

# Technology enhanced learning in Statistics

Jérémie Houssineau

28 May 2021

# Outline

- 1 TEL in general
- 2 TEL in Statistics
- 3 Interactive plots
- 4 Notebooks
- 5 Comparative judgement *by Ian Hamilton*

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# Why TEL

## Source

HEFCE (Higher Education Funding Council for England) (2009). “Enhancing Learning and Teaching Through the Use of Technology.”

### *Potential benefits of TEL:*

#### 1. Efficiency

→ existing processes carried out in a more cost-effective, time-effective, sustainable or scalable manner

#### 2. Enhancement

→ improving existing processes and the outcomes

#### 3. Transformation

→ radical, positive change in existing processes or introducing new processes

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### *Types of enhancement:*

1. Operational improvement
  - greater flexibility for students; resources more accessible
2. Quantitative change in learning
  - increased engagement; improved test scores
3. Qualitative change in learning
  - promoting reflection on learning; deeper engagement; richer understanding

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Tversky, B., Morrison, J.B. & Betrancourt, M. (2002). “Animation: can it facilitate?”  
International journal of human-computer studies, 57(4), 247-262

### 1. Static graphics?

→ only if carefully designed

### 2. Animated graphics?

→ research on efficacy not encouraging

→ often too complex or too fast to be accurately perceived

→ judicious use of interactivity may overcome both these disadvantages

A few examples: [Tesseract](#) | [Simulated annealing](#) | [Dirichlet process](#)

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# Longevity of TEL tools?

## 1. Trends

→ Article from 2013: *Is it a tool suitable for learning? A critical review of the literature on Facebook as a technology-enhanced learning environment*

## 2. Support

→ Flash no longer supported

## 3. Maintenance

→ Backward compatibility not always ensured

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## Home / Explore features of probability distributions

Select a distribution:

Poisson

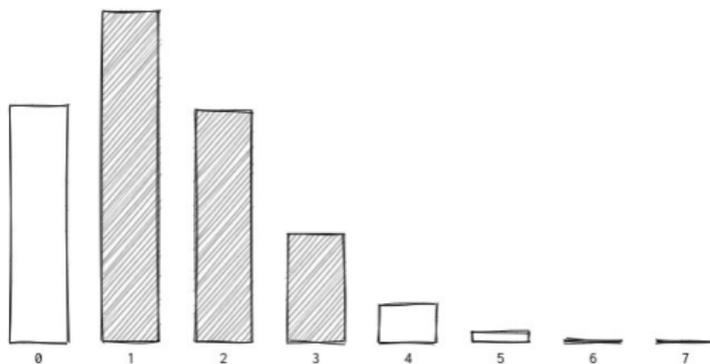
Parameter(s):

$\lambda = 1.4$  mean rate

Explore features

Highlight outcomes between 1 and

3



Developed by [Anna Ferrusson](#), Department of Statistics, University of Auckland

[Link](#)

## Home / Explore goodness-of-fit for probability distributions

Clear

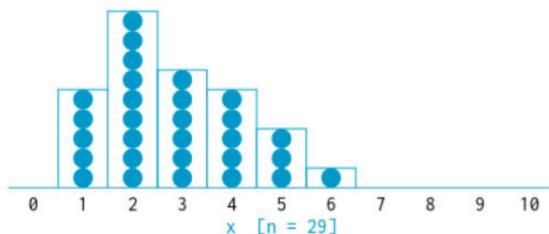
## The situation

Variable description Rounding - nearest 

## Sample data


 Compare to model


mean = 2.828

 Show mean Show standard deviation Show middle 95%Developed by [Anna Fergusson](#), Department of Statistics, University of Auckland

