

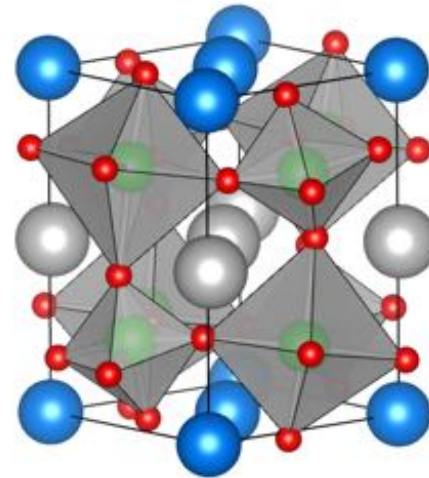
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# First principles design of new multiferroic materials

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*Nick Bristowe*

*Functional Materials Group, University of Kent, UK*



# Ferroelectricity vs ferromagnetism

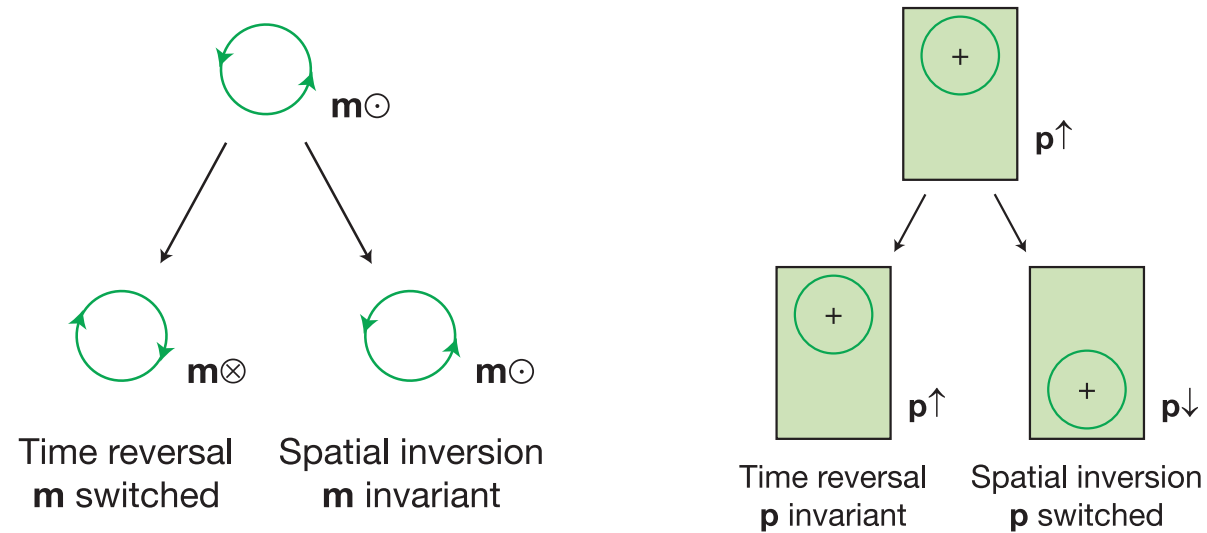
---

Both are types of “ferroics”

**Ferroelectricity** – spontaneous polarization  $\mathbf{P}$  (switchable with an electric field  $\mathbf{E}$ )

**Ferromagnetism** – spontaneous magnetization  $\mathbf{M}$  (switchable with a magnetic field  $\mathbf{H}$ )

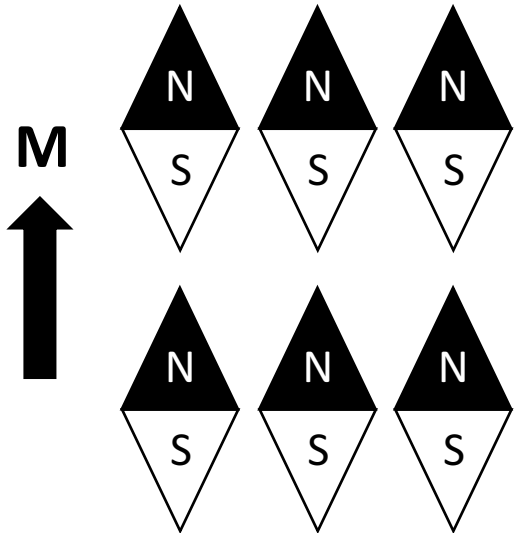
Classed by symmetry:



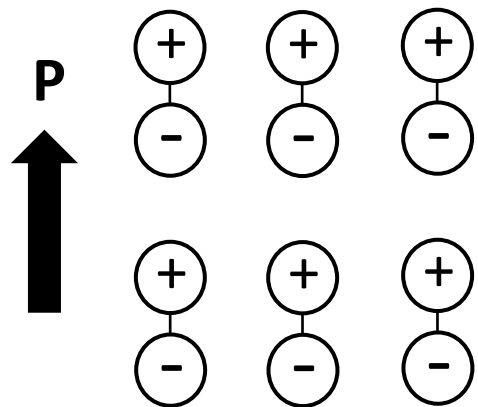
# Multiferroics

Multiferroic: material combining two or more ferroic parameters

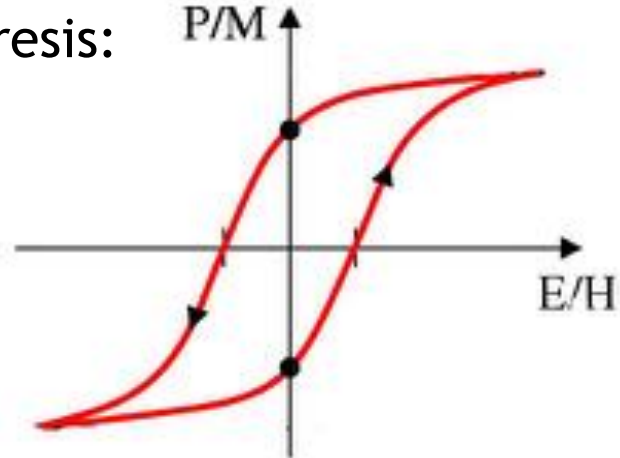
Ferromagnetic:



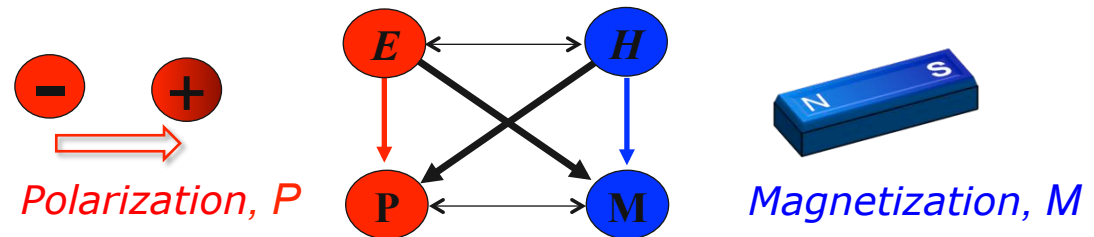
Ferroelectric:



• Hysteresis:



Magnetolectric:



Possible applications:

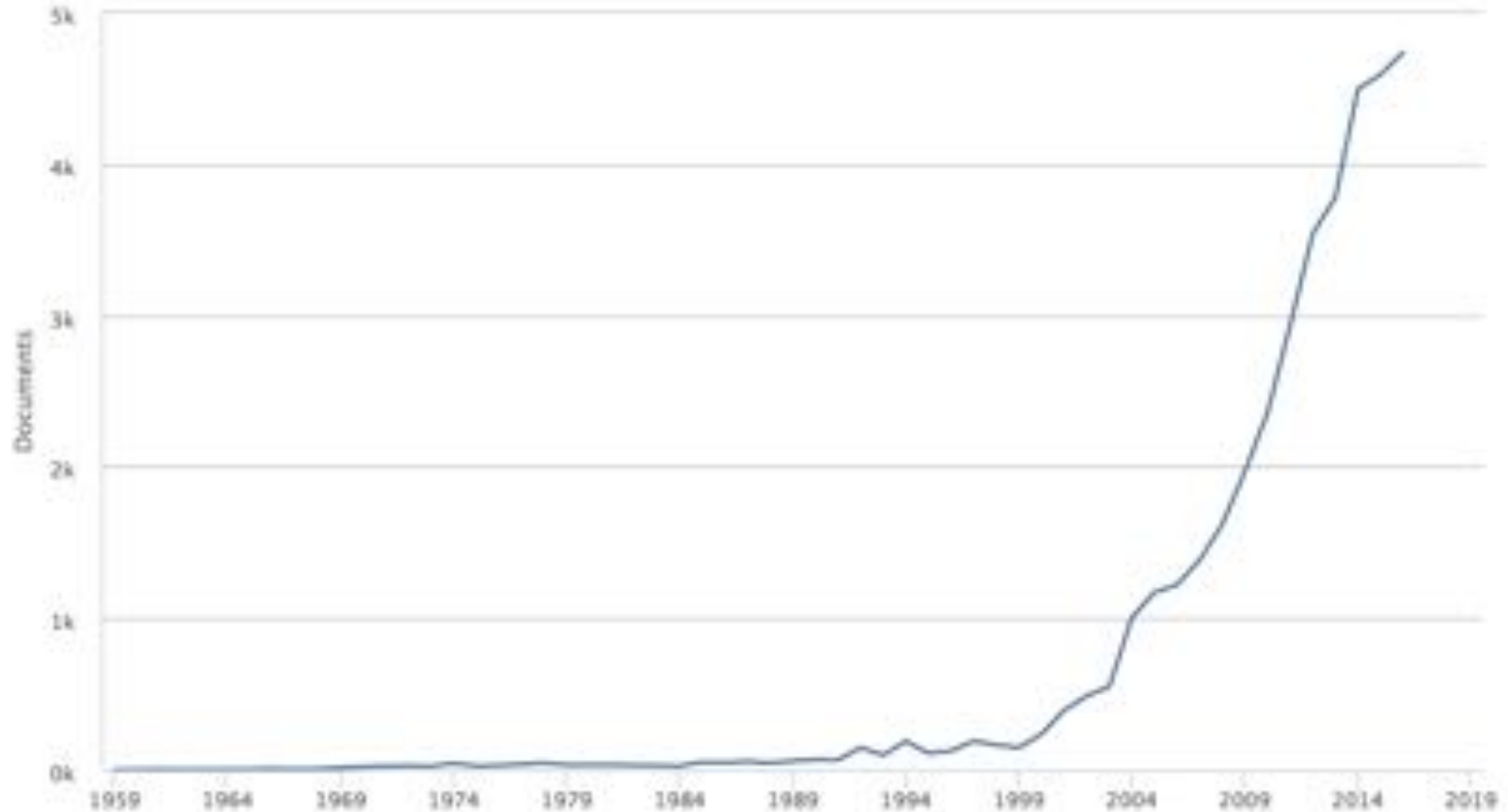
- Magnetolectric RAM: electric write / magnetic read
- 4-state memory

