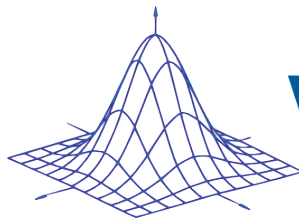


# Structural Representations of Materials for Machine Learning using the Novel Materials Discovery Big-Data Analytics Platform



Berk Onat

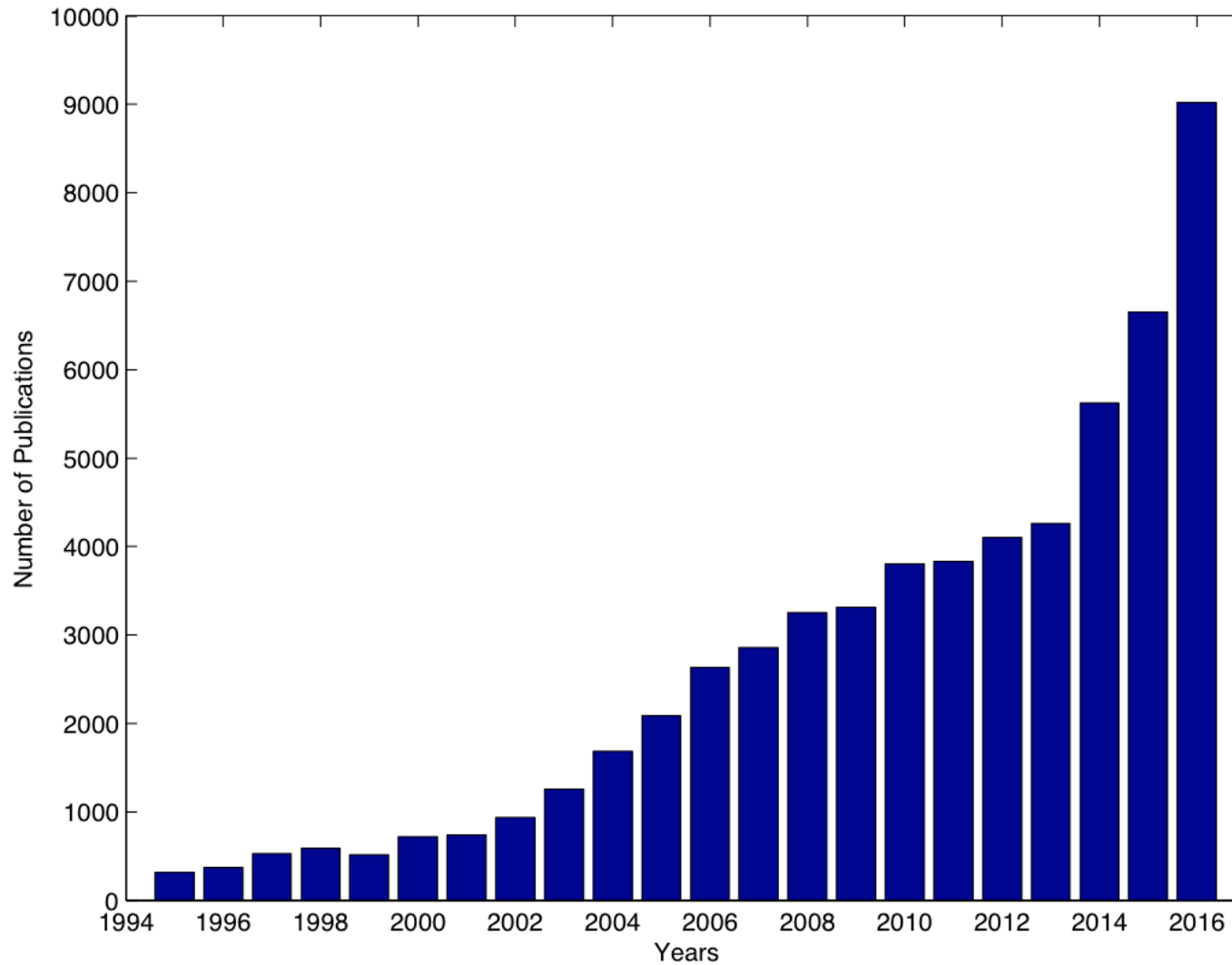
School of Engineering  
University of Warwick



**WCPM**

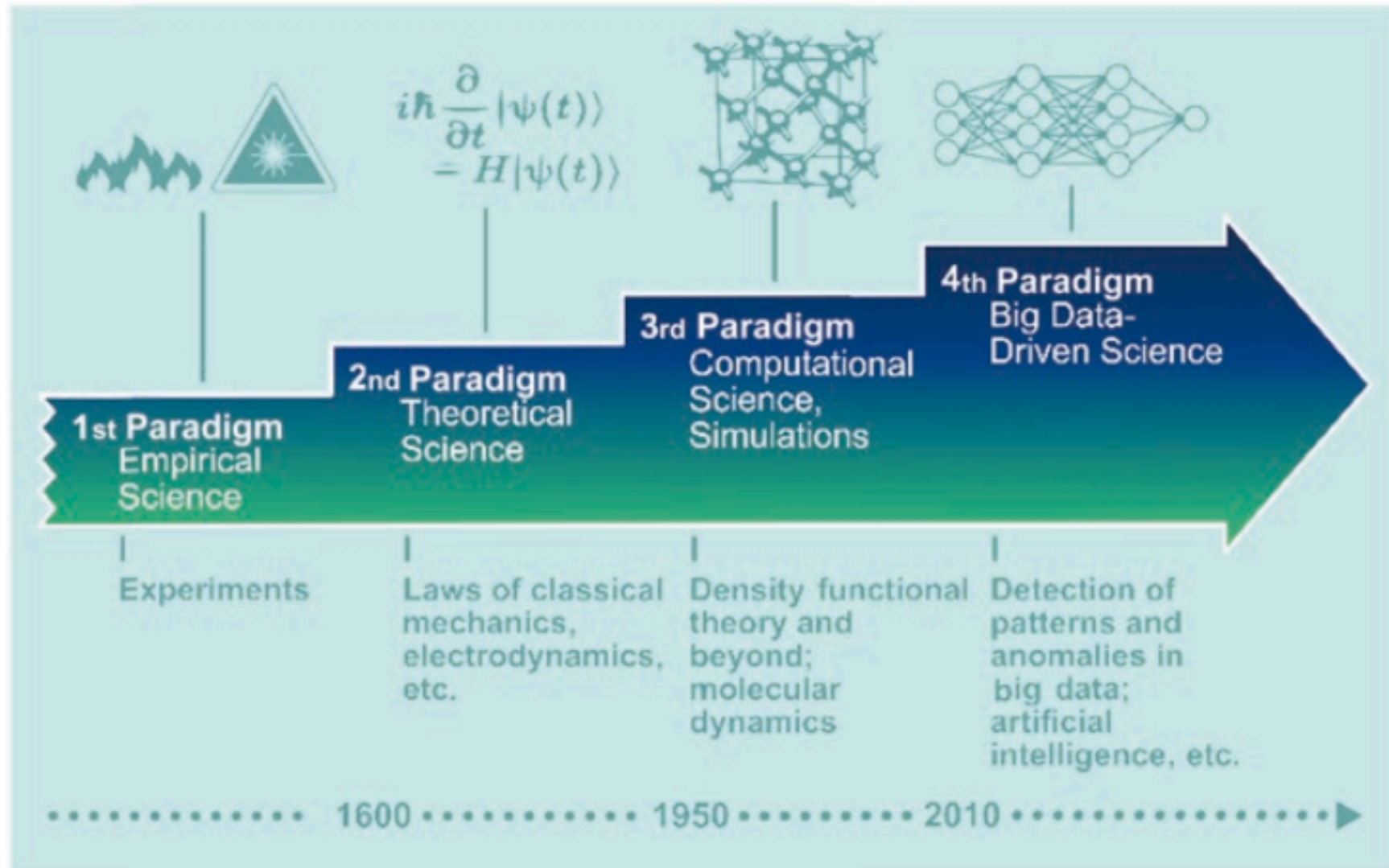
Warwick Centre for  
Predictive Modelling

# Why Machine Learning is popular now?



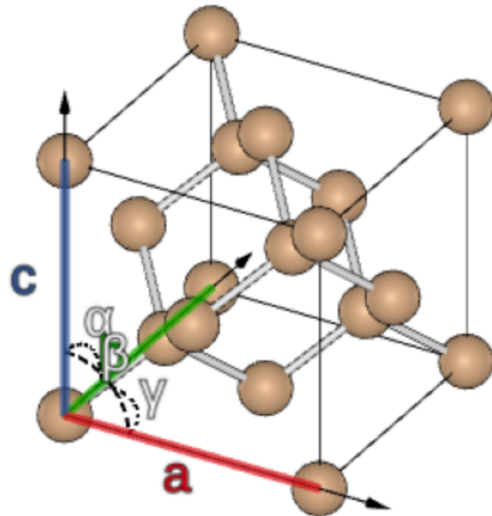
Number of publications per year between 1994 to 2016 (Web of Science)

# Paradigms of Material Science and Engineering

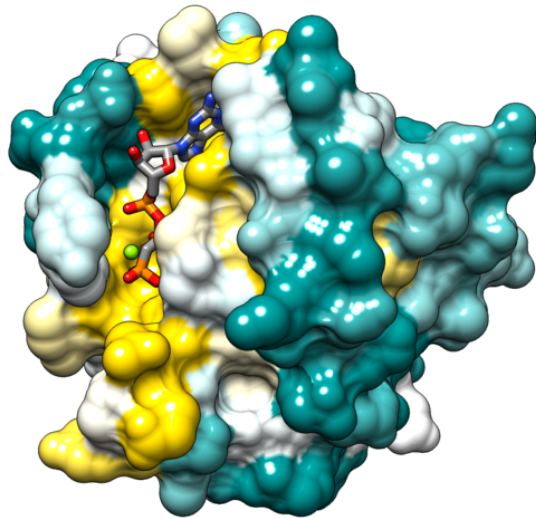


Ref: Claudia Draxl and Matthias Scheffler, "NOMAD: The FAIR concept for big data-driven materials science", MRS Bulletin, Volume 43, (2018) 676-682.

