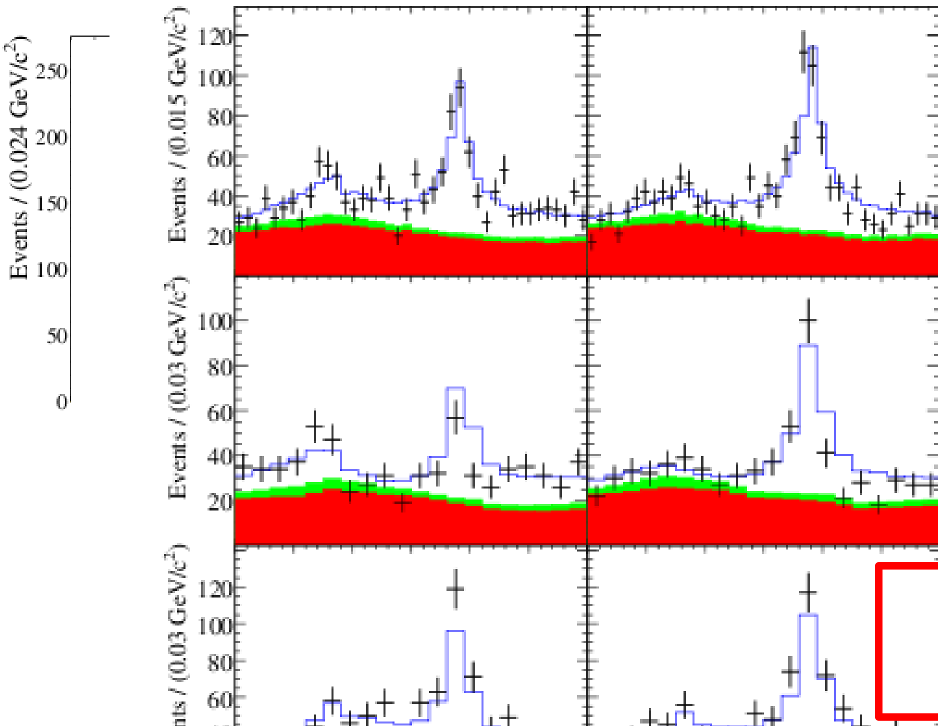


FIG. 4: Projection plots of the $\pi^+\pi^-$ invariant mass in the region of the $\rho^0(770)$ and $f_0(980)$ resonances. The left (right) plots are for B^- (B^+) candidates. The top row shows all candidates, the middle row shows those where $\cos\theta_H > 0$, and the bottom row shows those where $\cos\theta_H < 0$. The data are the black points with statistical error bars, the lower solid (red/dark) histogram is the $q\overline{q}$ component, the middle solid (green/light) histogram is the $B\overline{B}$ background contribution, while the blue open histogram shows the total fit result.

veraged over charge conjugate states) and CP asymmetries. ng fractions. The first uncertainty is statistical, the second The final column is the statistical significance of direct CP

$\mathcal{B}(B^+ \rightarrow \text{Mode})(10^{-6})$	A_{CP} (%)	DCPV sig.
$54.4 \pm 1.1 \pm 4.5 \pm 0.7$	$2.8 \pm 2.0 \pm 2.0 \pm 1.2$	
$7.2 \pm 0.4 \pm 0.7\,^{+0.3}_{-0.5}$	$+3.2 \pm 5.2 \pm 1.1\,^{+1.2}_{-0.7}$	0.9σ
$24.5 \pm 0.9 \pm 2.1\,^{+7.0}_{-1.1}$	$+3.2 \pm 3.5 \pm 2.0\,^{+2.7}_{-1.9}$	1.2σ
$.56 \pm 0.45 \pm 0.43\,^{+0.38}_{-0.15}$	$+44 \pm 10 \pm 4\,^{+5}_{-13}$	3.7σ
$10.3 \pm 0.5 \pm 1.3\,^{+1.5}_{[illegible]}$	$-10.6 \pm 5.0 \pm 1.1\,^{+3.4}_{[illegible]}$	1.8σ

Evidence for direct CP violation
But significant model dependence

Finding methods to reduce the model dependence is the goal of Les Nabis!

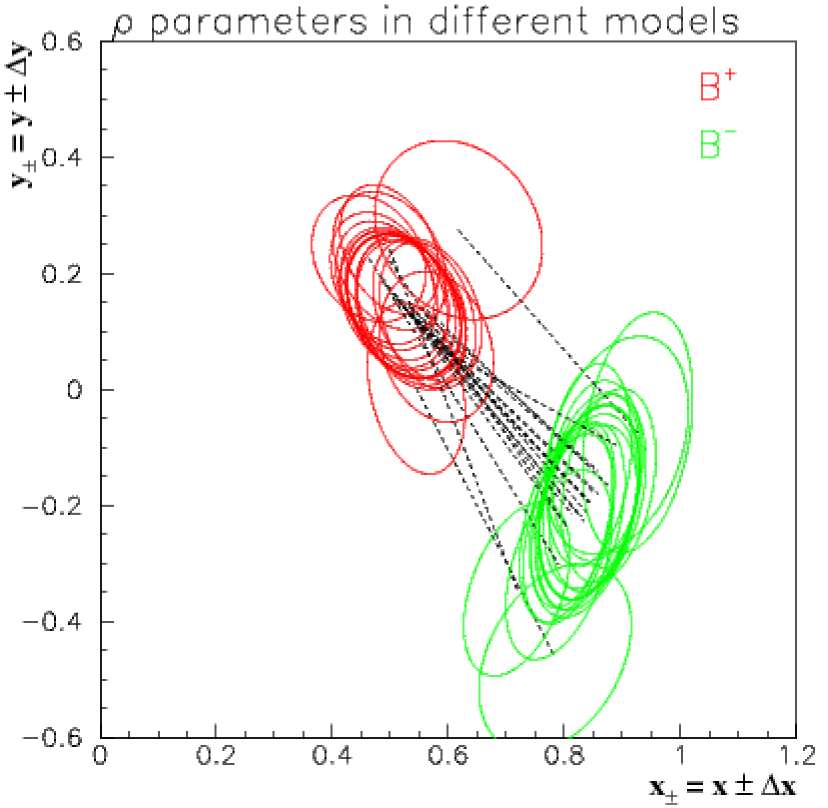
onant

BaBar PRD 78 (2008) 012004
See also Belle PRL 96 (2006) 251803

$B^+ \to K^+\pi^+\pi^-$ – model dependence

Complex coefficients parametrised as x + iy

→ $(x \pm \Delta x) + i(y \pm \Delta y)$ with CP violation



Ellipses correspond to fitted parameters obtained with different Dalitz plot models