# Research Activity

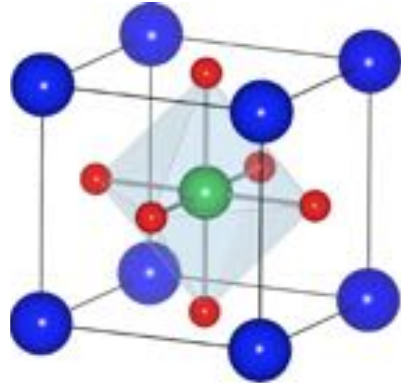
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Scopus result for papers published with “multiferroic” OR “magnetoelectric” mentioned in any field

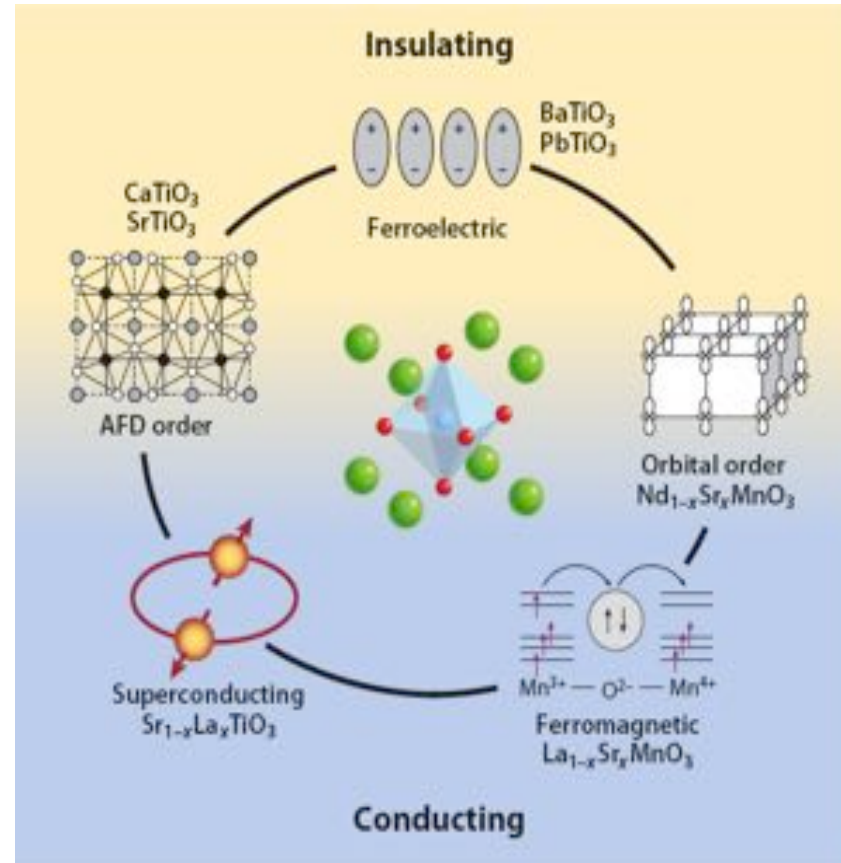
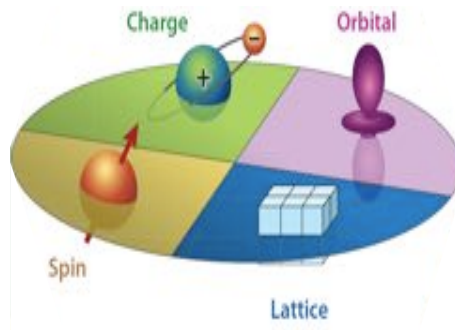
## Documents by year



# Perovskites



Wide range of properties  
Due to coupling degrees of freedom

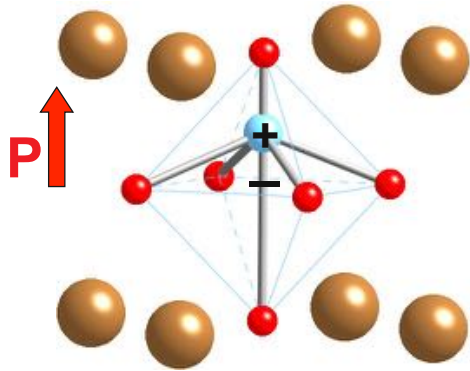


# Why are most perovskites NOT FE?

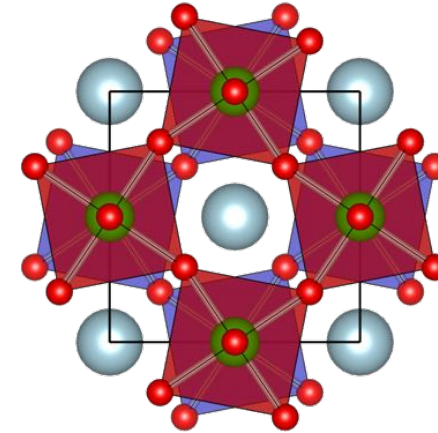
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Pure FE ground state

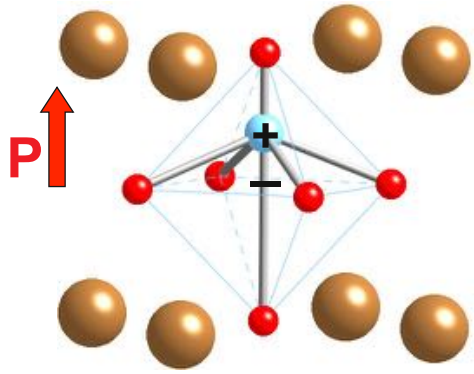


Purely tilted ground state

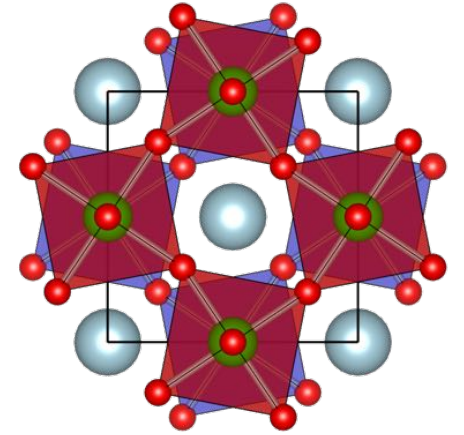


# Why are most perovskites NOT FE?

**PbTiO<sub>3</sub>**  
Pure FE ground state

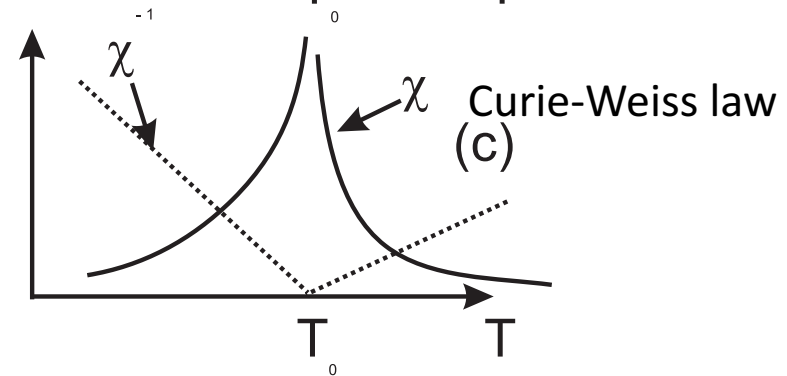
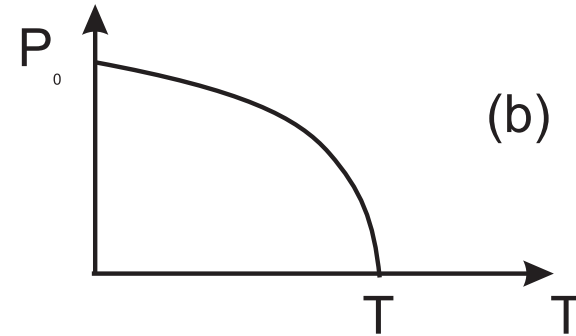
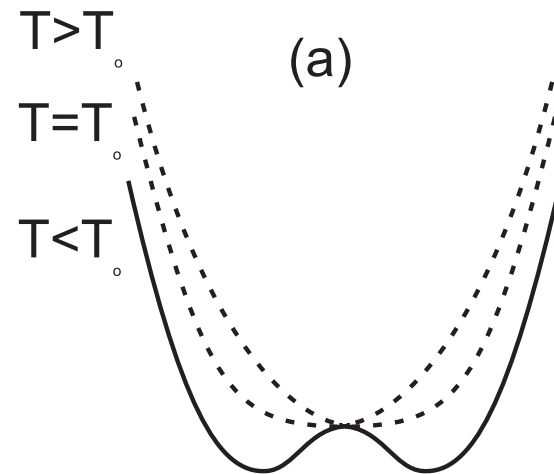


**CaTiO<sub>3</sub>**  
Purely tilted ground state



Proper phase transition (Landau)

$$f(T, P) = a_1 P^2 + a_{11} P^4 \quad a_1 = \alpha(T - T_0)$$

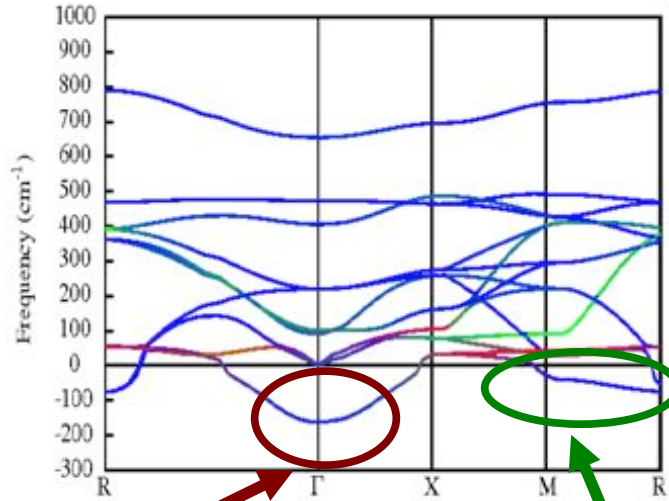


# Why are most perovskites NOT FE?

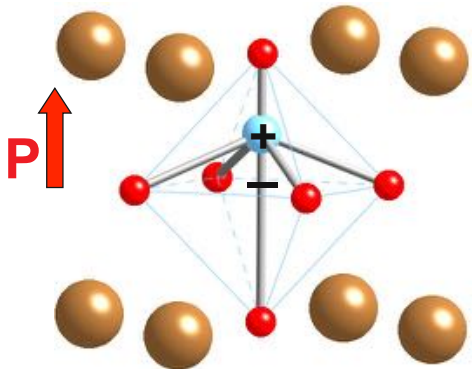
Structural instabilities from simple cubic