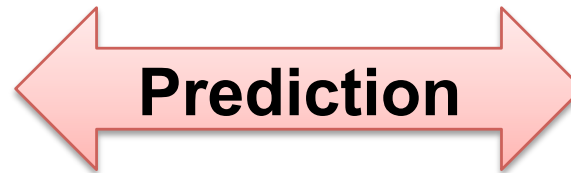
# Big-Data Analytics in Material Science and Engineering



**Si Diamond Crystal**



**HRAS Protein (~7000 Atoms) Ref: Wikipedia / PDB**



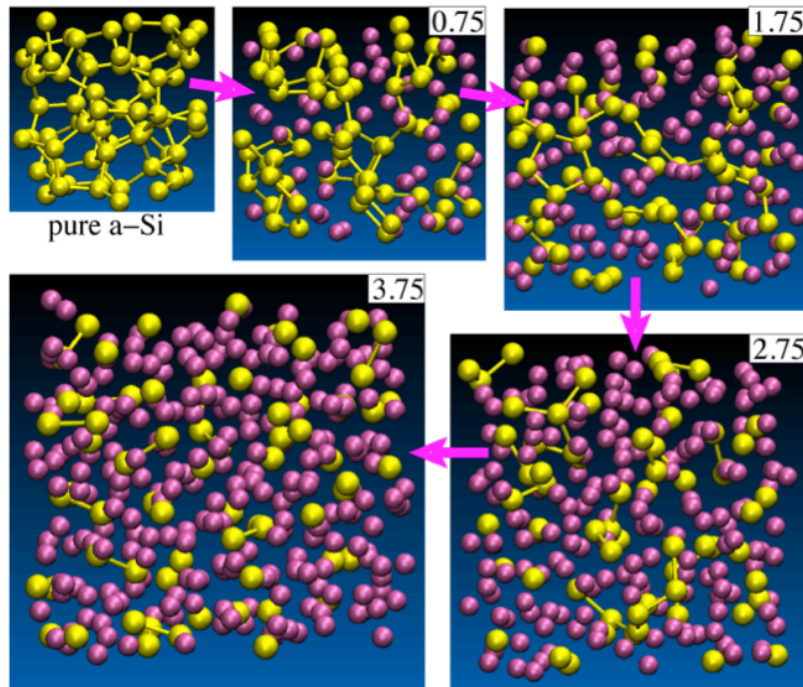
**Electronic or Structural Properties:**

- Energies**
- Forces**
- Atomic Charges**
- Magnetization**
- Band Structure**
- Band Gap**
- Density of States**
- ...**



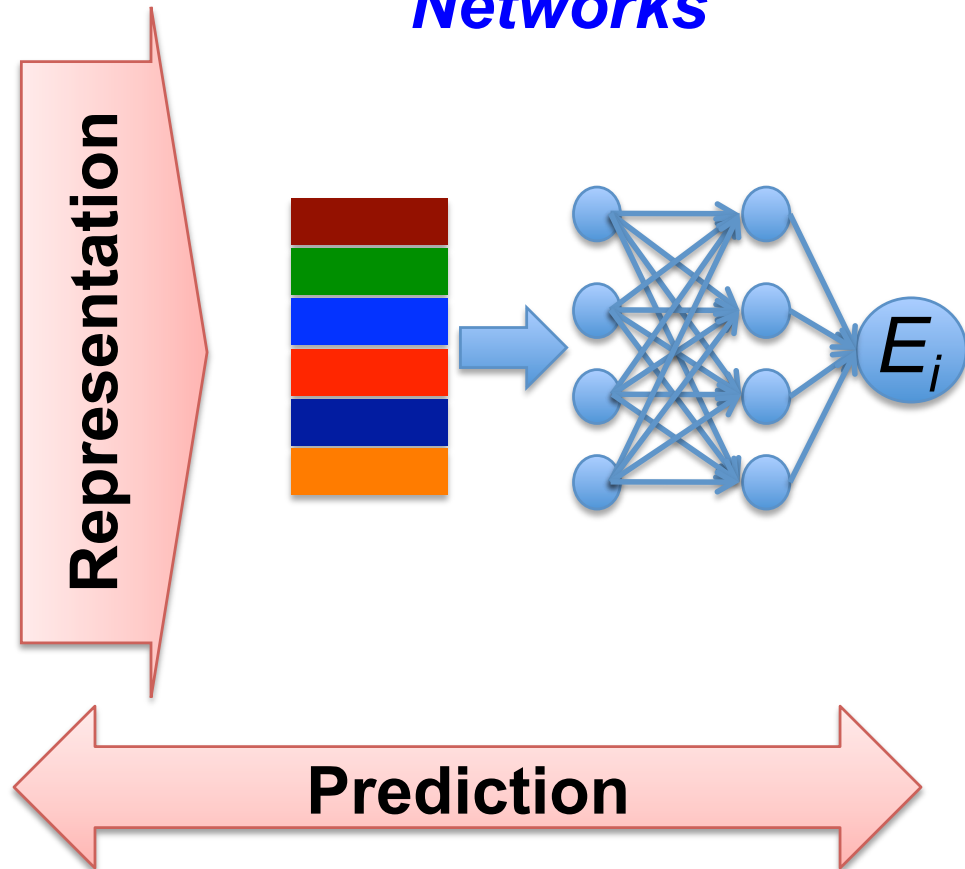
# Representation of Potential Energy Surface of Li-Si

## Lithiation of Amorphous Si



**19000 Structures**  
**SIESTA calculations**

## Implanted Neural Networks



**Ref:** Berk Onat, Ekin D. Cubuk, Brad D. Malone, and Efthimios Kaxiras,  
**PRB 97, 094106 (2018)**

# Novel Materials Discovery (NOMAD) Lab



The Novel Materials Discovery (NOMAD) Laboratory maintains the largest Repository, for input and output files of all important materials science data, helping to advance the field.

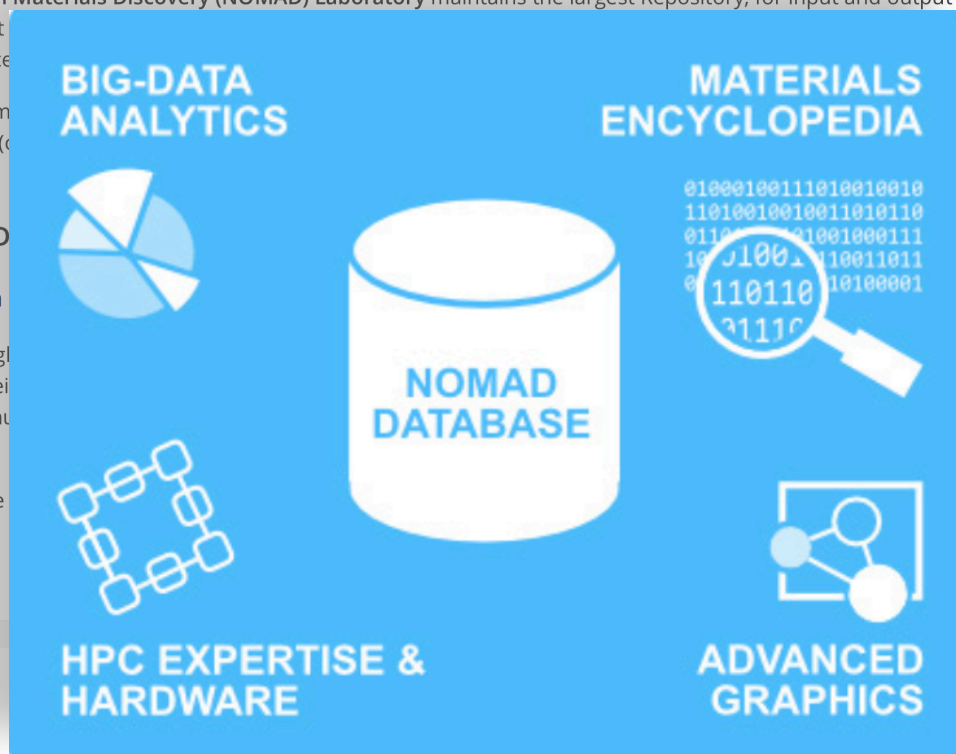
To learn more, visit our YouTube channel.