Significance of CP violation corresponds to the lack of overlap of the ellipses

Sources of model dependence

- Lineshapes
  - coupled channels, threshold effects, etc.
- Isobar formalism
  - "sum of Breit-Wigners" model violates unitarity
  - problem most severe for broad, overlapping resonances
    - even talking about "mass" and "width" for such states is not strictly correct (process dependent) – can only be defined by pole position
- Nonresonant contributions
  - such terms are small for D decays, but are found to be large for some B decays (not well understood why)
  - interference with other (S-wave) terms can lead to unphysical phase variations

Are methods used for D decay Dalitz plots also valid for B decays?

$D \to K^- \pi^+ \pi^0$

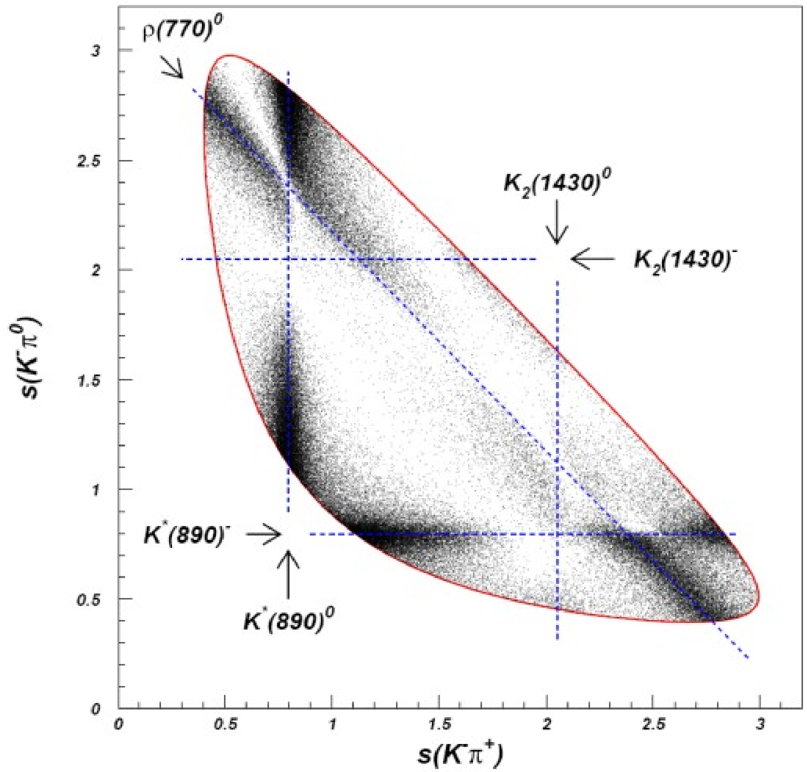
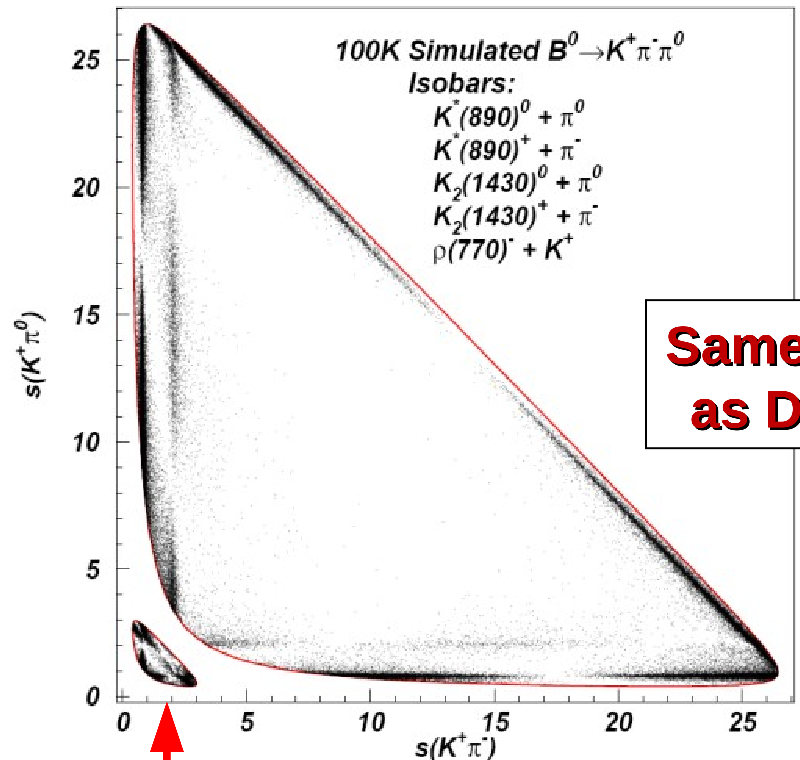


Image credit: Brian Meadows

$B \to K^- \pi^+ \pi^0$



Same model as D decay

D Dalitz plot on same scale

Which decays in particular should we look at?