**PbTiO<sub>3</sub>**

Pure FE ground state



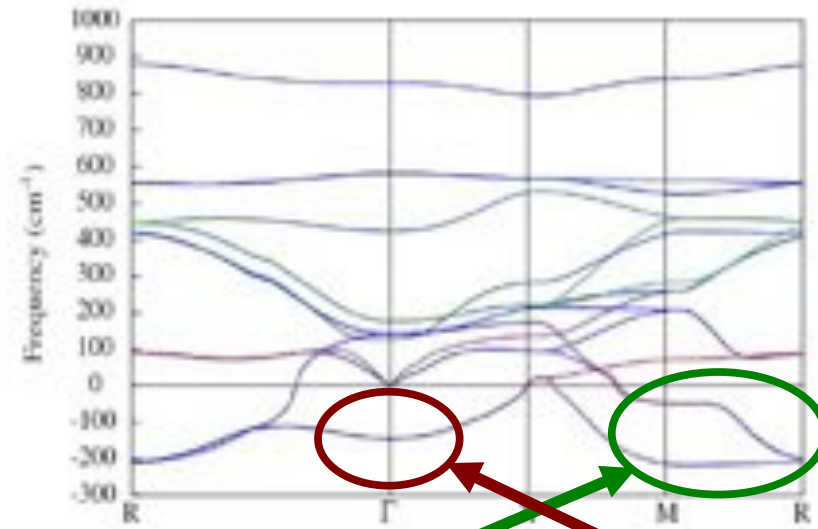
FE (ferroelectric)  
polar distortion



Phonons courtesy of Ph Ghosez

**CaTiO<sub>3</sub>**

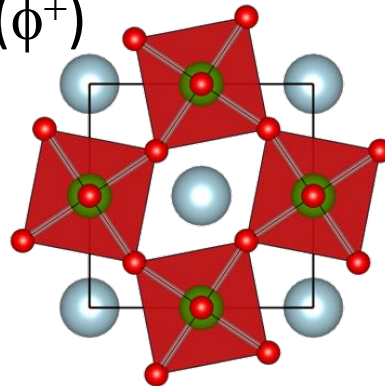
Purely tilted ground state



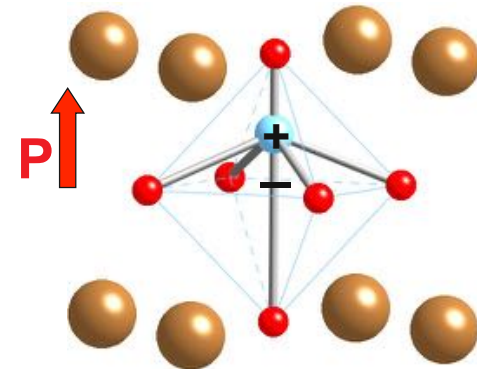
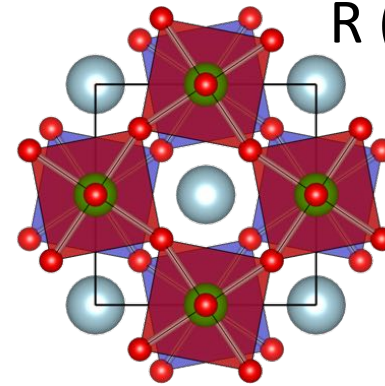
Oxygen Octahedral Tilts

FE (ferroelectric)  
polar distortion

M ( $\phi^+$ )



R ( $\phi^-$ )

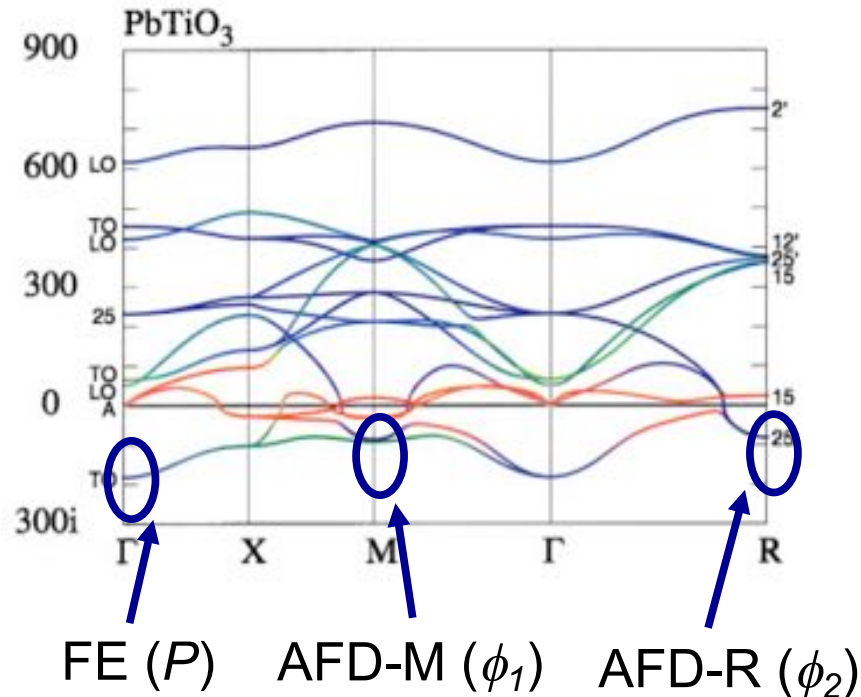




# Why are most perovskites NOT FE?

## Competing FE and AFD lattice instabilities

### Energy landscape



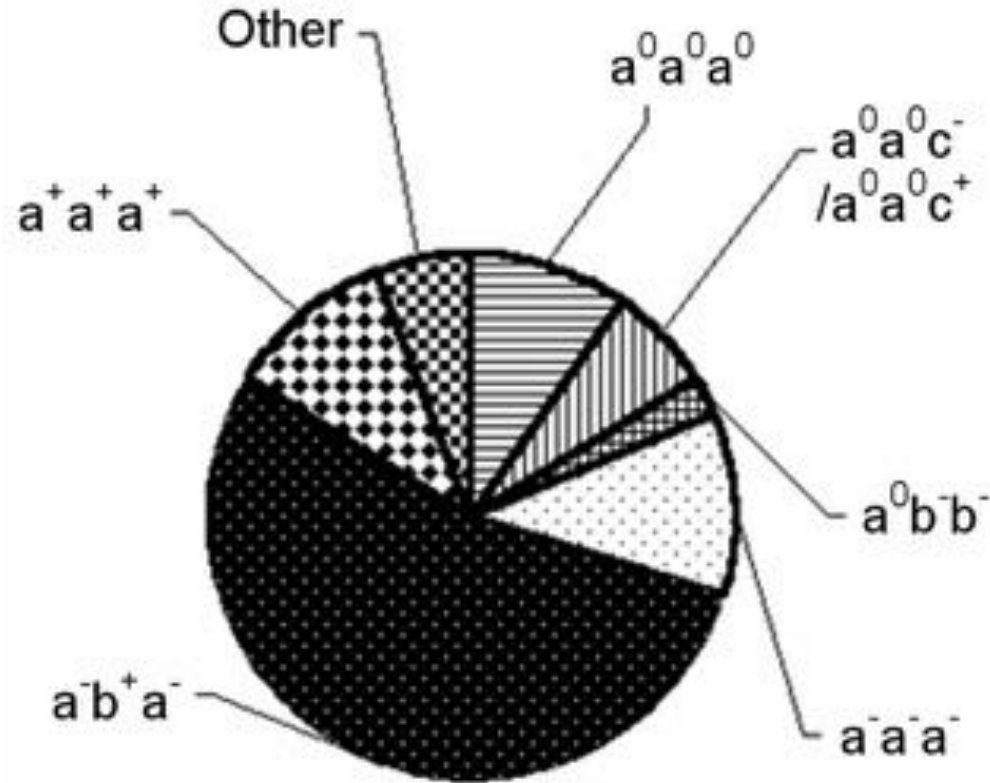
***Tilting often wins!***

$$E = \frac{1}{2} A_0 P^2 + \frac{1}{4} B_0 P^4 + C_{12} \phi_1^2 \phi_2^2$$
$$+ \frac{1}{2} A_1 \phi_1^2 + \frac{1}{4} B_1 \phi_1^4 + C_{01} \phi_1^2 P^2$$
$$+ \frac{1}{2} A_2 \phi_2^2 + \frac{1}{4} B_2 \phi_2^4 + C_{02} \phi_2^2 P^2$$

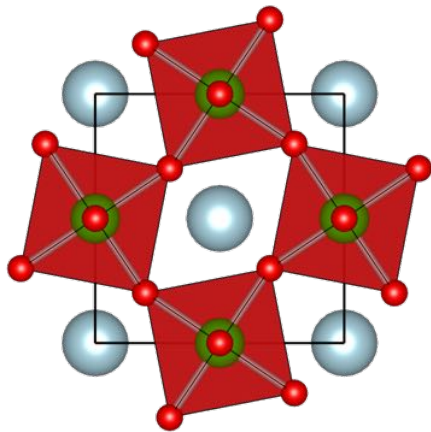
FE and AFD usually competing through bi-quadratic coupling ( $C_{01}, C_{02} > 0$ )