NOMAD

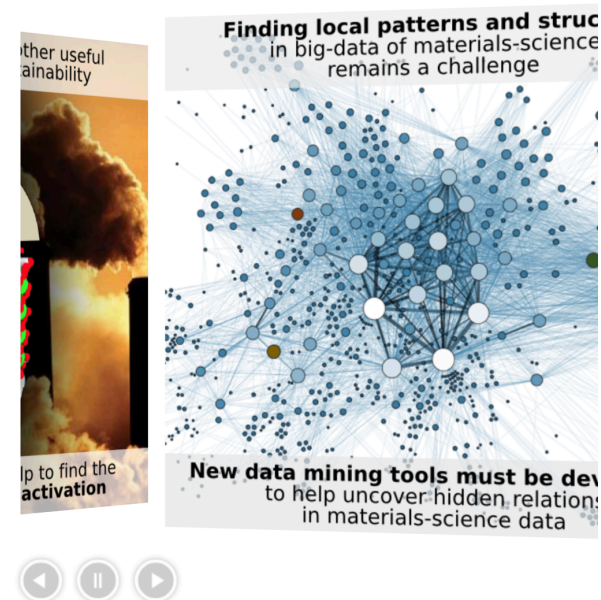
Data is a

Surprising! reason being. Clearly, many results.

This is the ... more



## NOMAD Success Stories



<http://www.nomad-coe.eu>

# Novel Materials Discovery (NOMAD) Lab



The NOMAD Laboratory  
A European Centre of Excellence

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Enter Search...

NOMAD REPOSITORY THE ARCHIVE ENCYCLOPEDIA BIG-DATA ANALYTICS ADVANCED GRAPHICS HPC INFRASTRUCTURE OUTREACH

Metric	Value
Total Energy Calculations	50,236,539
Different Geometries	37,376,432
Bulk Crystals	44,993,132
Surfaces	276,704
Molecules/Clusters	4,605,378
Band Structures	1,936,325

NOMAD Archive as of **March 2018**.

<http://www.nomad-coe.eu>

# Novel Materials Discovery (NOMAD) Lab

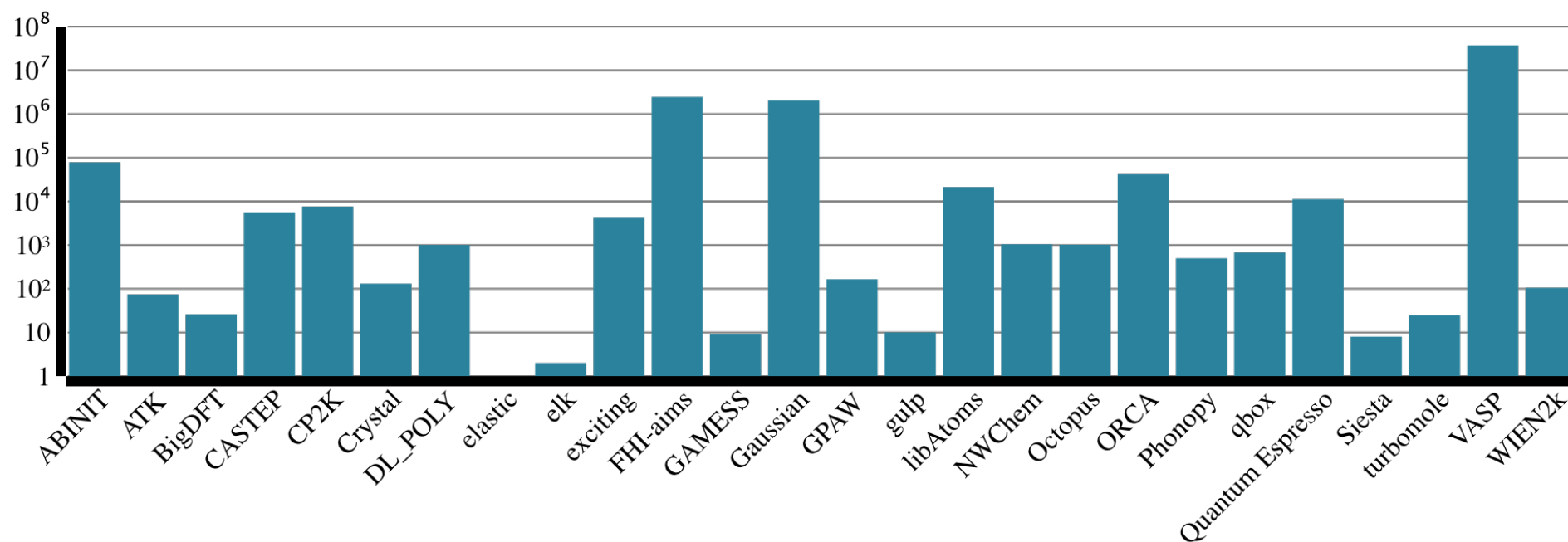


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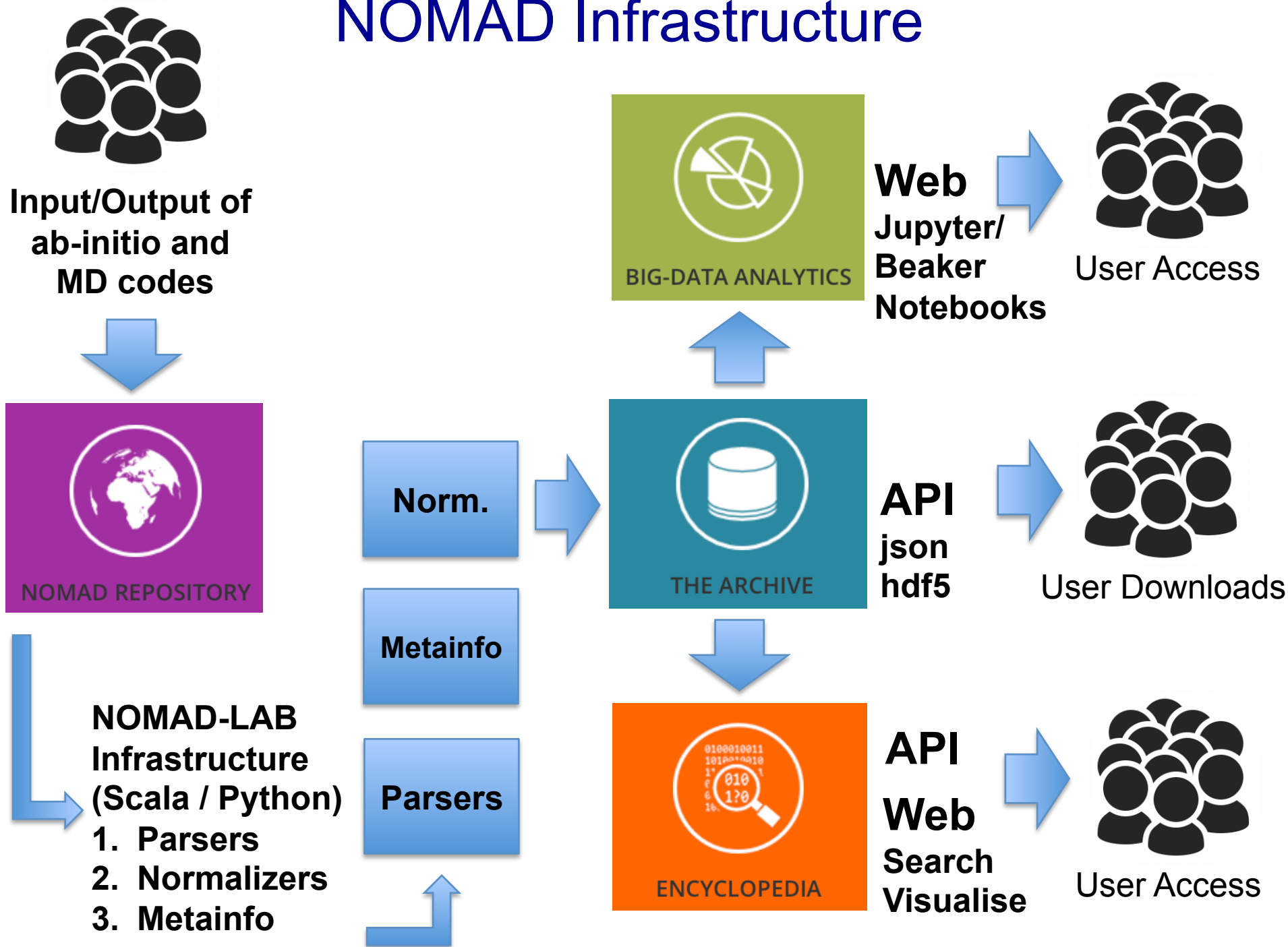
NOMAD REPOSITORY THE ARCHIVE ENCYCLOPEDIA BIG-DATA ANALYTICS ADVANCED GRAPHICS HPC INFRASTRUCTURE OUTREACH