Extracting weak phases from Dalitz plots

- Many methods exist in the literature
  - some have been used to date, others not yet
    - most results are statistically limited
  - still plenty of room for good new ideas
- Examples (there are many more!)
  - Snyder-Quinn method to measure α from $B \to \pi^+\pi^-\pi^0$
  - GGSZ/BP method to measure γ from $B^\pm \to DK^\pm$ with $D \to K_S\pi^+\pi^-$
  - Measurement of charm oscillation parameters using $D \to K_S\pi^+\pi^-$
  - Various methods to measure γ from three-body charmless B decays ($B_{\{u,d,s\}} \to \pi\pi\pi, K\pi\pi, KK\pi, KKK$)
  - Penguin-free measurements of β & β_s from $D\pi^+\pi^-$ & DK^+K^-, respectively
- I will mention just a couple of these examples ...

Searching for CP violation in charm Dalitz plots

- Standard Model effects are small
  - negligible in Cabibbo-favoured decays
  - not more than $O(10^{-3})$ in singly-Cabibbo-suppressed decays (see, *e.g.*, PRD 75 (2007) 036008)
  - can be enhanced up to $O(10^{-2})$ in various NP models
- Good channel for model-independent analysis
  - new LHCb analysis based on 'Miranda' approach
  - search for CP violation in $D^{\pm} \rightarrow K^{+}K^{-}\pi^{\pm}$
  - exploit $D_s^{\pm} \rightarrow K^{+}K^{-}\pi^{\pm}$ as control sample
  - care taken over binning to optimise sensitivity

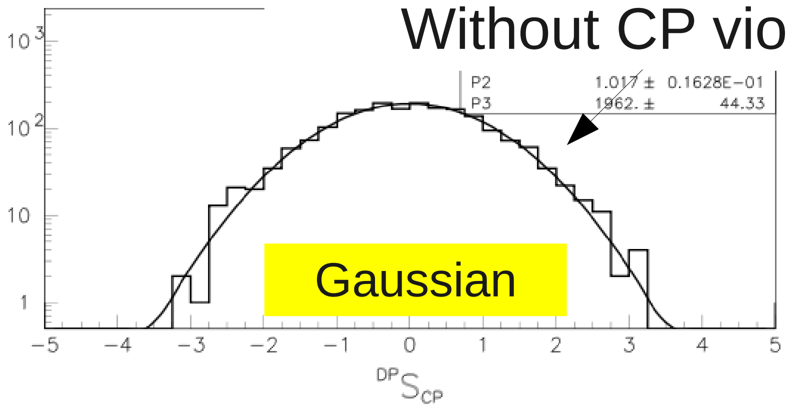
"Miranda" procedure a.k.a. Dalitz plot anisotropy

PRD 80 (2009) 096006

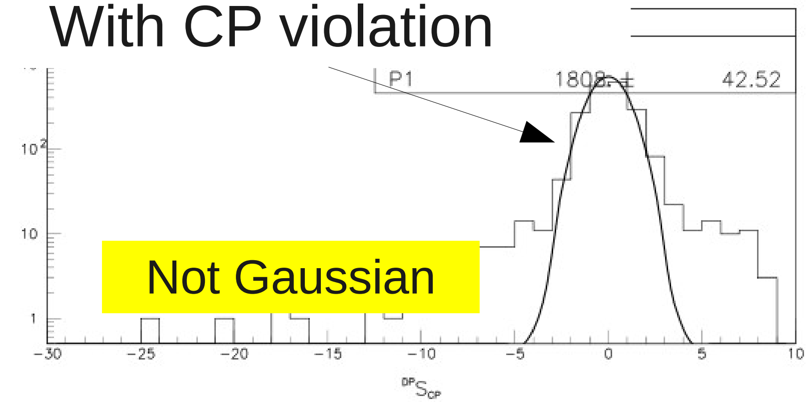
$$^{\mathrm{Dp}}S_{CP} \equiv \frac{N(i) - \bar{N}(i)}{\sqrt{N(i) + \bar{N}(i)}}$$

Toy model (using $B^+ \to K^+\pi^+\pi^-$)

Without CP violation



With CP violation



- Good model-independent way to identify CP violation
    - could be sufficient to identify non-SM physics in, e.g., charm decays
- Constant (DP independent) systematic asymmetries can be accounted for
- Can isolate region of the Dalitz plot where CP violation effects occur