# Why are most perovskites NOT FE?

They often tilt instead

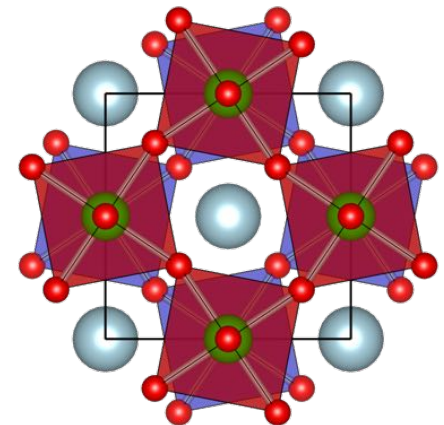


AFD (M-point) :  $\phi^+$



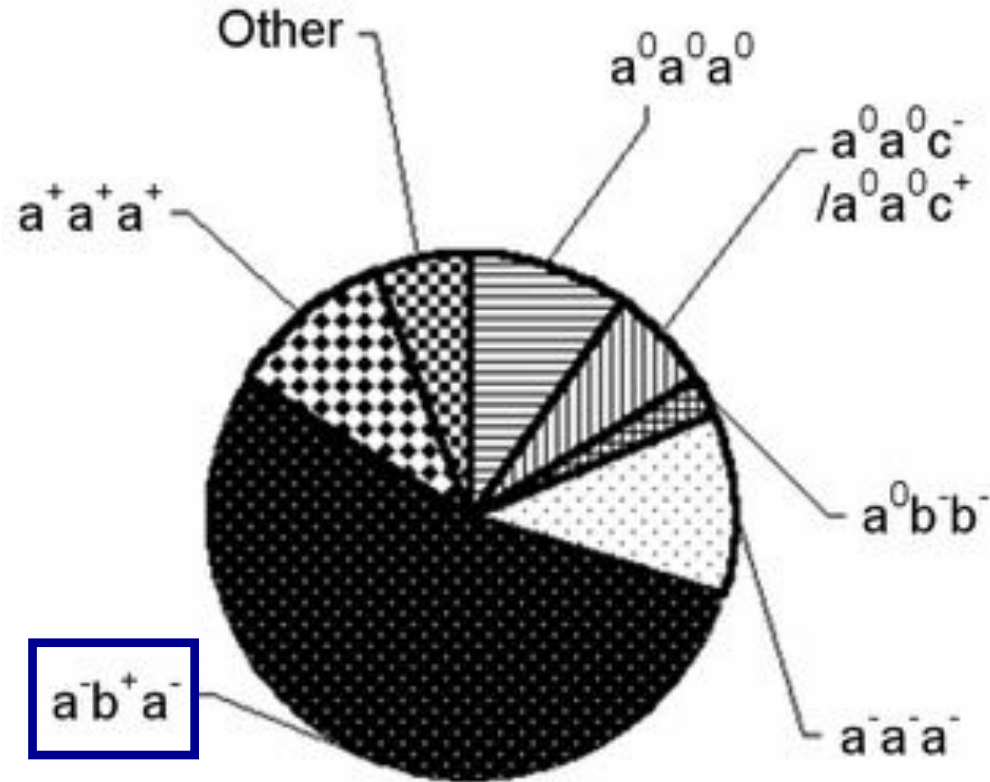
Lufaso and Woodward Acta Cryst. B57 725 (2001)

AFD (R-point) :  $\phi^-$

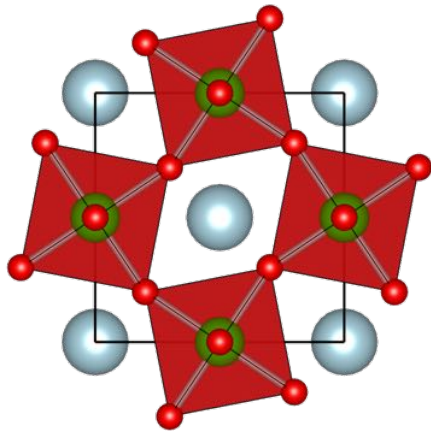


# Why are most perovskites NOT FE?

They often tilt instead



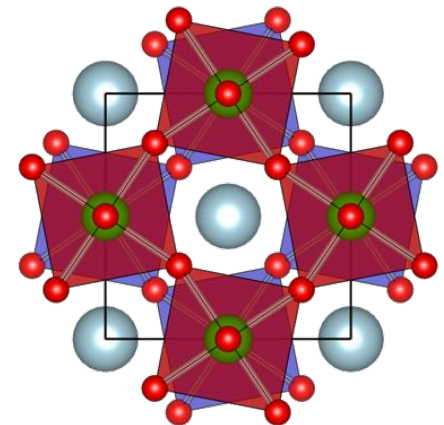
AFD (M-point) :  $\phi^+$



Lufaso and Woodward Acta Cryst. B57 725 (2001)

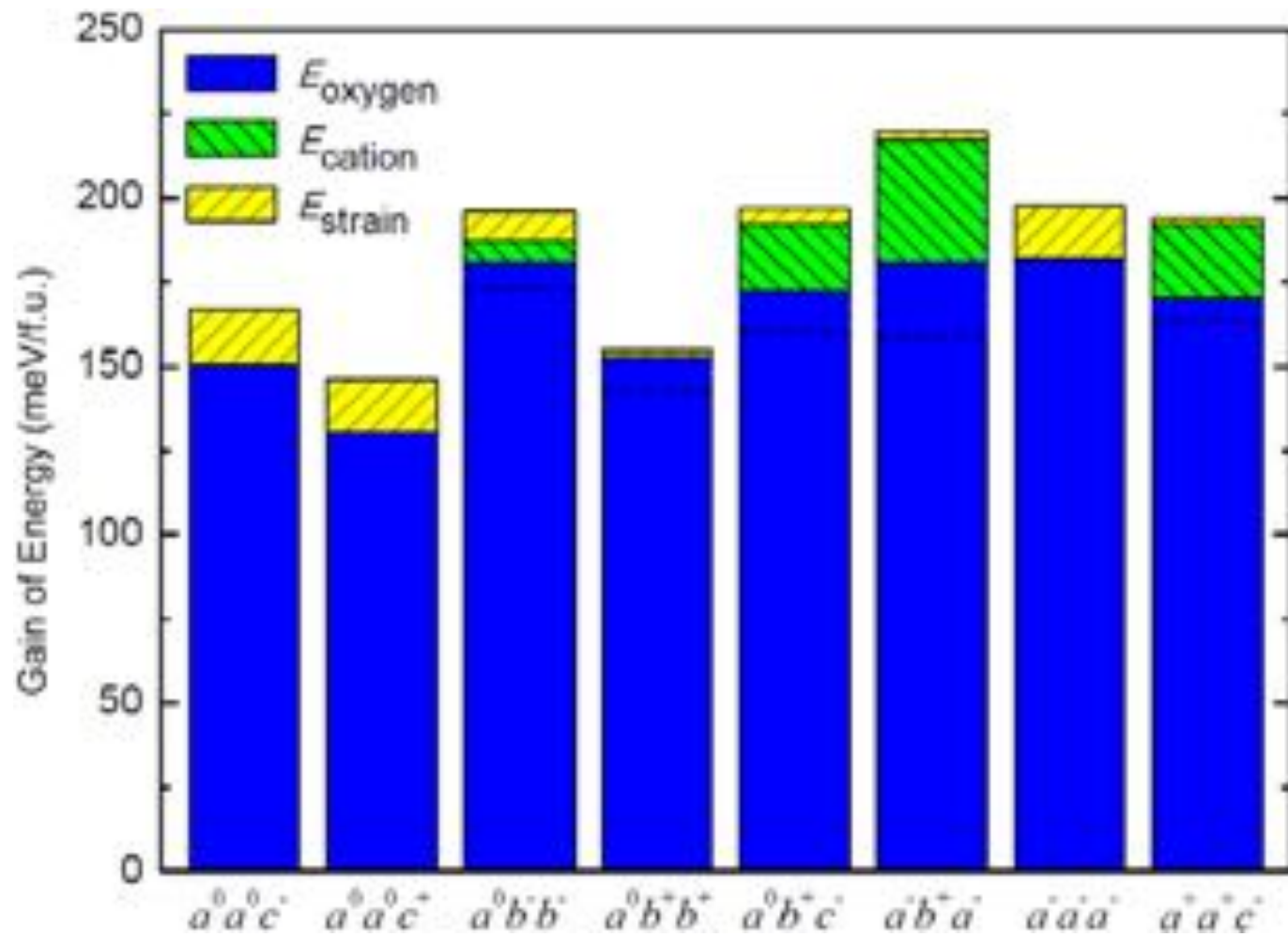
Detour: Why is *Pnma* most common?