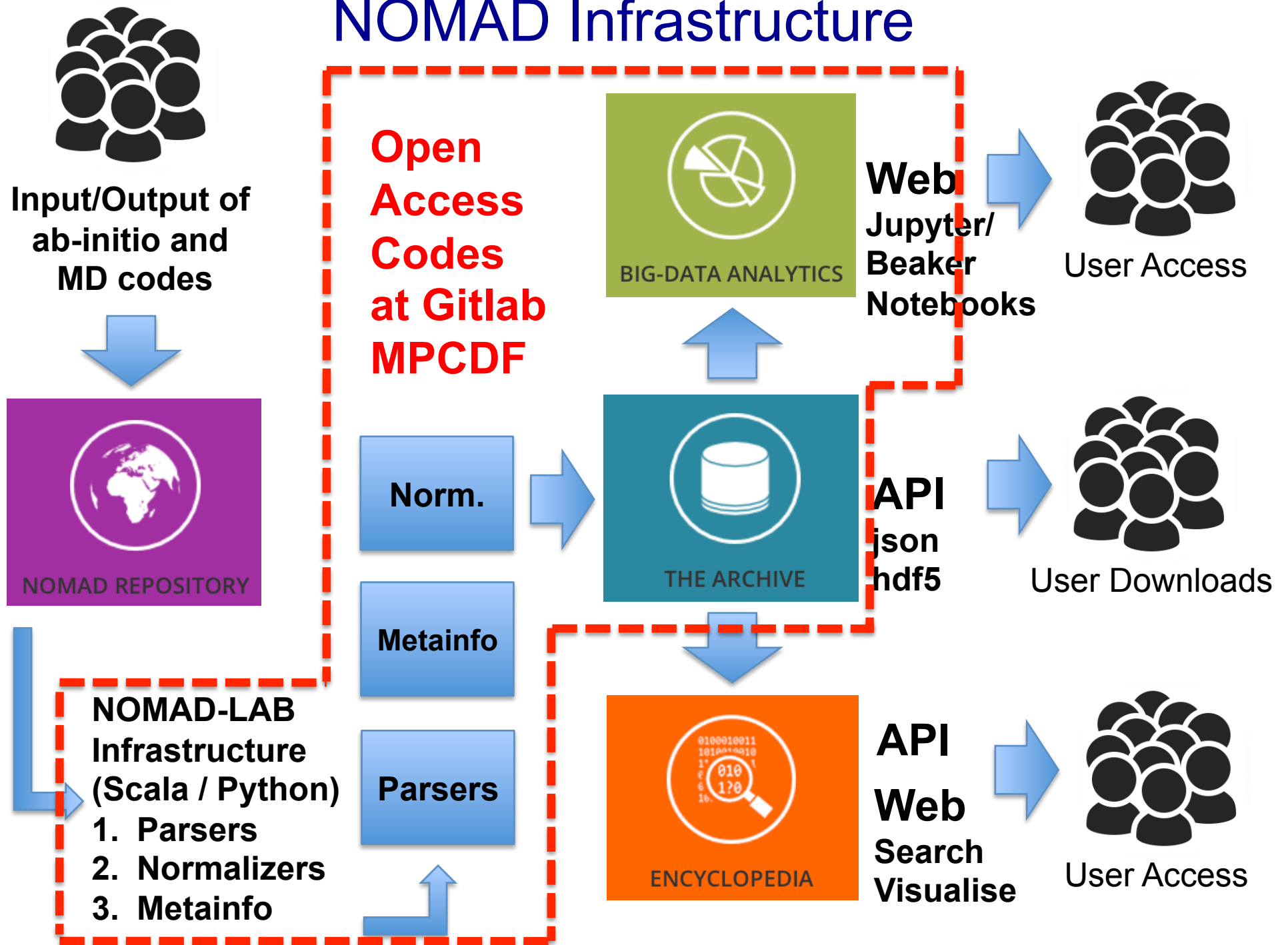
Codes with more than 100 uploads to NOMAD Archive as of **March 2018**.

<http://www.nomad-coe.eu>

# NOMAD Infrastructure



# NOMAD Infrastructure





# NOMAD Parsers

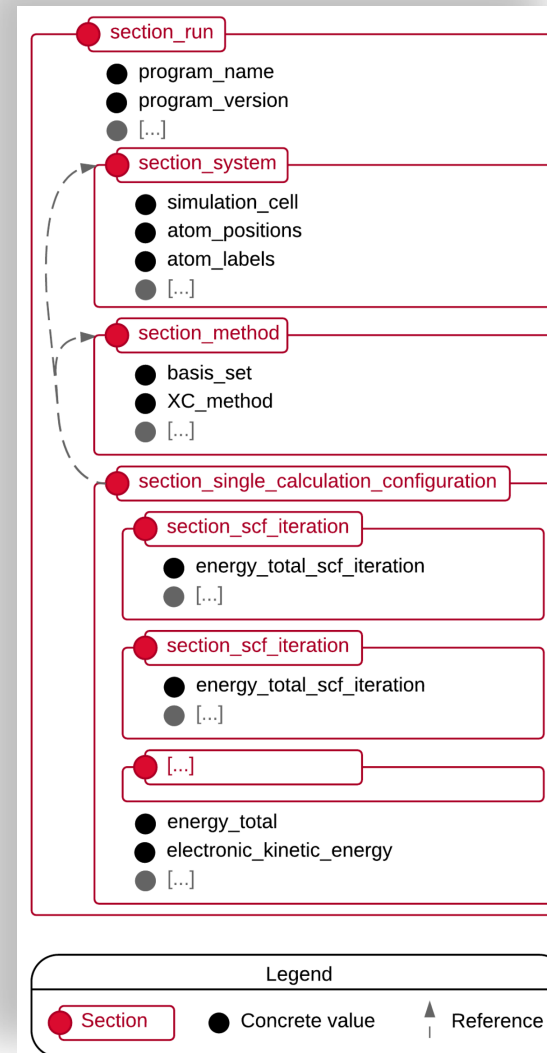
## Most cited 15 codes:

Code	Citations (2013-17)	Type	Search Name
Gaussian	19100	DFT	Frisch
VASP	17900	DFT	Kresse
Gromacs	11200	FF	Lindahl
LAMMPS	10300	FF	Plimpton
Amber	9440	FF	Kollman
NAMD	7110	FF	Schulten
GROMOS	7080	FF	Van Gunsteren
Quantum Espresso	6960	DFT	Giannozzi
ASE/ASAP	6650	FF	Jacobsen
CHARMM	6250	FF	Karplus
Discovery Studio	6240	DFT, FF	Accelrys
GAMESS	5780	DFT	Gordon
WIEN2k	5570	DFT	Blaha
CASTEP	5330	DFT	Payne
Molpro	4440	DFT	Werner

 Parser codes developed in our group.

 Parsers from other groups in NOMAD.

## Standard Metadata



Ref: L.M. Ghiringhelli, C. Carbogno, S. Levchenko, F. Mohamed, G. Huhs, M. Lueders, M. Oliveira, M. Scheffler, arXiv:1607.04738