But does not provide quantitative measure of weak phase

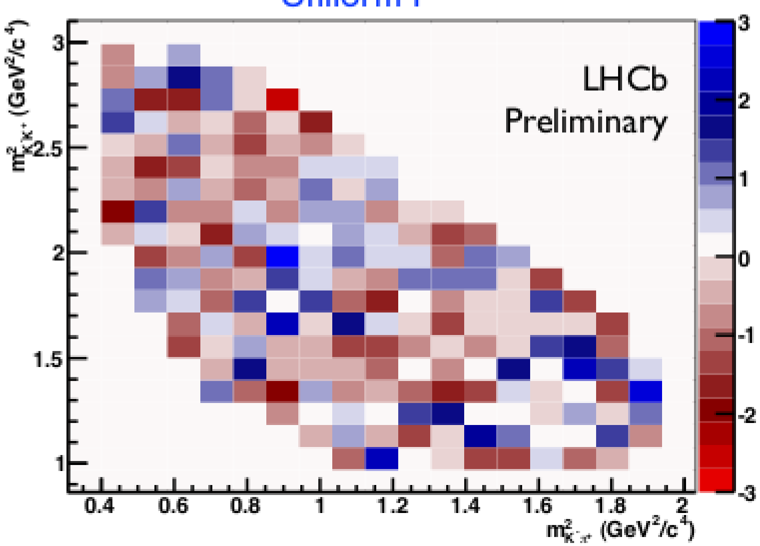
New charm CPV results at EPS

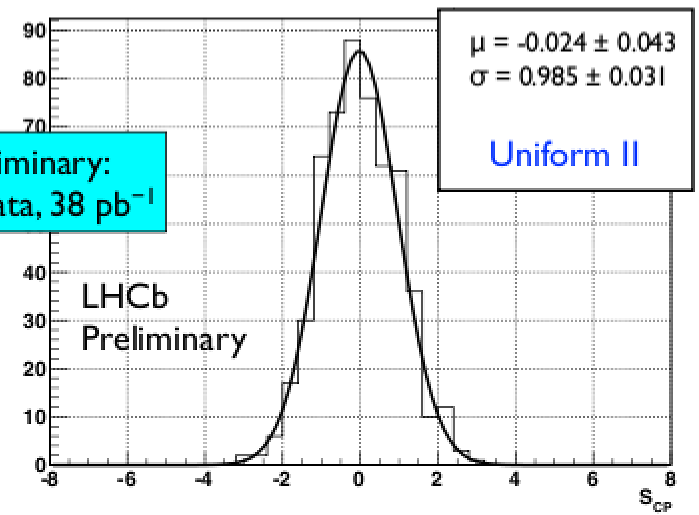
New LHCb results (shown by Mat Charles)

http://indico.in2p3.fr/materialDisplay.py?contribId=1028&sessionId=2&materialId=slides&confId=5116

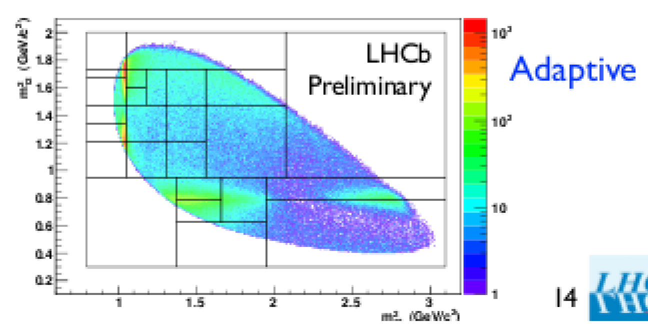
Results for $D^+ \to K^- K^+ \pi^+$

binning	χ^2/ndof	prob (%)
adaptive I	32.0/24	12.7
adaptive II	126.1/105	7.9
uniform I	191.3/198	82.1
uniform II	519.5/529	60.5





No evidence for CP violation in the 2010 dataset of 38 pb^{-1}



14

Prospects for improved analyses

- These new results put stringent limits on CP violation effects in $D^{\pm} \to K^{+}K^{-}\pi^{\pm}$ decays
  - (albeit in a manner that is slightly hard to quantify)
- Improved statistical sensitivity is guaranteed since LHCb already has a factor 10 more data on tape
- Further improvements possible using an alternative, unbinned method (arXiv:1105.5338)

Unbinned, model-independent CP violation search (arXiv:1105.5338)

The following test statistic correlates the difference between the $X \to abc$ and c.c. p.d.f.s, denoted by $f(\vec{x})$ and $\bar{f}(\vec{x})$, respectively, at different points in the multivariate space [13, 14]:

$$\begin{aligned} T &= \frac{1}{2}\int\int \left(f(\vec{x}) - \bar{f}(\vec{x})\right)\left(f(\vec{x}\,') - \bar{f}(\vec{x}\,')\right) \\ &\qquad \times \psi(|\vec{x} - \vec{x}\,'|)d\vec{x}d\vec{x}\,' \\ &= \frac{1}{2}\int\int \left[f(\vec{x})f(\vec{x}\,') + \bar{f}(\vec{x})\bar{f}(\vec{x}\,') - 2f(\vec{x})\bar{f}(\vec{x}\,')\right] \\ &\qquad \times \psi(|\vec{x} - \vec{x}\,'|)d\vec{x}d\vec{x}\,', \quad (3) \end{aligned}$$

where $\psi(|\vec{x} - \vec{x}\,'|)$ is a weighting function. T can be estimated without the need for any knowledge about the forms of f and $\bar{f}$ using $X \to abc$ and c.c. data as

$$\begin{aligned} T \approx& \frac{1}{n(n-1)}\sum_{i,j>i}^{n}\psi(\Delta\vec{x}_{ij}) \\ &+ \frac{1}{\bar{n}(\bar{n}-1)}\sum_{i,j>i}^{\bar{n}}\psi(\Delta\vec{x}_{ij}) - \frac{1}{n\bar{n}}\sum_{i,j}^{n,\bar{n}}\psi(\Delta\vec{x}_{ij}), \quad (4) \end{aligned}$$

where $\Delta\vec{x}_{ij} = |\vec{x}_i - \vec{x}_j|$ and n ($\bar{n}$) is the number of $X \to abc$ (c.c.) events. *N.b.*, in the order in which they appear in Eq. [4], the sums are over pairs of $X \to abc$ events, pairs of c.c. events and pairs consisting of an $X \to abc$ event and a c.c. event, respectively.

"energy test"

- low p-value when CP violation present
- flat p-value in absence of CP violation
- outperforms binned test

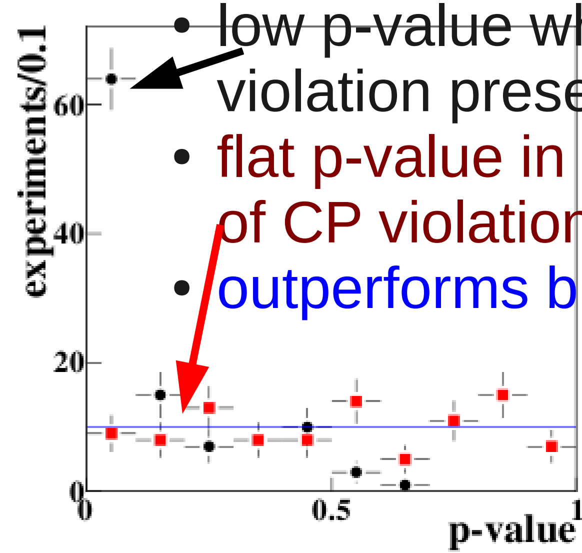


FIG. 4: p-value distributions obtained using the energy test on the CP-conserving (red squares) and CP-violating (black circles) ensembles of data sets. The (solid blue) line shows the expected distribution for the CP-conserving case.

test	$1\sigma(\%)$	$2\sigma(\%)$	$3\sigma(\%)$
χ^2	38 ± 5	3 ± 2	0 ± 1
energy	87 ± 3	52 ± 5	13 ± 3

TABLE II: Observed deviation levels for the CP-violating ensemble of data sets for the χ^2 and energy tests.