## The model

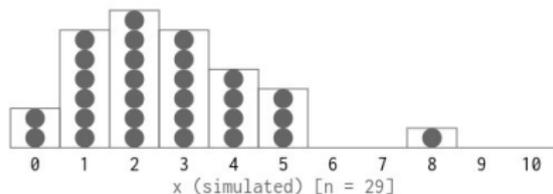
Select distribution  $\lambda =$  

## Simulated data

Generate  values


 Show over-fitted shape

mean = 2.655



# SOCR Bivariate Normal Distribution

### Settings

$\rho =$

$\mu_x =$    $\mu_y =$

$\sigma_x =$    $\sigma_y =$

Use WebGL

### Controls

< X <      < Y <

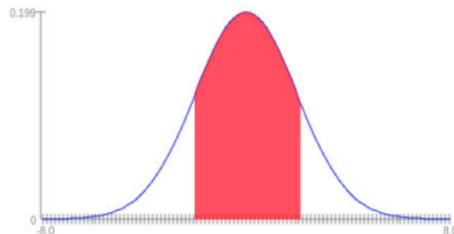
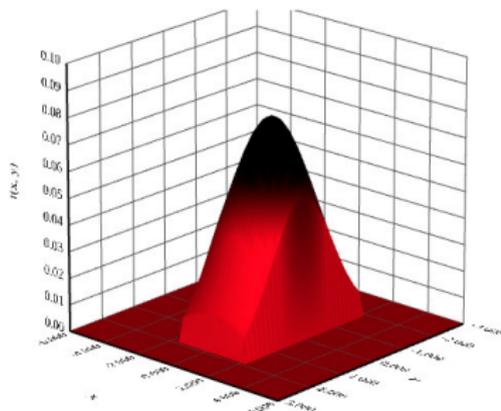
Marginal of X                       Marginal of Y  
 Conditional of X|Y = -2             Conditional of X|Y = 2  
 Conditional of Y|X = -2             Conditional of Y|X = 2

Probability Results

$P(-2 < Y < 2$	$X = 2) = 0.954$
$P(-2 < X < 2$	$Y = 2) = 0.683$

### Instructions

- **Requirements** - modern web-browser with HTML and JavaScript support. The 3D view of the bivariate distribution requires WebGL support.
- See the [SOCR Bivariate Normal Distribution Activity](#).
- Use the **Settings** to initialize the web-app. To activate new input settings click outside the component.
- In the **Control** panel you can select the appropriate bivariate limits for the X and Y variables, choose desired *Marginal* or *Conditional* probability function, and view the 1D Normal Distribution graph. Use any non-numerical character to specify infinity ( $\infty$ ).
- You can rotate the bivariate normal distribution in 3D by clicking and dragging on the graph.
- **Probability Results** are reported in the bottom text area.



[Link](#)

## Source

Christou, N., & Dinov, I.D. (2010). "A study of students' learning styles, discipline attitudes and knowledge acquisition in technology-enhanced probability and statistics education." *Journal of online learning and teaching*, 6(3).

### *Identify learning styles:*

1. Information processing: active / passive
2. Information perception: sensory / intuitive
3. Sensory channel: visual / auditory
4. Understanding process: sequential / global

### *Findings:*

1. Marginal but consistent effect of TEL  
→ improved satisfaction and quantitative performance
2. Dependent on learning style

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# bokedh



Histogram | Crossfilter

*Advantages:*

- Relatively simple to use
- Default style is often sufficient

*Drawbacks:*

- Backward compatibility is not always maintained
- Specific functions for plots ( $\neq$  `matplotlib`,  $\sim$  `ggplot`)

*Some example:*

- Normal likelihood with unknown mean
- Kalman filter

*Accessibility:*

*Alternative with R:* [Shiny](#) (Thank you Martyn)

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# Disclaimer



The following poorly-commented code is for illustration purposes only

# Example

## Initialisation

```
# True parameter
mu = 2
sig_default = 1.0

# Number of points to plot the p.d.f.s (reduce this number of speed)
N = 250

x = np.linspace(-5, 5, N)
y = normal_pdf(x, 0.0, 1.0)
N0 = ColumnDataSource(data=dict(x=x, y=y))
N1 = ColumnDataSource(data=dict(x=x, y=y))

y = normal_pdf(x, mu, sig_default**2)
N2 = ColumnDataSource(data=dict(x=x, y=y))

# Function regenerating the observations
max_n_obs = 10
obs_root = np.random.randn(max_n_obs)

y_obs = np.array((0,0.2))
```