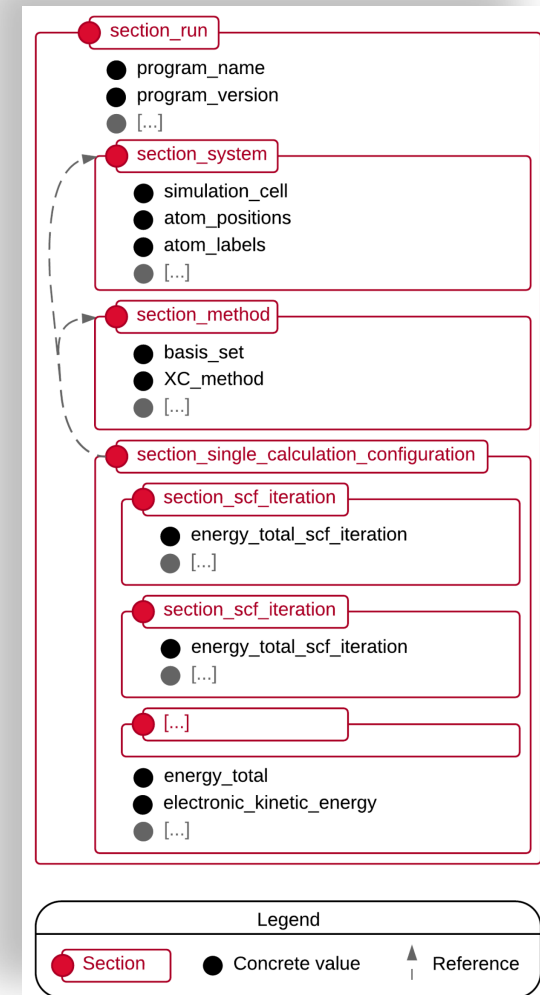
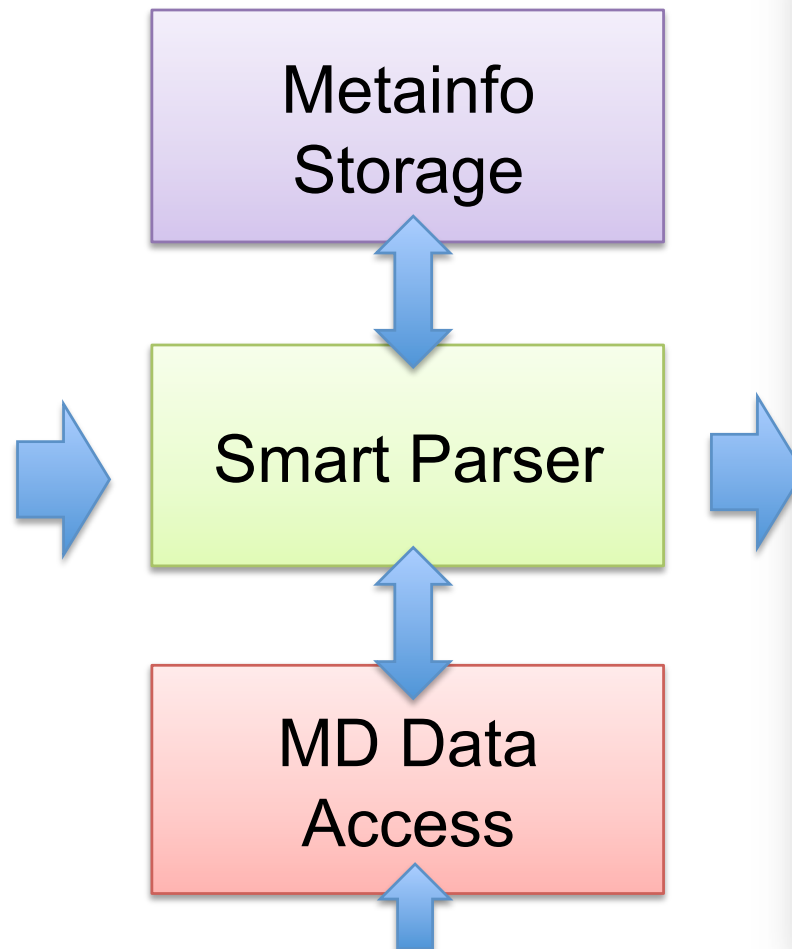


# Metainfo for MD Codes

<https://gitlab.mpcdf.mpg.de/nomad-lab/python-common>

<https://gitlab.mpcdf.mpg.de/nomad-lab/pymolfile>

Amber  
CHARMM  
Gromacs  
GROMOS  
NAMD  
Tinker



Supports **128**

Topology/Trajectory :  
Formats

**ASE**, Mdtraj, MdAnalysis, **ParmEd**,  
**GROMOSTopo**, **CHARMM\_Reader**,  
**Pymolfile** (VMD plugins)

# NOMAD Encyclopedia



Clear all Search

*If your material should not contain other elements, activate "Exclusive search".*

Exclusive search

Element Formula/Material Properties AND OR NOT ( )

*Once all your search criteria are added, execute your search by clicking on the search button.*

H 1																	He 2	
Li 3	Be 4											B 5	C 6	N 7	O 8	F 9	Ne 10	
Na 11	Mg 12											Al 13	Si 14	P 15	S 16	Cl 17	Ar 18	
K 19	Ca 20	Sc 21	Ti 22	V 23	Cr 24	Mn 25	Fe 26	Co 27	Ni 28	Cu 29	Zn 30	Ga 31	<b>Ge 32</b>	As 33	Se 34	Br 35	Kr 36	
Rb 37	Sr 38	Y 39	Zr 40	Nb 41	Mo 42	Tc 43	Ru 44	Rh 45	Pd 46	Ag 47	Cd 48	In 49	Sn 50	Sb 51	Te 52	I 53	Xe 54	
Cs 55	Ba 56			Hf 72	Ta 73	W 74	Re 75	Os 76	Ir 77	Pt 78	Au 79	Hg 80	Tl 81	Pb 82	Bi 83	Po 84	At 85	Rn 86
Fr 87	Ra 88																	
Lanthanoids																		
La 57	Ce 58	Pr 59	Nd 60	Pm 61	Sm 62	Eu 63	Gd 64	Tb 65	Dy 66	Ho 67	Er 68	Tm 69	Yb 70	Lu 71				
Actinoids																		
Ac 89	Th 90	Pa 91	U 92	Np 93	Pu 94	Am 95	Cm 96	Bk 97	Cf 98	Es 99	Fm 100	Md 101	No 102	Lr 103				

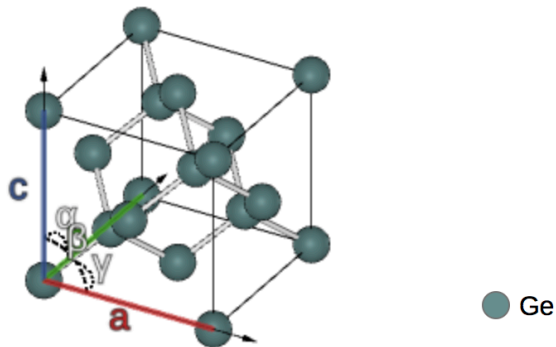
*Add chemical elements to your query.*

- Alkali metals
- Alkaline earth metals
- Transition metals
- Post-transition metals
- Metalloids
- Other nonmetals
- Halogens
- Noble gases
- Lanthanoids
- Actinoids

# NOMAD Encyclopedia

## Ge - space group 227

### Structure



Show axis

Show bonds



Virtual Reality files

System type: bulk

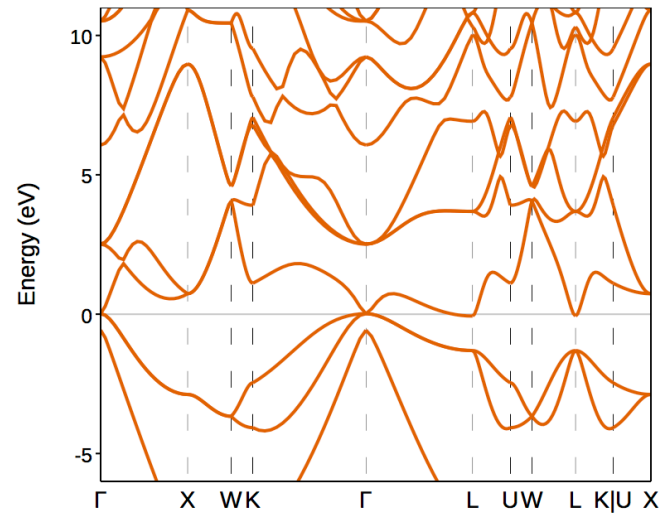
Space group: 227 (Fd-3m)

Structure type: diamond

### Electronic structure

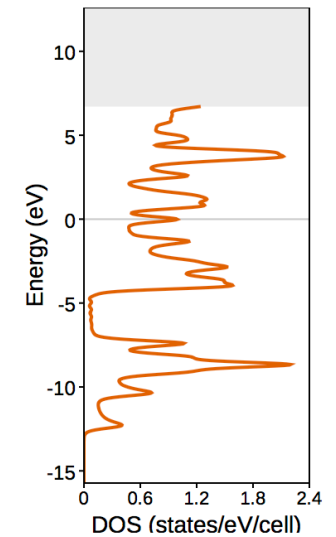


#### Band structure



From calculation 26048  
(GGA - VASP)

#### DOS

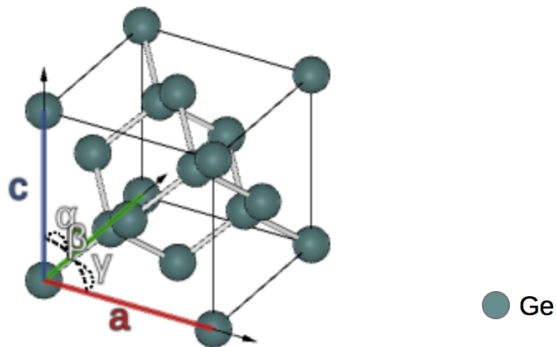


From calculation 26048  
(GGA - VASP)

# NOMAD Encyclopedia

## Ge - space group 227

### Structure +



Show axis  Show bonds  Virtual Reality files

System type: bulk

Space group: 227 (Fd-3m)

Structure type: diamond

### Methodology +

#### Available calculations

##### Functional

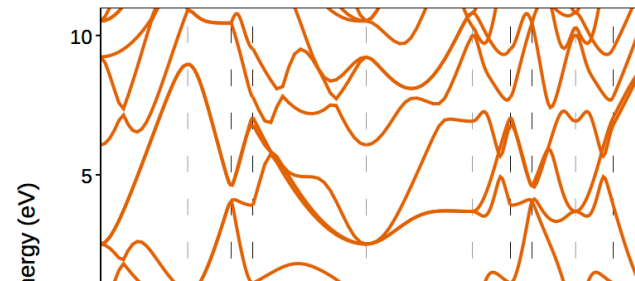
431 LDA  
518 GGA

##### Code

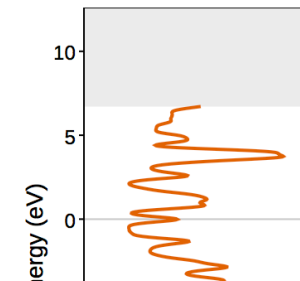
620 FHI-aims  
230 VASP  
78 GPAW  
21 exciting