Snyder-Quinn method for α

PHYSICAL REVIEW D VOLUME 48, NUMBER 5 1 SEPTEMBER 1993

Measuring *CP* asymmetry in $B \to \rho\pi$ decays without ambiguities

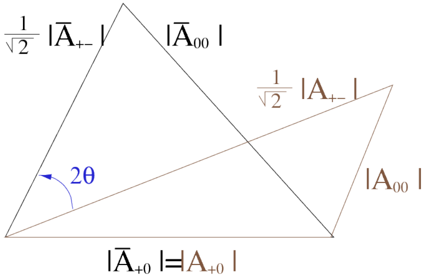
PRD 48 (1993) 2139

Arthur E. Snyder and Helen R. Quinn
Stanford Linear Accelerator Center, Stanford University, Stanford, California 94309
(Received 24 February 1993)

- Methods to measure α exploit time-dependent CP violation in B_d decays via $b \to u$ transitions (eg. $B_d \to \pi^+\pi^-$)

PRL 65 (1990) 3381

- Penguin "pollution" can be subtracted using Gronau-London isospin triangles built from $A(\pi^+\pi^-)$, $A(\pi^+\pi^0)$, $A(\pi^0\pi^0)$
- Expect discrete ambiguities in the solution for α



- Ambiguities can be resolved if you measure both real and imaginary parts of $\lambda = (q/p)(\bar{A}/A)$
  - ie. measure cos(2α) as well as sin(2α)

Toy model for $B \to \pi^+\pi^-\pi^0$ Dalitz plot

Contributions only from $\rho^+\pi^-$, $\rho^-\pi^+$ and $\rho^0\pi^0$

PRD 48 (1993) 2139

27 parameters renamed “U” and “I” in commonly used notation

H.Quinn and J.Silva, PRD 62 (2000) 054002

TABLE I. The time and kinematic dependence of contributions to the distribution of events.

Time dependence	Kinematic form	Amplitude measured	α dependence (all $P_i=0$)
1	f^+f^{+*}	$S_3S_3^* + \bar{S}_4\bar{S}_4^*$	1
$\cos(\Delta M t)$	f^+f^{+*}	$S_3S_3^* - \bar{S}_4\bar{S}_4^*$	1
$\sin(\Delta M t)$	f^+f^{+*}	$\mathrm{Im}(q\bar{S}_4S_3^*)$	$\sin(2\alpha)$
1	f^-f^{-*}	$S_4S_4^* + \bar{S}_3\bar{S}_3^*$	1
$\cos(\Delta M t)$	f^-f^{-*}	$S_4S_4^* - \bar{S}_3\bar{S}_3^*$	1
$\sin(\Delta M t)$	f^-f^{-*}	$\mathrm{Im}(q\bar{S}_3S_4^*)$	$\sin(2\alpha)$
1	f^0f^{0*}	$(S_5S_5^* + \bar{S}_5\bar{S}_5^*)/4$	1
$\cos(\Delta M t)$	f^0f^{0*}	$(S_5S_5^* - \bar{S}_5\bar{S}_5^*)/4$	1
$\sin(\Delta M t)$	f^0f^{0*}	$\mathrm{Im}(q\bar{S}_5S_5^*)/4$	$\sin(2\alpha)$
1	$\mathrm{Re}(f^+f^{-*})$	$\mathrm{Re}(S_3S_4^* + \bar{S}_4\bar{S}_3^*)$	1
$\cos(\Delta M t)$	$\mathrm{Re}(f^+f^{-*})$	$\mathrm{Re}(S_3S_4^* - \bar{S}_4\bar{S}_3^*)$	1
$\sin(\Delta M t)$	$\mathrm{Re}(f^+f^{-*})$	$\mathrm{Im}(q\bar{S}_4S_4^* - q^*S_3\bar{S}_3^*)$	$\sin(2\alpha)$
1	$\mathrm{Im}(f^+f^{-*})$	$\mathrm{Im}(S_3S_4^* + \bar{S}_4\bar{S}_3^*)$	1
$\cos(\Delta M t)$	$\mathrm{Im}(f^+f^{-*})$	$\mathrm{Im}(S_3S_4^* - \bar{S}_4\bar{S}_3^*)$	1
$\sin(\Delta M t)$	$\mathrm{Im}(f^+f^{-*})$	$\mathrm{Re}(q\bar{S}_4S_4^* - q^*S_3\bar{S}_3^*)$	$\cos(2\alpha)$
1	$\mathrm{Re}(f^+f^{0*})$	$\mathrm{Re}(S_3S_5^* + \bar{S}_4\bar{S}_5^*)/2$	1
$\cos(\Delta M t)$	$\mathrm{Re}(f^+f^{0*})$	$\mathrm{Re}(S_3S_5^* - \bar{S}_4\bar{S}_5^*)/2$	1
$\sin(\Delta M t)$	$\mathrm{Re}(f^+f^{0*})$	$\mathrm{Im}(q\bar{S}_4S_5^* + q^*S_3\bar{S}_5^*)/2$	$\sin(2\alpha)$
1	$\mathrm{Im}(f^+f^{0*})$	$\mathrm{Im}(S_3S_5^* + \bar{S}_4\bar{S}_5^*)/2$	1
$\cos(\Delta M t)$	$\mathrm{Im}(f^+f^{0*})$	$\mathrm{Im}(S_3S_5^* - \bar{S}_4\bar{S}_5^*)/2$	1
$\sin(\Delta M t)$	$\mathrm{Im}(f^+f^{0*})$	$\mathrm{Re}(q\bar{S}_4S_5^* - q^*S_3\bar{S}_5^*)/2$	$\cos(2\alpha)$
1	$\mathrm{Re}(f^-f^{0*})$	$\mathrm{Re}(S_4S_5^* + \bar{S}_3\bar{S}_5^*)/2$	1
$\cos(\Delta M t)$	$\mathrm{Re}(f^-f^{0*})$	$\mathrm{Re}(S_4S_5^* - \bar{S}_3\bar{S}_5^*)/2$	1
$\sin(\Delta M t)$	$\mathrm{Re}(f^-f^{0*})$	$\mathrm{Im}(q\bar{S}_3S_5^* - q^*S_4\bar{S}_5^*)$	$\sin(2\alpha)$
1	$\mathrm{Im}(f^-f^{0*})$	$\mathrm{Im}(S_4S_5^* + \bar{S}_3\bar{S}_5^*)/2$	1
$\cos(\Delta M t)$	$\mathrm{Im}(f^-f^{0*})$	$\mathrm{Im}(S_4S_5^* - \bar{S}_3\bar{S}_5^*)/2$	1
$\sin(\Delta M t)$	$\mathrm{Im}(f^-f^{0*})$	$\mathrm{Re}(q\bar{S}_3S_5^* - q^*S_4\bar{S}_5^*)/2$	$\cos(2\alpha)$