AFD (R-point) :  $\phi^-$

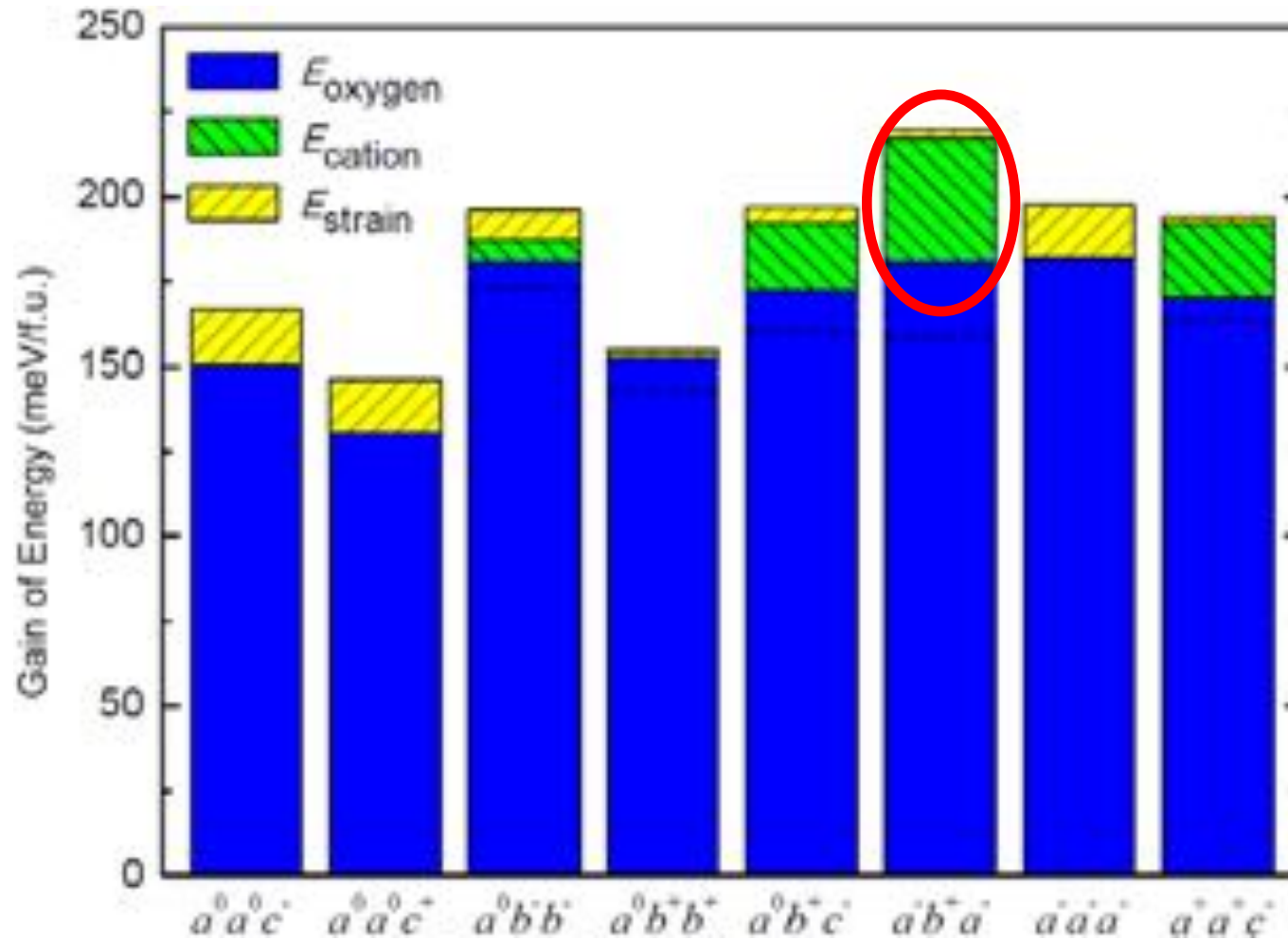


# *Pnma* most stable

---



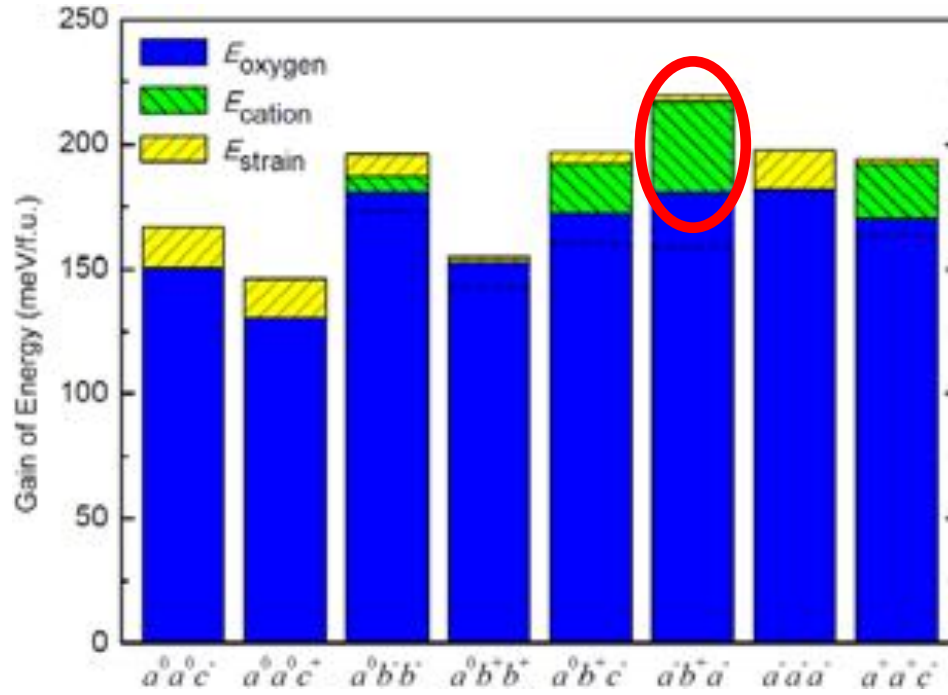
# *Pnma* most stable



Due to other motions  
(not tilts!)

-> couplings at play?

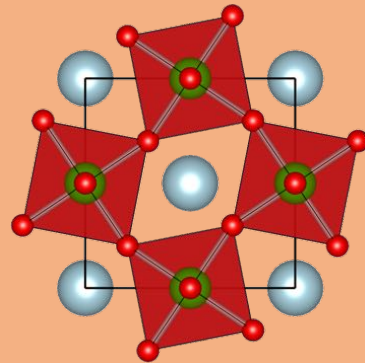
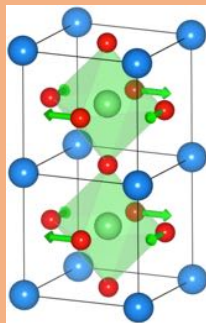
# Trilinear terms



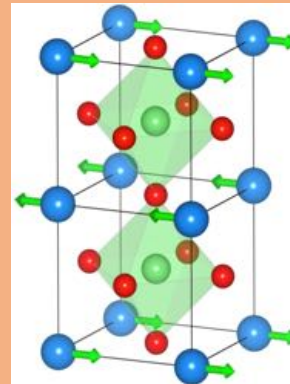
$$\mathcal{F}(X_5^-, \phi_z^+, \phi_{xy}^-) \propto \lambda \phi_z^+ \phi_{xy}^- X_5^-$$

Miao, Bristowe et al JPCM 26 035401 (2014)

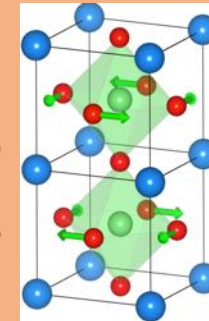
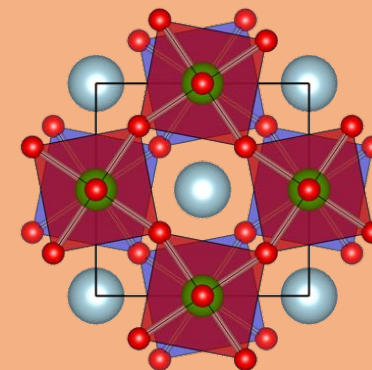
AFD (M-point) :  $\phi_z^+$



Anti-polar :  $X_5^-$



AFD (R-point) :  $\phi_x^-$

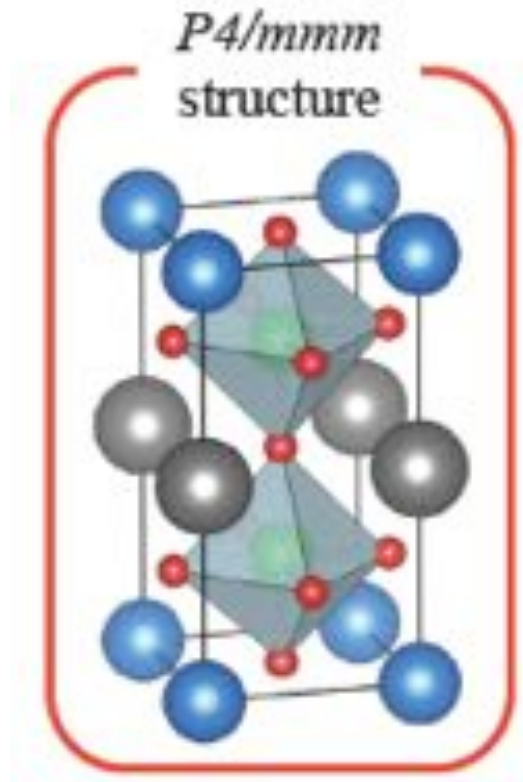


# Can we cooperatively couple AFD with FE?

---

$$\mathcal{F}(X_5^-, \phi_z^+, \phi_{xy}^-) \propto \lambda \phi_z^+ \phi_{xy}^- X_5^-$$

Turn anti-polar  $X$  mode to polar mode?



Consider digital superlattice

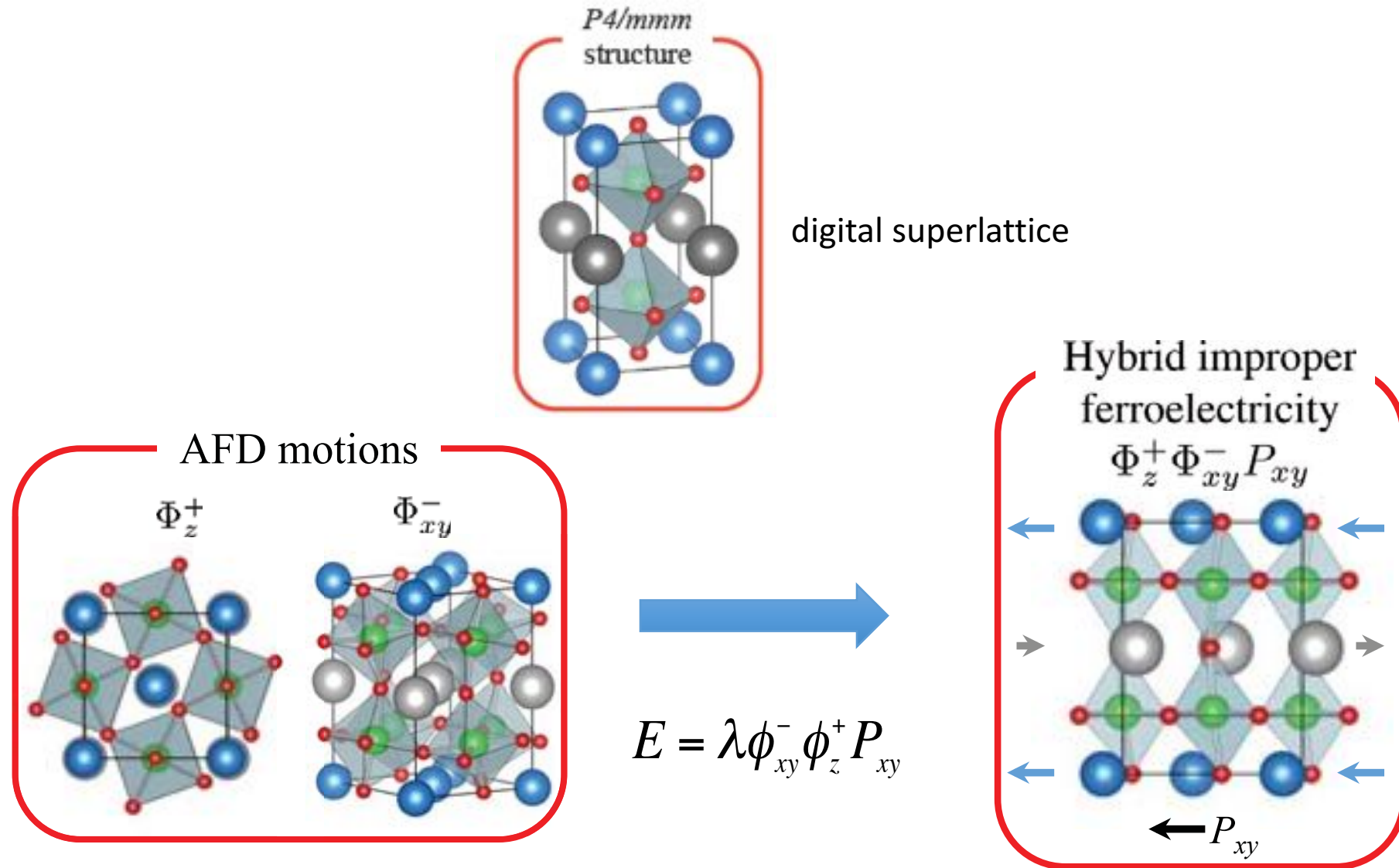
Layers of **A** and **A'** in alternate (001) planes

can be grown layer-by-layer (e.g. PLD MBE)

or naturally ordered (e.g. double perovskites)

*(the same concept will work on thicker superlattices, and other layered materials e.g. RP, DJ, Aurivilius)*