### Electronic structure +

#### Band structure

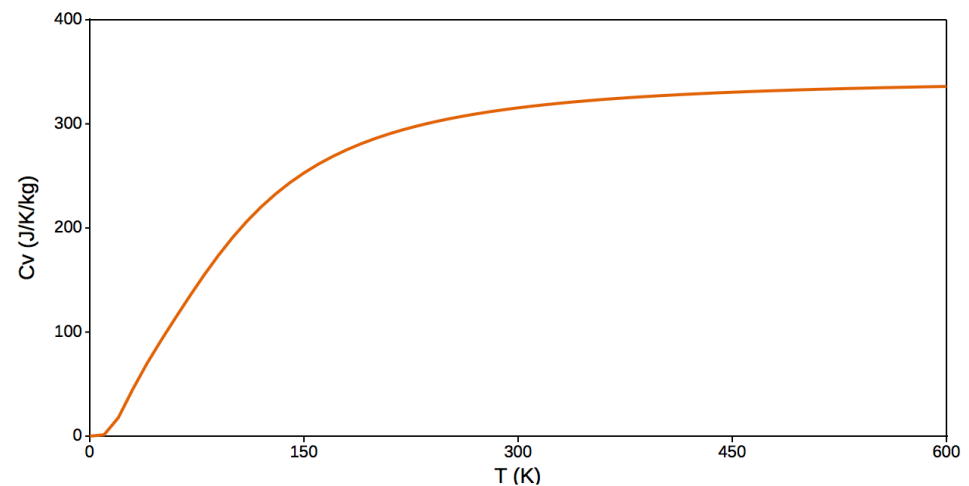


#### DOS



### Vibrational and thermal properties +

#### Specific heat



From calculation 1478973 (LDA - FHI-aims)

# NOMAD Big-Data Analytics & Query



The NOMAD Laboratory  
A European Centre of Excellence



BIG-DATA ANALYTICS

[PROJECT](#) [INDUSTRY](#) [TEAM](#) [RELATED PROJECTS](#) [NEWS](#) [PRESS KIT](#) [CONTACT US](#)

[INTRODUCTION TO BIG-DATA ANALYTICS](#) [ANALYTICS TOOLKIT FORUM](#) [ANALYTICS TOOLKIT](#) [LOGIN](#) [DASHBOARD](#) [TERMS](#)

## BIG-DATA ANALYTICS

We develop and implement methods that identify correlations and structure in big data of materials. This will enable scientists and engineers to decide which materials are useful for specific applications or which new materials should be the focus of future studies.

Despite the huge number of possible materials (e.g. GaAs, Al<sub>2</sub>O<sub>3</sub>, etc.), we note that “the chemical compound space” is sparsely populated when the focus is on selected properties or functions (e.g. structure: rock salt vs. zinkblende, electrical conductivity, etc.). NOMAD offers big-data analytics tools that will help to sort all of the available materials data to identify trends and anomalies. For more information click the “INTRODUCTION TO” button above.

The following tutorials are designed to get started with the Analytics Toolkit (click title to show/hide details of the selected tutorial):

### Archive Query

[Querying and visualizing the content of the NOMAD Archive](#)

### Atomic properties

[A periodic table of elements for atomic data collections](#)

### Crystal structure prediction

[On-the-fly data analysis for the NOMAD Archive](#)

[Predicting energy differences between crystal structures](#)

[Tutorial on compressed sensing for materials property prediction](#)

[Discovering simple descriptors for crystal-structure classification](#)

Learn about the results of the NOMAD competition

Filter:

show featured only

Author:

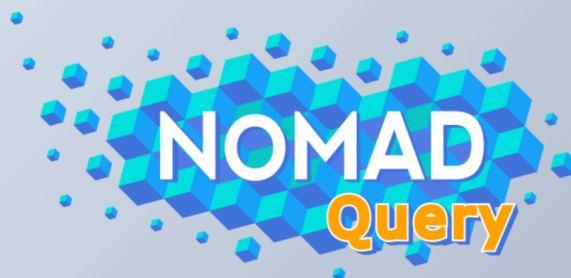
Method:

Keywords:

text filter:

Results according to filter: 16

# NOMAD Big-Data Archive and Query



atom\_species = C H O N + Add - Delete

AND

Enter your query ... + Add - Delete

**calculation\_uploader\_name**  
Name of the uploader of this calculation, given as <first\_name last\_name>

**crystal\_system**  
Name of the crystal system. Can be one of the following: triclinic, monoclinic, orthorhombic, tetragonal, trigonal, hexagonal or cubic.

**electronic\_structure\_method**  
String identifying (one of) the electronic structure method used in the calculation.

## Results

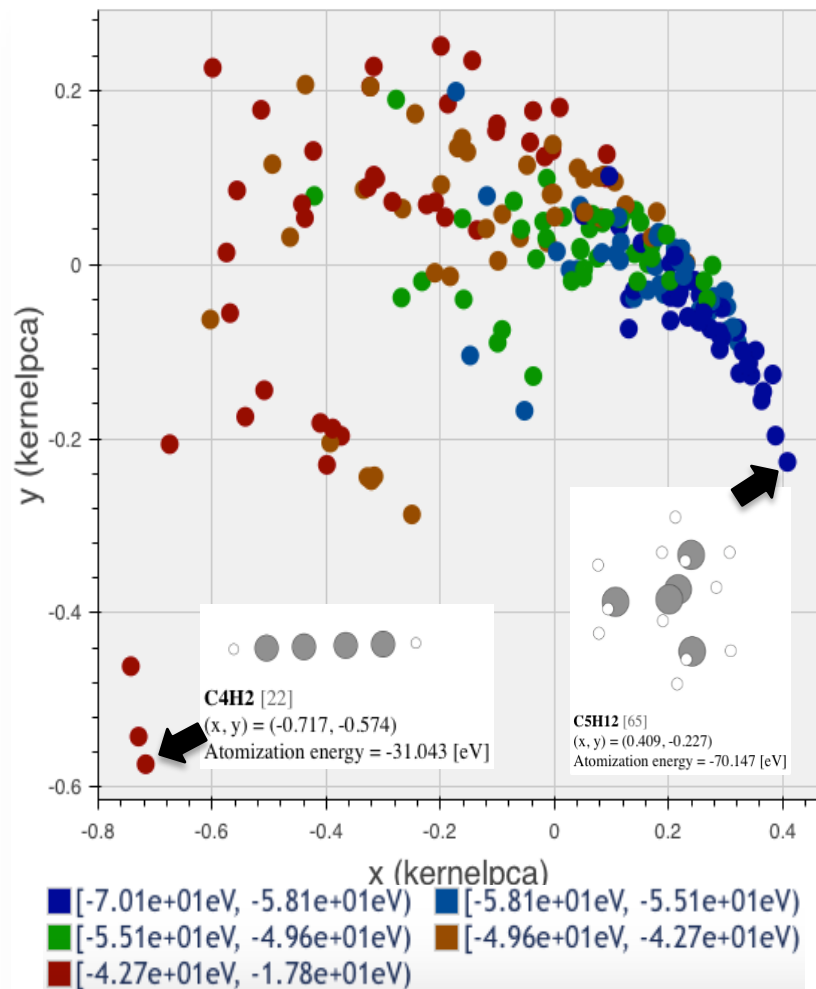
About 2,676,000 results (0.20 seconds)

#1 [nmd://N8T2cMu-S78puq5u4gOpcDLxCOYD5/C--0g6U9SJVmCJHn0tUuE5o3Nf\\_o1](#)

[Springer: sd\\_1252879, ...](#)

<b>Program Name:</b>	Gaussian	<b>Chemical Formula:</b>	O <sub>2</sub>
<b>Atom Symbols:</b>	O	<b>XC Functional Name:</b>	HYB_GGA_XC_HSE06
<b>Basis Set Type:</b>	gaussians	<b>System Composition:</b>	O <sub>2</sub>
<b>System Reweighted Composition:</b>	O <sub>100</sub>	<b>System Type:</b>	Molecule / Cluster

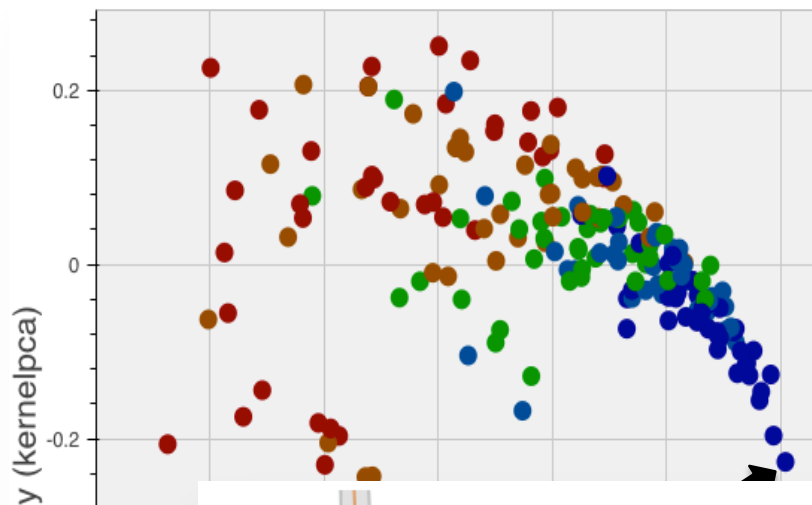
# Similarity Map with SOAP Representation