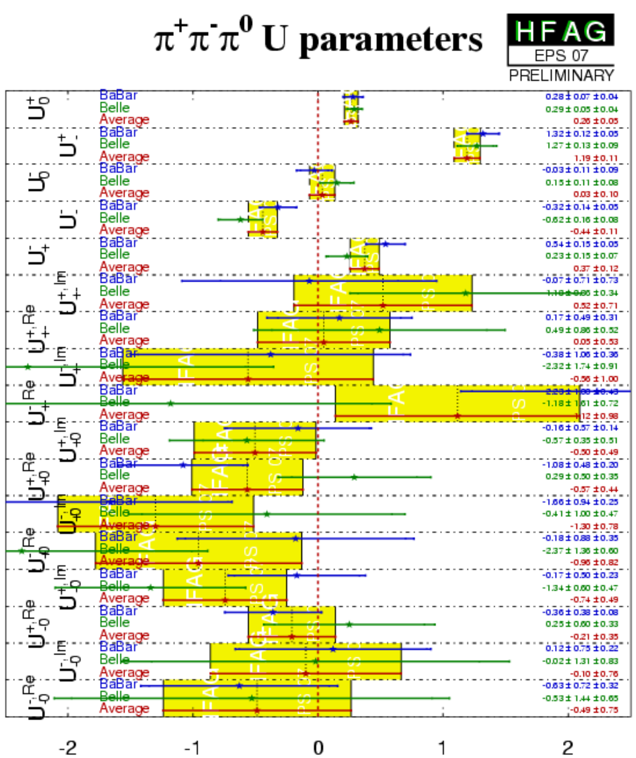
Note: physical observables depend on either $\sin(2\alpha)$ or $\cos(2\alpha)$ – never “directly” on α

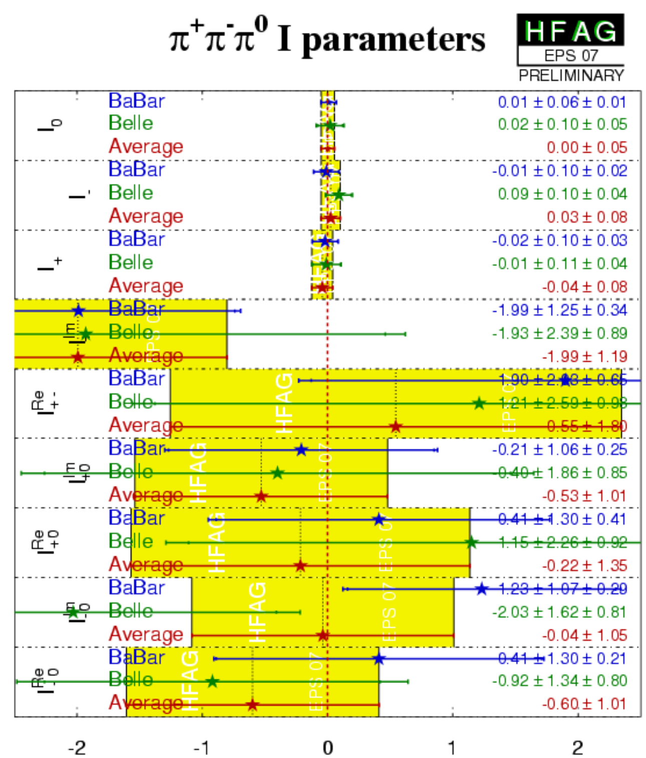
f terms contain hadronic physics (lineshape, spin)

$S_3 = A(\rho^+\pi^-)$, $S_4 = A(\rho^-\pi^+)$, $S_5 = A(\rho^0\pi^0)$,

$B \to \pi^+\pi^-\pi^0$ – B factory results

- Results from
  - Belle, 449 M BB pairs: PRL 98 (2007) 221602, PRD 77 (2008) 072001
  - BaBar, 375 M BB pairs: PRD 76 (2007) 012004





$B \to \pi^+\pi^-\pi^0$ – B factory results

- Results from
  - Belle, 449 M BB pairs: PRL 98 (2007) 221602, PRD 77 (2008) 072001
  - BaBar, 375 M BB pairs: PRD 76 (2007) 012004