# Example

## Plot

```
# Set up plot
plot = figure(plot_height=400, plot_width=800, title="Prior, posterior and
              sampling distributions",
              tools="crosshair,pan,reset,save,wheel_zoom",
              x_range=[-5, 5], y_range=[0, 1.1])

plot.line('x', 'y', legend='prior', source=N0, line_width=3, line_alpha=0.6)
plot.line('x', 'y', source=N1, line_width=3, line_alpha=0.6, legend='
              posterior', line_dash='dashed')
plot.line('x', 'y', source=N2, line_width=3, line_alpha=0.6, legend='sampling
              ', color='firebrick')

obs_data_list = []
obs_plot_list = []
for i in range(max_n_obs):
    obs = obs_root[i]*sig_default + mu
    x_obs = obs*np.ones(2)
    obs_data_list.append(ColumnDataSource(data=dict(x=x_obs, y=y_obs)))
    obs_plot_list.append(plot.line('x', 'y', source=obs_data_list[i],\
                                   color='firebrick', line_width=3, line_alpha=0.6))
```

# Example

## Widgets

```
# Set up widgets
button = Button(label="Regenerate observations")
mu_0 = Slider(title="mu_0", value=0, start=-5, end=5, step=0.1)
sigma_0 = Slider(title="sigma_0", value=1, start=0.01, end=5, step=0.1)
sigma = Slider(title="sigma", value=sig_default, start=0.01, end=5, step=0.1)
n_obs = Slider(title="n", value=0, start=0, end=max_n_obs, step=1)
```

# Example

## Update plot I

```

# Update data frames
def update(attrname, old, new):
    mu_0_val = mu_0.value
    var_0 = sigma_0.value**2
    n = n_obs.value
    var = sigma.value**2
    loc_obs = obs_root * sigma.value + mu
    for i in range(max_n_obs):
        x_obs = loc_obs[i]*np.ones(2)
        vis = (i < n)
        obs_data_list[i].data = dict(x=x_obs, y=y_obs)
        obs_plot_list[i].visible = vis

    obs = 0
    if n > 0:
        obs = np.mean(loc_obs[:n])

    mu_post = (n * var_0 * obs + var * mu_0_val) / (n * var_0 + var)
    var_post = (var_0 * var) / (n * var_0 + var)
    N0.data = dict(x=x, y=normal_pdf(x, mu_0_val, var_0))
    N1.data = dict(x=x, y=normal_pdf(x, mu_post, var_post))
    N2.data = dict(x=x, y=normal_pdf(x, mu, var))

```

# Example

## Update plot II

```
# Function regenerating the observations
def reg():
    global obs_root
    obs_root = np.random.randn(max_n_obs)
    update('value', 1, 1)

button.on_click(reg)
mu_0.on_change('value', update)
sigma_0.on_change('value', update)
sigma.on_change('value', update)
n_obs.on_change('value', update)

# Set up layouts and add to document
inputs = widgetbox(button, mu_0, sigma_0, sigma, n_obs)

curdoc().add_root(row(inputs, plot, width=800))
curdoc().title = "Normal likelihood: unknown mean"
```

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*In general:*

- Gentle introduction to programming
- Accessible even with little knowledge of Python/R
- Suitable environment for active learning

*Jupyter notebooks:*

- Intuitive environment
- Can be run online with the [GitHub + Binder](#) solution
- [Example](#)



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# R Notebooks

The screenshot shows an R Notebook window titled "Untitled1". The code editor contains the following R code:

```

1 ---
2 title: "R Notebook"
3 output: htmL_notebook
4 ---
5
6 {r}
7 DT::datatable(mtcars, width = 500)
8 ---

```

The rendered output displays a data table with 500 entries (shown as 5 rows) and a search bar. The table columns are mpg, cyl, disp, hp, drat, wt, and qsec. The data shown is as follows:

	mpg	cyl	disp	hp	drat	wt	qsec
Mazda RX4	21	6	160	110	3.9	2.62	16.46
Mazda RX4 Wag	21	6	160	110	3.9	2.875	17.02
Datsun 710	22.8	4	108	93	3.85	2.32	18.61
Hornet 4 Drive	21.4	6	258	110	3.08	3.215	19.44
Hornet Sportabout	18.7	8	360	175	3.15	3.44	17.02

The interface also shows a status bar at the bottom with the time 7:35, "Chunk 1", and "R Markdown".

## Concluding remarks

- There is an opportunity for quantitative and qualitative enhancement
  - Interactive plots for engagement
  - Notebooks for active learning
- Gradual increase in students' degrees of freedom
- Happy to help if anyone wants to try **bokeh**

What do you think?

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# Comparative Judgement

Over to you, Ian.