# Rotationally driven ferroelectricity

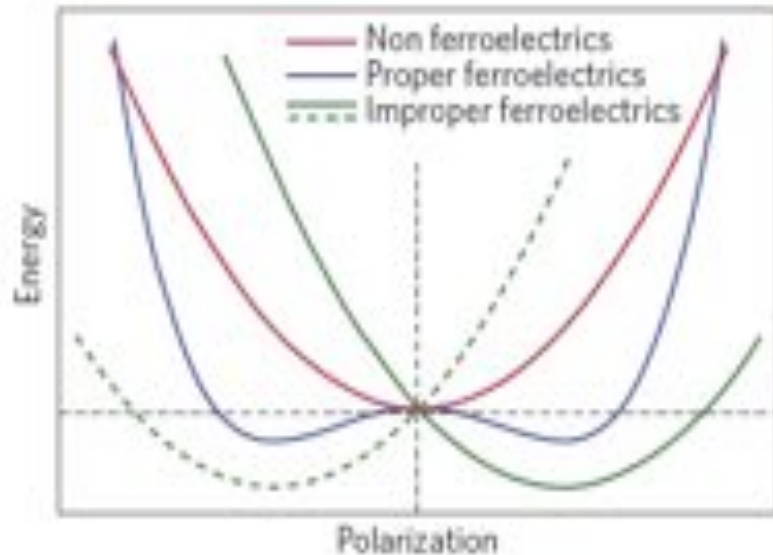


Only ingredient is *Pnma* type rotations and layering



# (Hybrid) Improper Ferroelectricity

Shift the well to lower energy through the coupling with other phonon modes



“**Hybrid**” = requires two independent order parameters belonging to a different subspaces

Hybrid improper ferroelectricity

$$E = \frac{1}{2} A_0 P^2 + \frac{1}{4} B_0 P^4 + C_{12} \phi_1^2 \phi_2^2 + \frac{1}{2} A_1 \phi_1^2 + \frac{1}{4} B_1 \phi_1^4 + C_{01} \phi_1^2 P^2 + \frac{1}{2} A_2 \phi_2^2 + \frac{1}{4} B_2 \phi_2^4 + C_{02} \phi_2^2 P^2$$

$$+ \lambda \phi_1 \phi_2 P$$

**Trilinear**  
coupling term

- $\lambda \phi_1 \phi_2$  acts as an effective field shifting  $P$  well to lower energy
- **Switching  $P$  requires reversing either  $\phi_1$  or  $\phi_2$  (and perhaps  $M$ )**

# Experimental signatures

nature  
materials

ARTICLES

PUBLISHED ONLINE: 12 JANUARY 2015 | DOI: 10.1038/NMAT4168

## Experimental demonstration of hybrid improper ferroelectricity and the presence of abundant charged walls in $(\text{Ca,Sr})_3\text{Ti}_2\text{O}_7$ crystals

Yoon Seok Oh<sup>1,2†</sup>, Xuan Luo<sup>3</sup>, Fei-Ting Huang<sup>1,2</sup>, Yazhong Wang<sup>1,2</sup> and Sang-Wook Cheong<sup>1,2,3\*</sup>

PRL 114, 035701 (2015)

PHYSICAL REVIEW LETTERS

week ending  
23 JANUARY 2015

## Negative Thermal Expansion in Hybrid Improper Ferroelectric Ruddlesden-Popper Perovskites by Symmetry Trapping

M. S. Senn,<sup>1,2,\*</sup> A. Bombardi,<sup>1</sup> C. A. Murray,<sup>1</sup> C. Vecchini,<sup>3</sup> A. Scherillo,<sup>4</sup> X. Luo,<sup>5</sup> and S. W. Cheong<sup>5,6</sup>

nature

Vol 452 | 10 April 2008 | doi:10.1038/nature06817


LETTERS

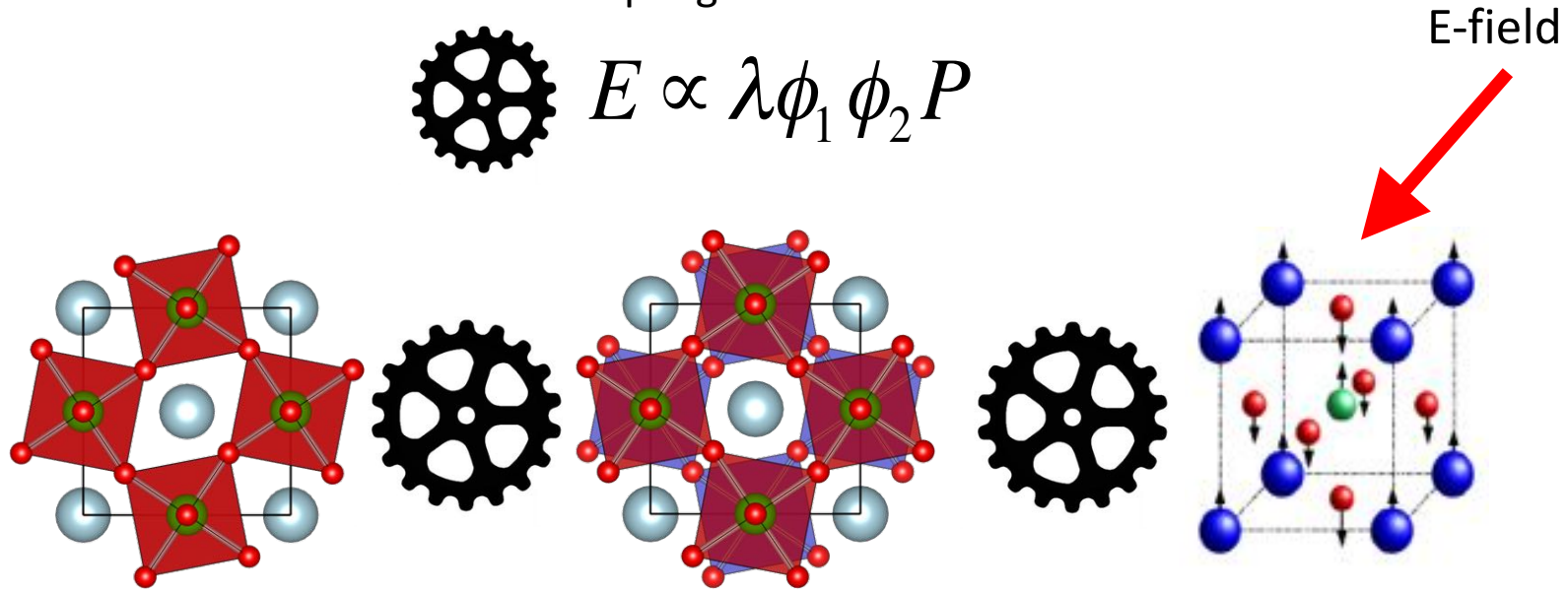
## Improper ferroelectricity in perovskite oxide artificial superlattices

Eric Bousquet<sup>1\*</sup>, Matthew Dawber<sup>2\*†</sup>, Nicolas Stucki<sup>2</sup>, Céline Lichtensteiger<sup>2</sup>, Patrick Hermet<sup>1</sup>, Stefano Gariglio<sup>2</sup>, Jean-Marc Triscone<sup>2</sup> & Philippe Ghosez<sup>1</sup>

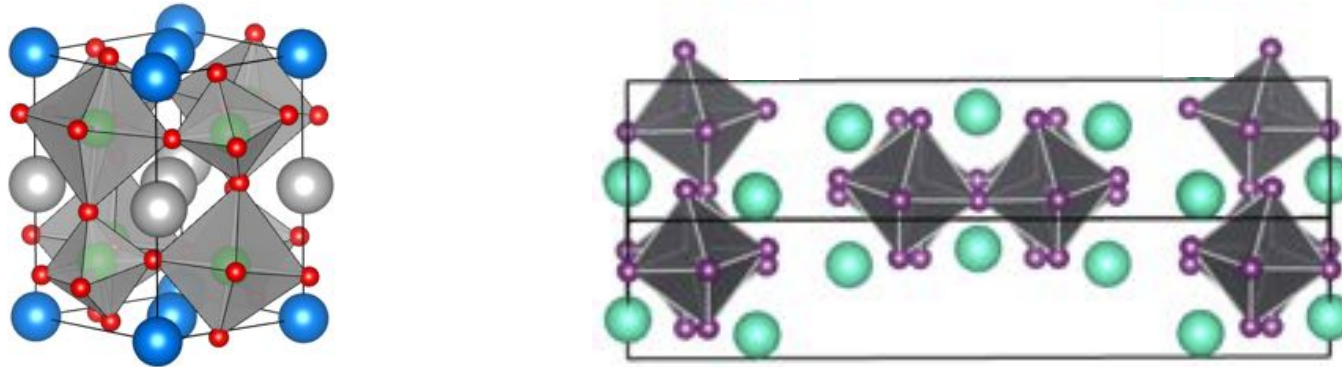
# Hybrid Improper Ferroelectricity

Tri-linear coupling of lattice modes:


$$E \propto \lambda \phi_1 \phi_2 P$$



Typically in *layered* perovskites with  $a^-a^+$  tilt pattern:



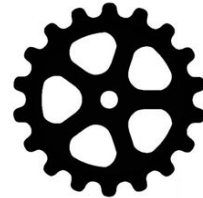
# Alternative to tilts?