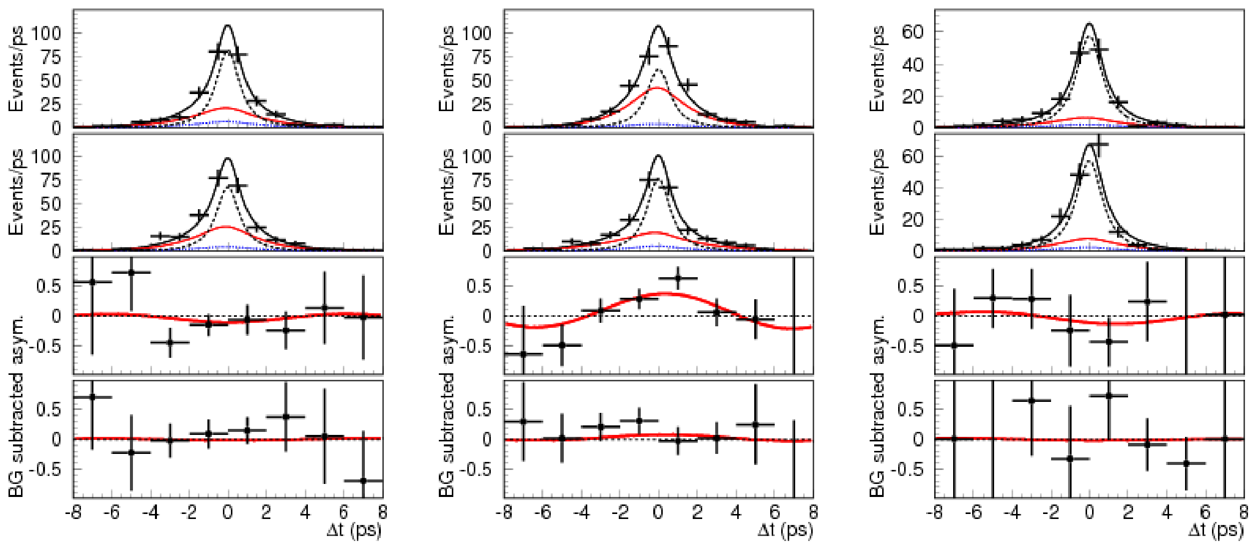
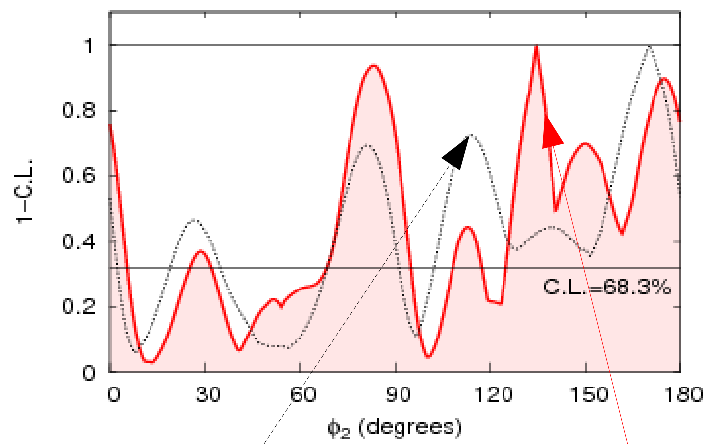


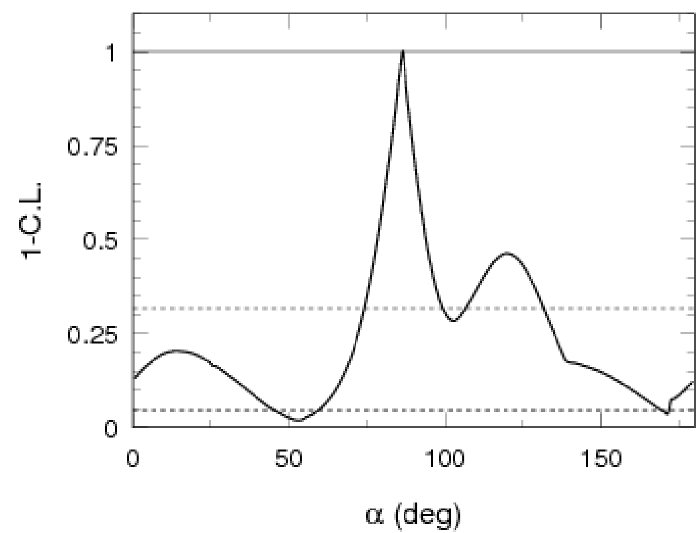
FIG. 10: Proper time distributions of good tag ($r > 0.5$) regions for $f_{\rm tag} = B^0$ (upper) and $f_{\rm tag} = \overline{B}^0$ (middle upper), in $\rho^+\pi^-$ (left), $\rho^-\pi^+$ (middle), $\rho^0\pi^0$ (right) enhanced regions, where solid (red), dotted, and dashed curves correspond to signal, continuum, and $B\overline{B}$ PDFs. The middle lower and lower plots show the background-subtracted asymmetries in the good tag ($r > 0.5$) and poor tag ($r < 0.5$) regions, respectively. The significant asymmetry in the $\rho^-\pi^+$ enhanced region (middle) corresponds to a non-zero value of U^-_-.