[1] C. Poelking, A. Ziletti, L. Ghiringhelli, and G. Csányi, NOMAD. S. De, A. Bartók, G. Csányi, and M. Ceriotti, Phys. Chem. Chem. Phys. (2016)



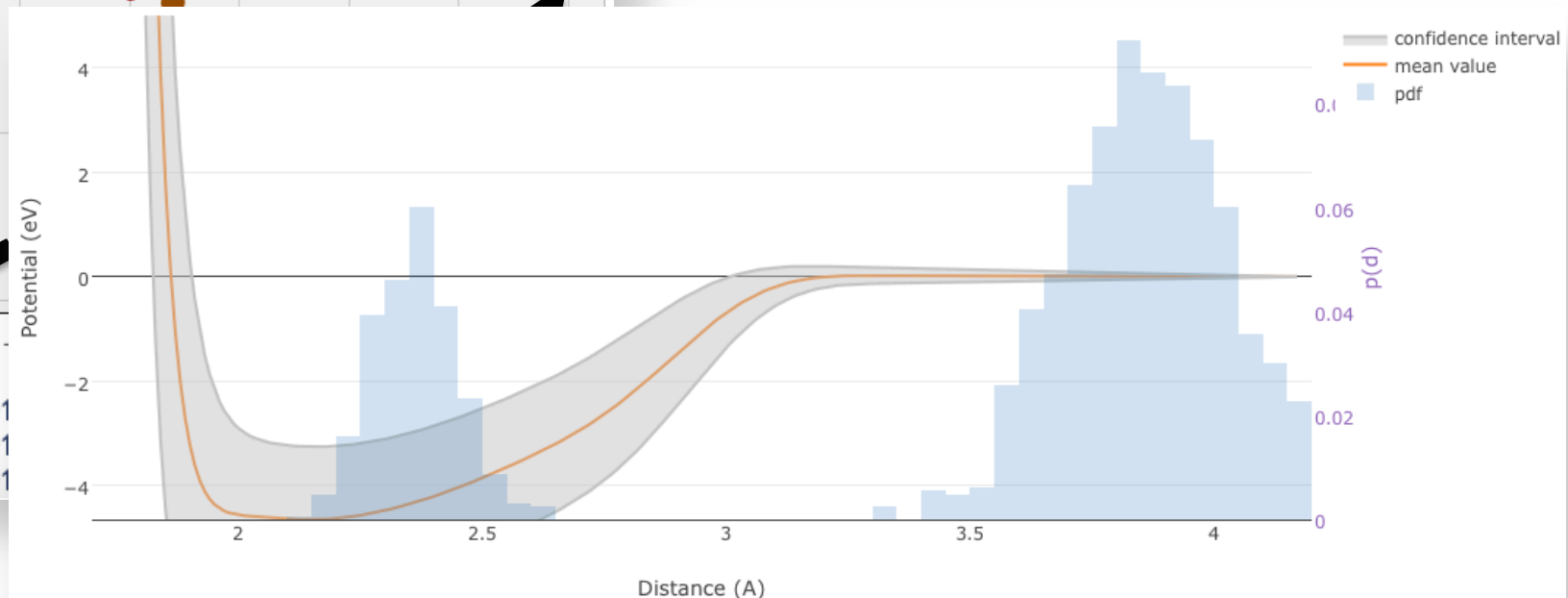
# Similarity Map with SOAP Representation



■ [-7.01e+01  
■ [-5.51e+01  
■ [-4.27e+01

- [1] C. Poelking, A. Ziletti, L. Ghiringhelli, and G. Csányi, NOMAD. S. De, A. Bartók, G. Csányi, and M. Ceriotti, Phys. Chem. Chem. Phys. (2016)
- [2] Ádám Fekete, Aldo Glielmo, Martina Stella, and Alessandro De Vita, NOMAD Big-Data Analytics

## Pair-Potential Predictor for Si



# Classification of Representations

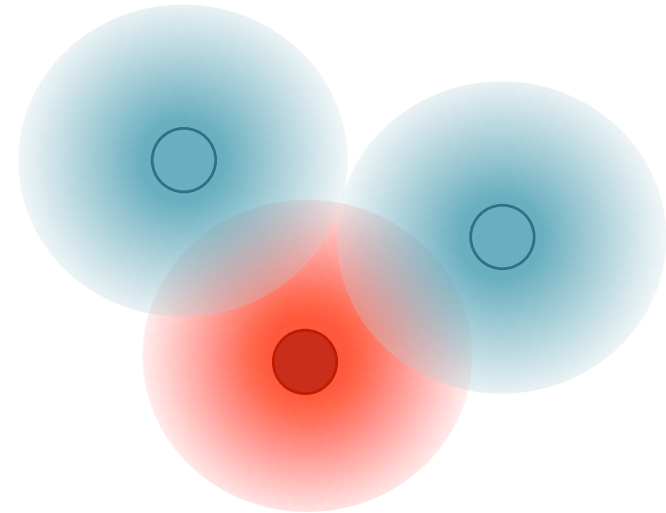
Atomic neighbor density		Histogram			Connectivity (Graphs)		Physical Property
Symmetry Adapted		Direct	Direct		Direct		Direct
Kernel/ Power expansion	Functions/ Filters	Expansion/Tensor	Structure	Electronic	Static Builds	Hierarchical Builds	Combination of any property with any math. operation
SOAP	Sym. Funcs, Chebyshev expansion, AGNI	MBTR	k-bags, Bag of Bonds/ Angles ...	Electronic Band Structure, DOS	n-gram, Graphs, CGCNN, Coulomb Matrix	Building blocks or Ligand/ Residue based Graphs	SISSO

**Ref:** Berk Onat, James Kermode (2018) *under preparation*

# Smooth Overlap of Atomic Positions (SOAP)

$$\rho_{\mathcal{X}}(\mathbf{r}) = \sum_{i \in \mathcal{X}} \exp\left(-\frac{(\mathbf{x}_i - \mathbf{r})^2}{2\sigma^2}\right)$$

$$\tilde{k}(\mathcal{X}, \mathcal{X}') = \int d\hat{R} \left| \int \rho_{\mathcal{X}}(\mathbf{r}) \rho_{\mathcal{X}'}(\hat{R}\mathbf{r}) d\mathbf{r} \right|^n$$



## Power Expansion:

$$\rho_{\mathcal{X}}(\mathbf{r}) = \sum_{blm} c_{blm} g_b(|\mathbf{r}|) Y_{lm}(\hat{\mathbf{r}})$$

$$p(\mathcal{X})_{b_1 b_2 l} = \pi \sqrt{\frac{8}{2l+1}} \sum_m (c_{b_1 l m})^\dagger c_{b_2 l m}$$

## SOAP Kernel:

$$k(\mathcal{X}, \mathcal{X}') = \hat{\mathbf{p}}(\mathcal{X}) \cdot \hat{\mathbf{p}}(\mathcal{X}')$$

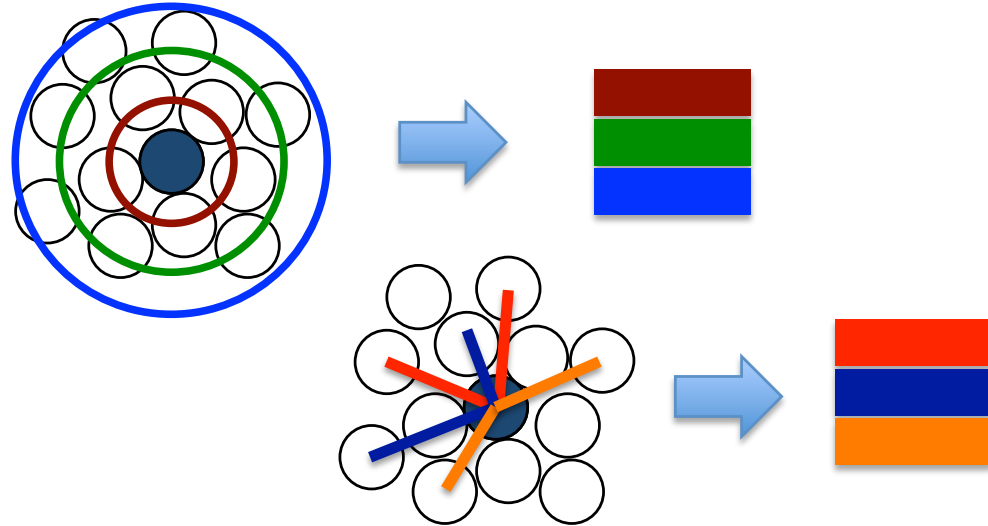
Ref: A. P. Bartok, R. Kondor and G. Csanyi, PRB 87, 184115, (2013)