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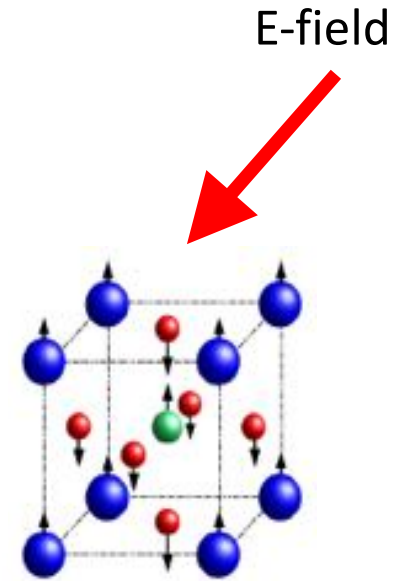
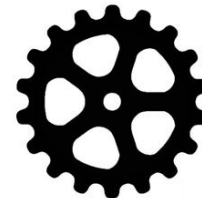
Tri-linear coupling of lattice modes:

$$\text{gear} \quad E \propto \lambda R_1 R_2 P$$

$R_1?$



$R_2?$



Want R to strongly couple to electronic degrees of freedom:



orbital



magnetic

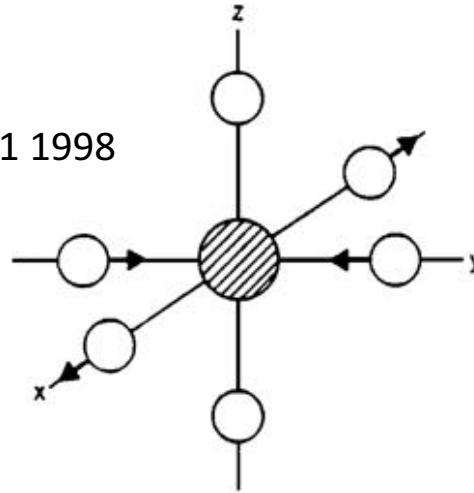


charge

# Jahn-Teller distortion

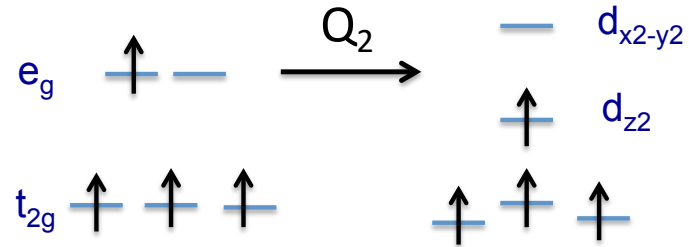
The “ $Q_2$ ” distortion:

Goodenough, Annu. Rev. Mater. Sci. 28 1 1998



Orthorhombic with two short, medium and long bond lengths

e.g.  $Mn^{3+}$

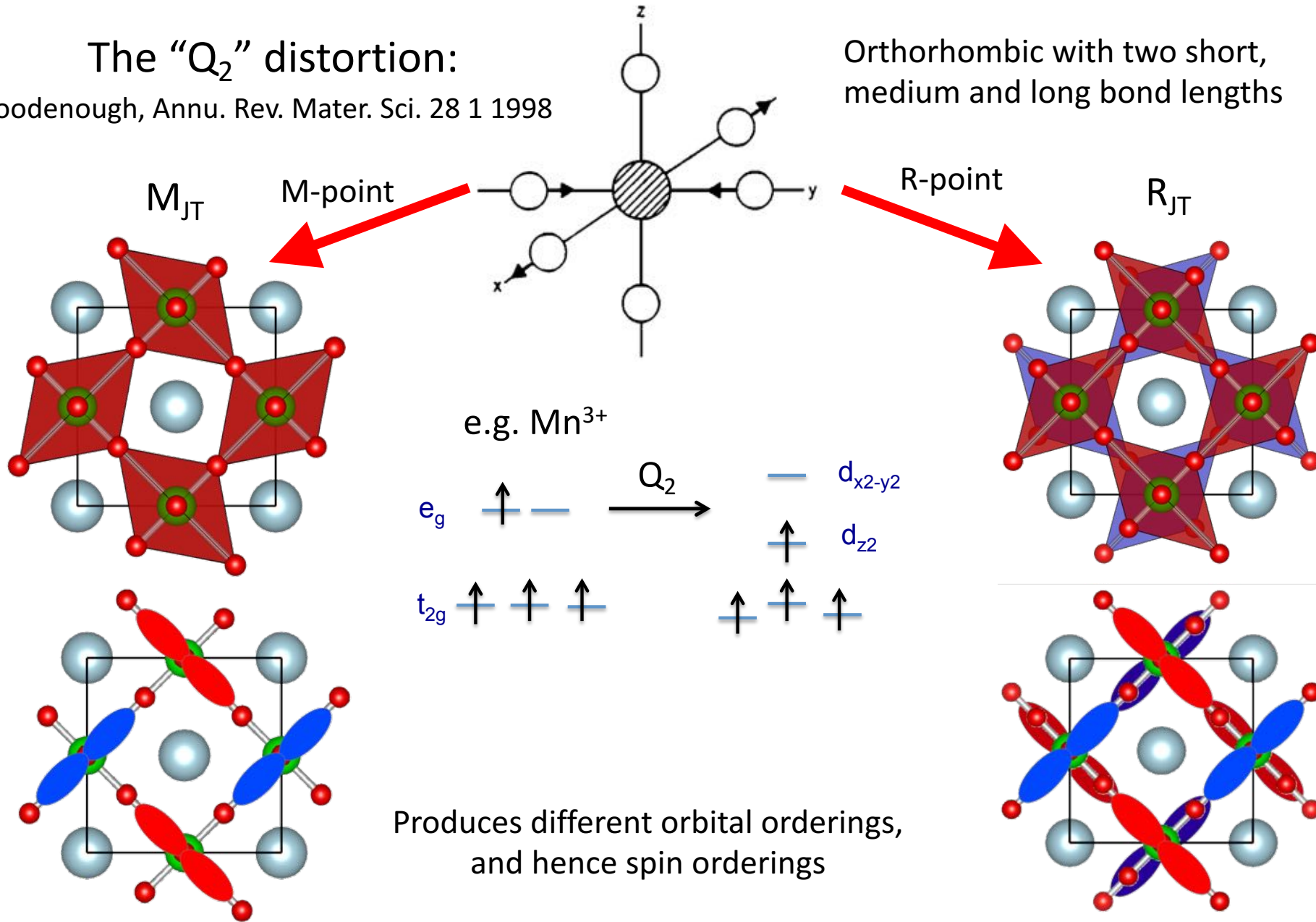


# Jahn-Teller distortion

The “ $Q_2$ ” distortion:

Goodenough, Annu. Rev. Mater. Sci. 28 1 1998


Orthorhombic with two short, medium and long bond lengths

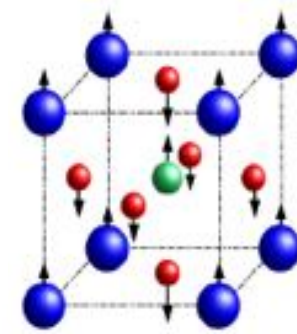
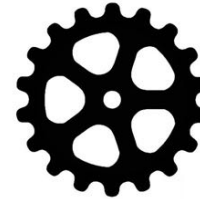
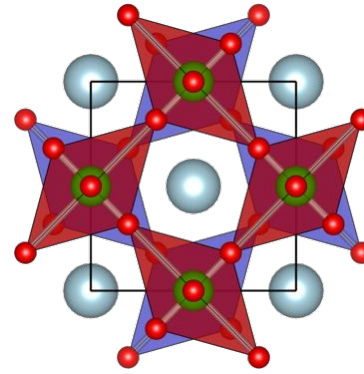
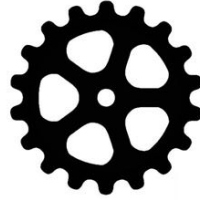
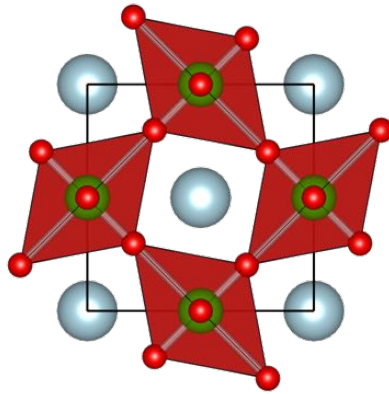


# Alternative to tilts – Jahn-Teller distortion

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Tri-linear coupling of lattice modes:

  $E \propto \lambda R_1 R_2 P$



# Alternative to tilts – Jahn-Teller distortion

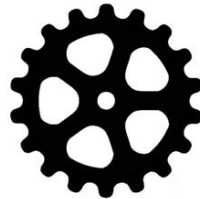
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Tri-linear coupling of lattice modes:

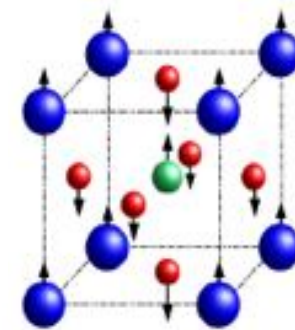
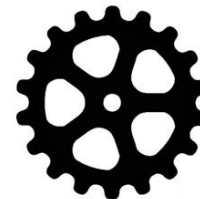
$$\text{gear} \quad E \propto \lambda R_1 R_2 P$$



magnetic



orbital

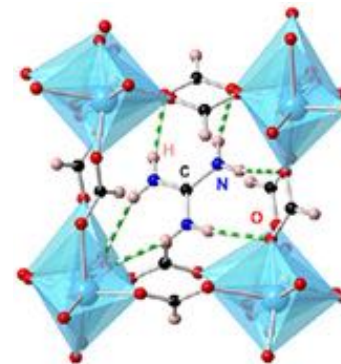


Potential applications: magnetoelectrics, electrochromic, MITs, transistors .... ??

Similar mechanism proposed in related MOFs for multiferroic magnetoelectric applications

[1] Stroppa *et al.*, *Adv. Mater.* **25**, 2284 (2013)

[2] Tian *et al.*, *Phys. Status Solidi RRL* **9**, 62 (2015)

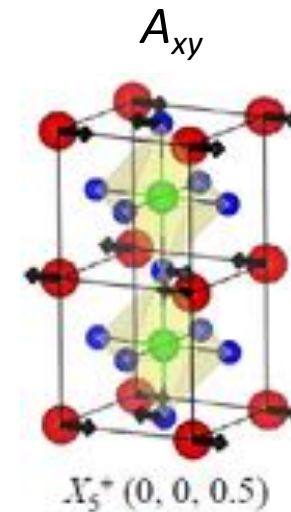
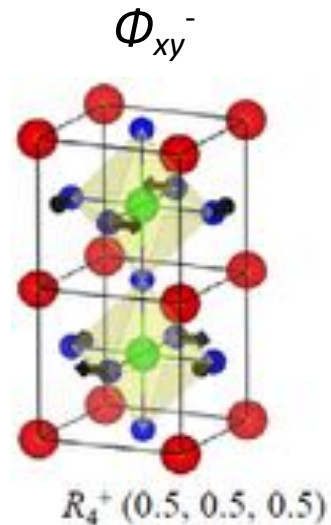
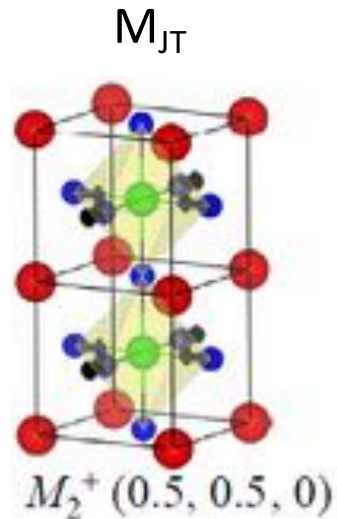




# Lattice-driven Jahn-Teller distortion

$M_{JT}$  is allowed, and always appears, in  $Pnma$  perovskites [1,2]

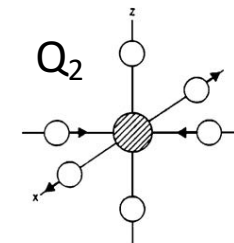
$$E \propto \lambda M_{JT} \phi_{xy}^- A_{xy}$$



Does not have to appear as an electronic instability!