$\rho^+\pi^-$ $\rho^-\pi^+$ $\rho^0\pi^0$

$B \to \pi^+\pi^-\pi^0$ – B factory results

- Results from
  - Belle, 449 M BB pairs: PRL 98 (2007) 221602, PRD 77 (2008) 072001
  - BaBar, 375 M BB pairs: PRD 76 (2007) 012004





Contour from $B \to \pi^+\pi^-\pi^0$ only

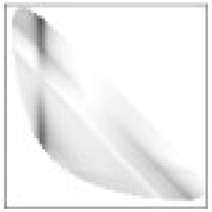
Including also information on $B^+ \to \rho^+\pi^0$ and $B^+ \to \rho^0\pi^+$

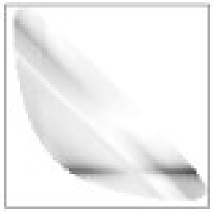
$B^{\pm} \rightarrow DK^{\pm}$ with $D \rightarrow K_S\pi^+\pi^-$

Interference between $b \rightarrow u$ and $b \rightarrow c$ amplitudes when D is reconstructed in final state common to D^0 and $\bar{D}^0$ provides sensitivity to γ

$$|M_{\pm}(m_+^2, m_-^2)|^2 = |f_D(m_+^2, m_-^2) + re^{i\delta_B \pm i\phi_3} f_D(m_-^2, m_+^2)|^2$$

$$= \Bigg| \quad \text{[plot]} \quad + re^{i\delta_B \pm i\phi_3} \quad \text{[plot]} \quad \Bigg|^2$$





Model ($f_D(m_+^2, m_-^2)$) taken from measurements of $|f_D|^2$ using flavour tagging D* decays – model dependence

BaBar obtain
$\gamma = (68^{+15}_{-14} \pm 4 \pm 3)°$
(from DK^-, D^*K^- & DK^{*-})

PRL 105 (2010) 121801

Belle obtain
$\phi_3 = (78^{+11}_{-12} \pm 4 \pm 9)°$
(from DK^- & D^*K^-)

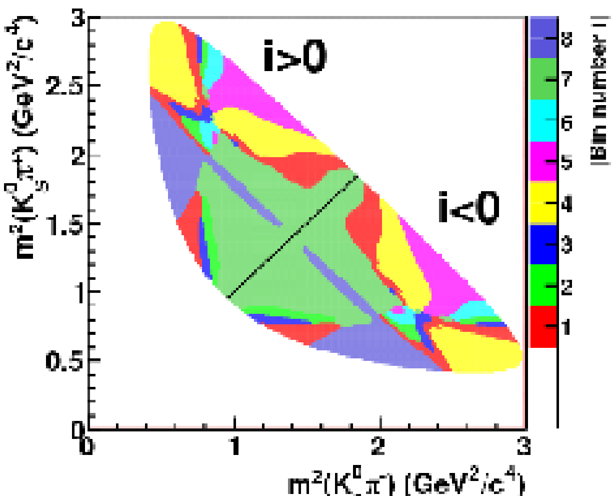
PRD 81 (2010) 112002

$B^{\pm} \to DK^{\pm}$ with $D \to K_S\pi^+\pi^-$

Solution – bin the Dalitz plot and use $\psi(3770) \to D\bar{D}$ events (CLEOc, BES) to measure per-bin phases

PRD 68, 054018 (2003), EPJ C 47, 347 (2006); EPJ C 55, 51 (2008)

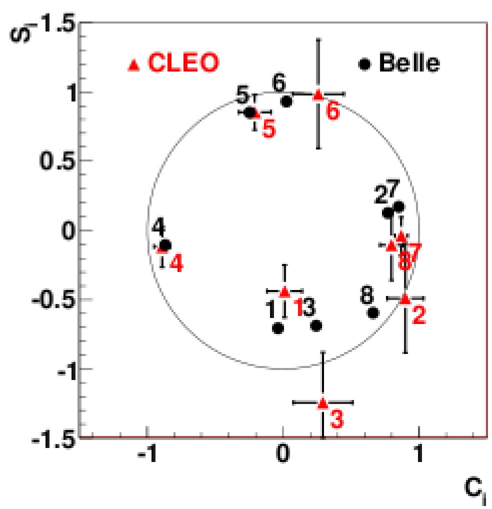
(unusual bin shapes to attempt to optimise sensitivity)



$$M_i^{\pm} = h\{K_i + r_B^2 K_{-i} + 2\sqrt{K_i K_{-i}}(x_{\pm}c_i + y_{\pm}s_i)\}$$

$$x_{\pm} = r_B \cos(\delta_B \pm \phi_3) \quad y_{\pm} = r_B \sin(\delta_B \pm \phi_3)$$

c_i, s_i measured by CLEO
PRD 82, 112006 (2010)



First model independent measurement of γ in this mode by Belle

Belle obtain

$\varphi_3 = (77.3\ ^{+15.1}_{-14.9} \pm 4.2 \pm 4.3)°$

Content of the lectures

- Why do we believe that multibody hadronic decays of heavy flavours may provide a good laboratory to search for new sources of CP violation?

Today

- Which decays in particular should we look at?

- What methods can we use to study them?

Thursday

- What are the difficulties we encounter when trying to do the analysis?

Summary

- Dalitz plot analyses provide promising methods to measure weak phases and CP violation
- Many attractive features …
- … but significant complications due to model dependence
- Need progress on several fronts
  - Understand better (ππ), (Kπ), (KK), (Dπ), (DK) systems
  - “Nonresonant” contributions and 3-body unitarity
  - Methods to combat model-dependence
  - Nabis initiative set up to try to address this

Fermilab fixed target charm and beauty experiments

5. PHYSICS OF CHARM AND BEAUTY

From hep-ex/0008076

E400 - charmed particle production by neutrons

E653 - Charm and Beauty Decays in a Hybrid Emulsion Spectrometer

E672 - Hadronic Final States in Association with High Mass Dimuons

E687 - Photoproduction of Charm and Beauty

E691 - Charm Production with the Tagged Photon Spectrometer

E743 - Charm Production in pp Collisions with LEBC-FMPS

E769 - Hadroproduction of charm

E771 - Beauty Production by Protons

E781/SELEX - Study of Charm Baryon Physics

E789 - beauty-Quark Mesons and Baryons

E791 - Hadroproduction of Charm

E831/FOCUS - Heavy Quarks study Using the Wideband Photon Beam