A. P. Bartok, G. Csanyi, Int. J. Quantum Chemistry 115, 1051–1057, (2015)

# Symmetry Functions

## Radial Symmetry Functions:

$$G_2^i = \sum_j e^{-\eta(R_{ij}-R_s)^2} \cdot f_c(R_{ij}),$$

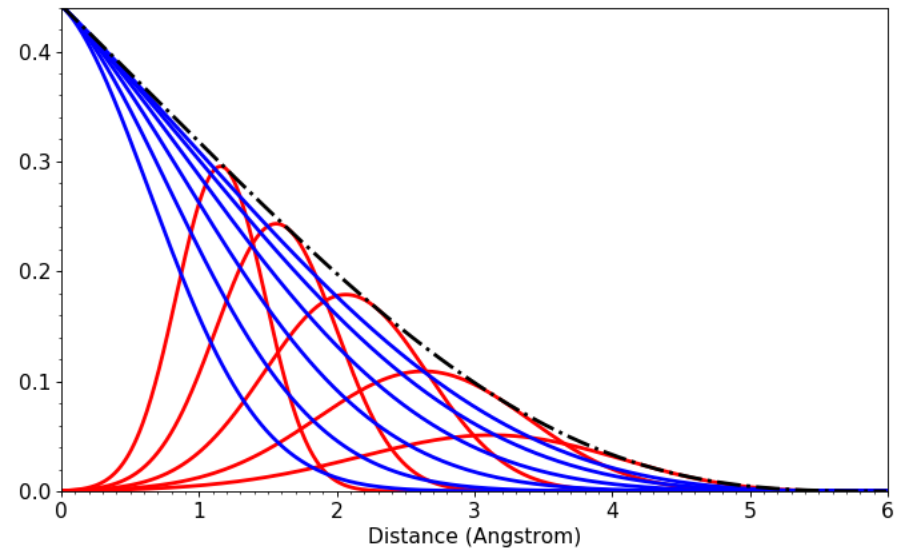


## Angular Symmetry Functions:

$$G_3^i = 2^{1-\zeta} \sum_j \sum_{k \neq j} (1 + \lambda \cdot \cos \theta_{ijk})^\zeta \cdot e^{-\eta(R_{ij}^2 + R_{ik}^2 + R_{jk}^2)} \cdot f_c(R_{ij})f_c(R_{ik})f_c(R_{jk}),$$

## Cutoff function:

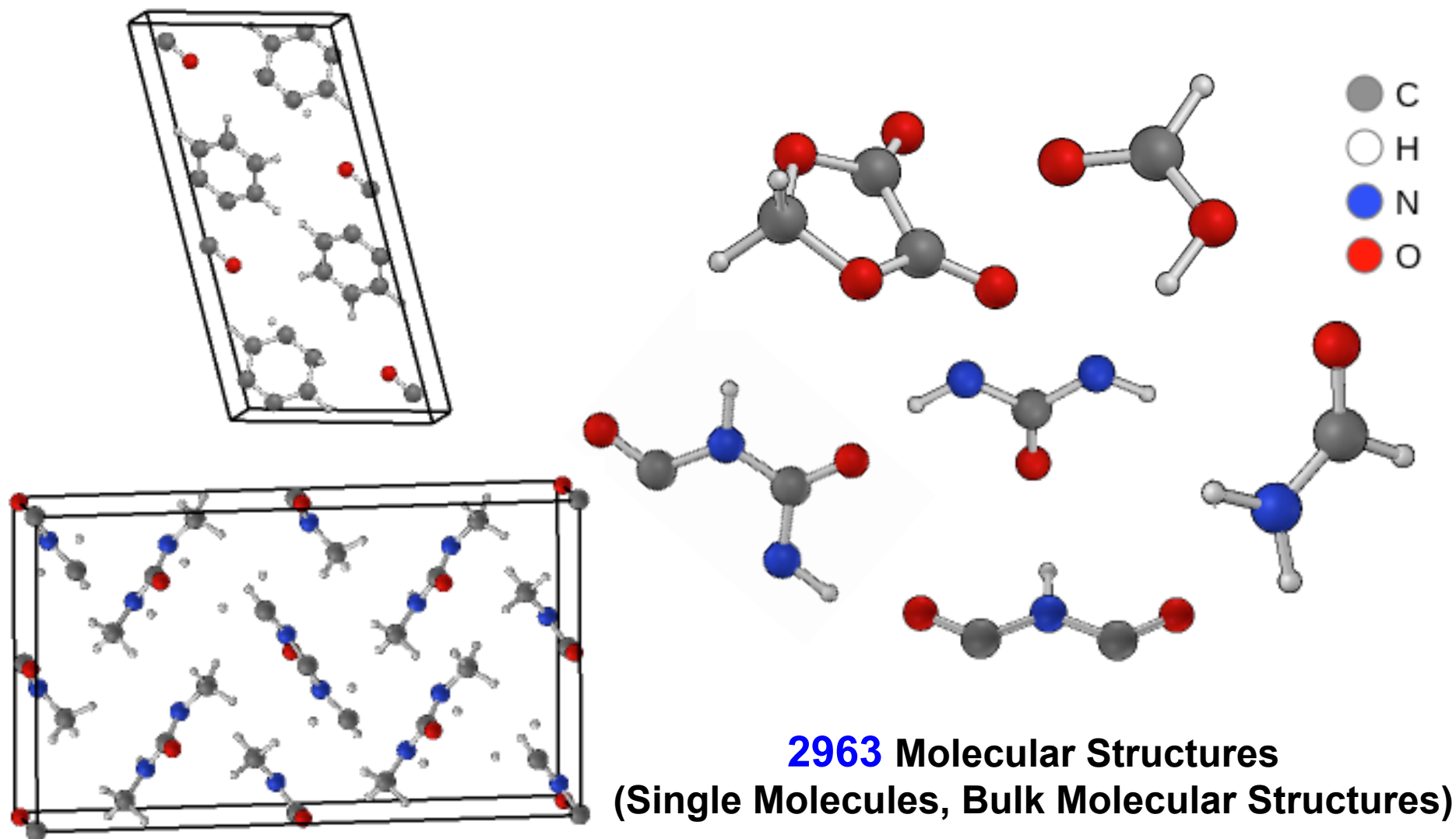
$$f_c(R_{ij}) = \begin{cases} \tanh^3 \left[ 1 - \frac{R_{ij}}{r_c} \right] & \text{for } R_{ij} \leq r_c \\ 0.0 & \text{for } R_{ij} > r_c \end{cases}$$



Ref: N. Artrith, B. Hiller and J. Behler, *Physica Status Solidi B*, 250, 1191 (2013)

G. Imbalzano, A. Anelli, D. Giofré, S. Klees, J. Behler, M. Ceriotti, *J Chem. Phys* 148, 241730 (2018)

# Compressibility Tests with CUR and FPS Methods on C,H,N,O Structures



# CUR Decomposition

$$\mathbf{X} \approx \tilde{\mathbf{X}} = \mathbf{C} \mathbf{U} \mathbf{R},$$

## Selecting Columns of X:

- 1) SVD Decomposition
- 2) Column scoring with right singular vector  $\mathbf{v}$

$$\pi_c = \sum_{j=1}^k (v_c^{(j)})^2,$$

- 3) Select  $\mathbf{c}$  from  $k$  columns (Here we apply CUR[k=1])
- 4) Orthogonalize all other columns of  $\mathbf{X}$  to  $\mathbf{c}$

$$\mathbf{R} = \mathbf{X},$$

$$\mathbf{U} = \mathbf{C}^+ \mathbf{X} \mathbf{X}^+,$$

## Error estimation:

$$\epsilon = \|\mathbf{X} - \mathbf{C} \mathbf{U} \mathbf{R}\|_F / \|\mathbf{X}\|_F$$

# Farthest Point Sampling (FPS)

## Selecting Columns of X:

- 1) Select first column randomly
- 2) Select  $N$  columns according to

$$k = \operatorname{argmax}(\min_j |X_k - X_j|),$$

- 3) Build  $C$  matrix using the selected columns

$$\mathbf{R} = \mathbf{X},$$
$$\mathbf{U} = \mathbf{C}^+ \mathbf{X} \mathbf{X}^+,$$

## Error estimation:

$$\epsilon = \|\mathbf{X} - \mathbf{CUR}\|_F / \|\mathbf{X}\|_F$$





Horizon 2020

# NOMAD: Novel Materials Discovery

<http://www.nomad-coe.eu>

WARWICK

Dr. Berk Onat  
Research Fellow



*Dr. James R. Kermode*  
Associate Professor



**Warwick Centre of  
Predictive Modelling**

## NOMAD Collaborators

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## Acknowledgement

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This work is supported in part by **NOMAD Project** and **University of Warwick**.

**NOMAD project** has received funding from the **European Union's Horizon 2020** research and innovation programme under grant agreement No. 676580.