Here we define a Jahn-Teller *distortion*:

by the symmetry of the mode ( $Q_2$ ), whether it is electronically or lattice driven



[1] Carpenter & Howard, Acta Cryst. B **65**, 134 (2009)

[2] Miao, Bristowe, Xu, Verstraete & Ghosez, JPCM **26** 035401 (2014)

# Highlight three P-JT couplings

---

**Symmetry analysis supported by first principles calculations (PBEsol+U and/or B1WC)**

1) Superlattices ( $d^1-d^0$ )  
Titanates:  $\text{ATiO}_3$ - $\text{RTiO}_3$

$$E \propto \lambda M_{JT} \phi_{xy}^- P_{xy}$$

Bristowe, Varignon, Fontaine, Bousquet & Ghosez,  
Nat. Commun. **6**, 6677 (2015)

2) Superlattices ( $d^2-d^2$ )  
Vanadates:  $\text{RVO}_3$ - $\text{R}'\text{VO}_3$

$$E \propto \lambda M_{JT} P_z R_{JT}$$

Varignon, Bristowe, Bousquet & Ghosez,  
Sci Reports **5**, 15364 (2015)

3) Epitaxial bulk (all d fillings)  
ferrites, titanates, manganites ...

$$E \propto \lambda M_{JT} P_{xy} A_{xy}$$

Varignon, Bristowe & Ghosez,  
Phys. Rev. Lett **116**, 057602 (2016)

# Collaborators

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Philippe Ghosez



Eric Bousquet



Denis Fontaine

# Highlight three P-JT couplings

---

Symmetry analysis supported by first principles calculations (PBEsol+U and/or B1WC)

1) Superlattices ( $d^1-d^0$ )  
Titanates:  $\text{ATiO}_3$ - $\text{RTiO}_3$

$$E \propto \lambda M_{JT} \phi_{xy}^- P_{xy}$$

Bristowe, Varignon, Fontaine, Bousquet & Ghosez,  
Nat. Commun. **6**, 6677 (2015)

2) Superlattices ( $d^2-d^2$ )  
Vanadates:  $\text{RVO}_3$ - $\text{R}'\text{VO}_3$

$$E \propto \lambda M_{JT} P_z R_{JT}$$

Varignon, Bristowe, Bousquet & Ghosez,  
Sci Reports **5**, 15364 (2015)

3) Epitaxial bulk (all d fillings)  
ferrites, titanates, manganites ...

$$E \propto \lambda M_{JT} P_{xy} A_{xy}$$

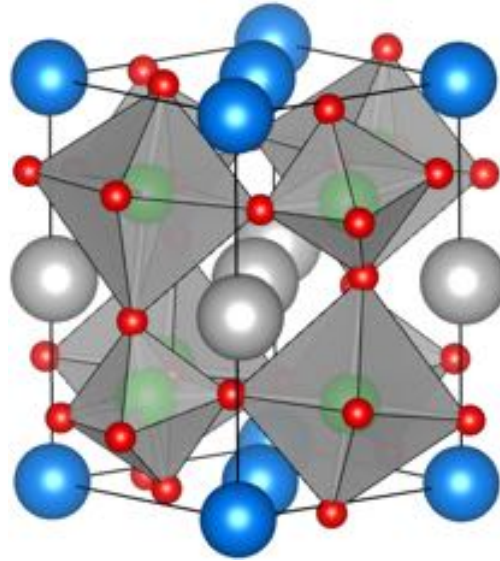
Varignon, Bristowe & Ghosez,  
Phys. Rev. Lett **116**, 057602 (2016)

# ATiO<sub>3</sub>-RTiO<sub>3</sub> superlattice

**A<sup>2+</sup>** = Sr, Ba, (Ca)

**Ti<sup>3.5+</sup>** = Ti

**R<sup>3+</sup>** = La, Pr, Sm Y,  
Tm, (Lu)



**Ground-state**  
(In all cases!)

- Monoclinic P2<sub>1</sub> symmetry
- Insulating
- Ferroelectric
- Ferromagnetic

Symmetry adapted mode analysis

R, A	$\Phi$		Q		$M_{JT}$	P	$\Delta$	$\Delta E$
	$\Phi_z^+$	$\Phi_{xy}^-$	$P_{xy}$	B				
Sm, Sr	0.96	1.19	0.56	0.10	0.04	14.9	0.46	20.1
Y, Sr	1.10	1.30	0.66	0.11	0.04	16.7	0.57	18.0
Tm, Sr	1.18	1.36	0.72	0.11	0.03	18.2	0.63	16.4
Sm, Ba	0.75	0.96	0.48	0.13	0.07	18.6	0.50	18.5
Y, Ba	0.95	1.08	0.59	0.14	0.07	21.2	0.60	13.9
Tm, Ba	1.05	1.16	0.65	0.16	0.07	23.4	0.66	10.5

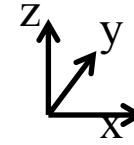
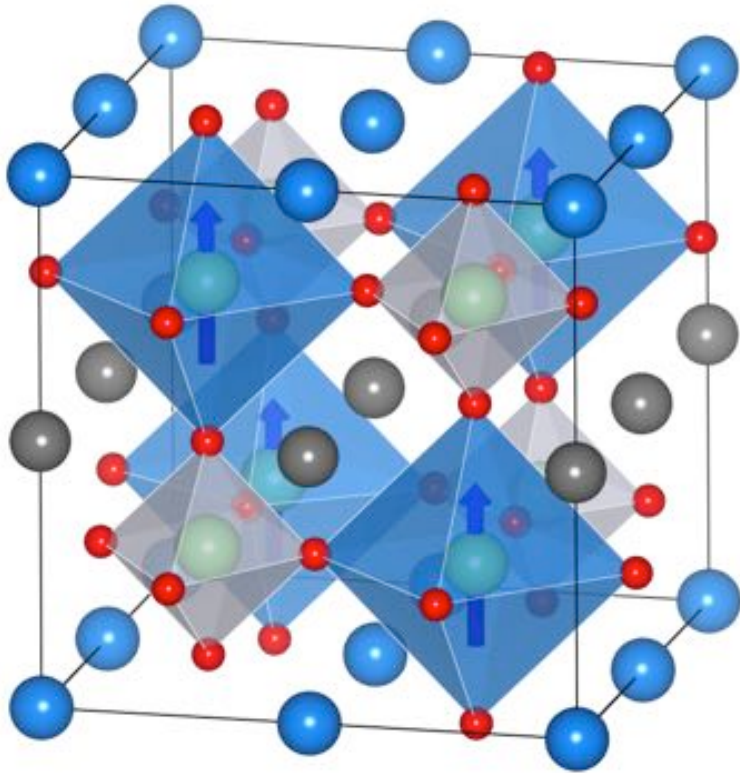
(a<sup>0</sup>a<sup>0</sup>c<sup>+</sup>)(a<sup>-</sup>a<sup>-</sup>c<sup>0</sup>)

Pnma-like (a<sup>-</sup>a<sup>-</sup>c<sup>+</sup>)  
ground state

$$E = \lambda \phi_{xy}^- \phi_z^+ P_{xy}$$

Ferroelectric:  
Amplification of P  
through dissimilar Z\*

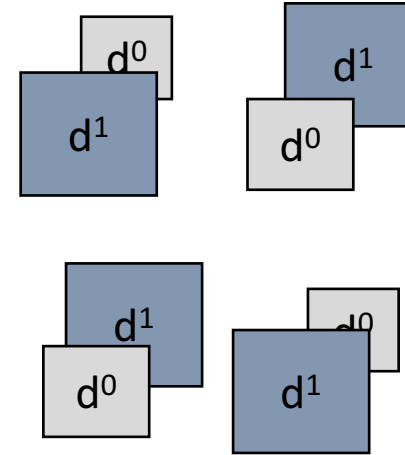
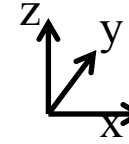
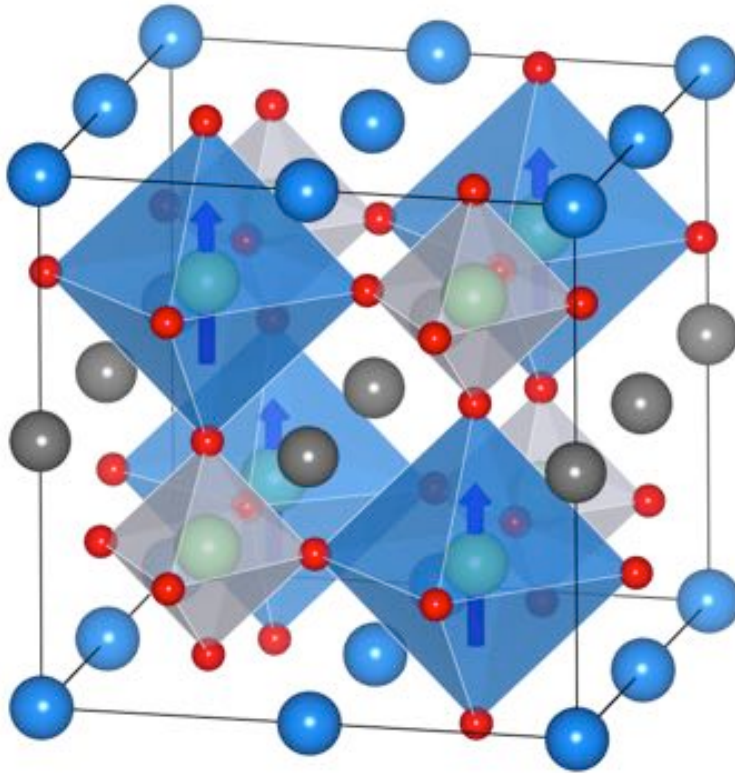
# System remains insulating



R, A	$\Phi$		Q		$M_{JT}$	P	$\Delta$	$\Delta E$
	$\Phi_z^+$	$\Phi_{xy}^-$	$P_{xy}$	B				
Sm, Sr	0.96	1.19	0.56	0.10	0.04	14.9	0.46	20.1
Y, Sr	1.10	1.30	0.66	0.11	0.04	16.7	0.57	18.0
Tm, Sr	1.18	1.36	0.72	0.11	0.03	18.2	0.63	16.4
Sm, Ba	0.75	0.96	0.48	0.13	0.07	18.6	0.50	18.5
Y, Ba	0.95	1.08	0.59	0.14	0.07	21.2	0.60	13.9
Tm, Ba	1.05	1.16	0.65	0.16	0.07	23.4	0.66	10.5

# System remains insulating

---



Charge ordered ( $d^1$ -  $d^0$ ) state associated with a Breathing distortion

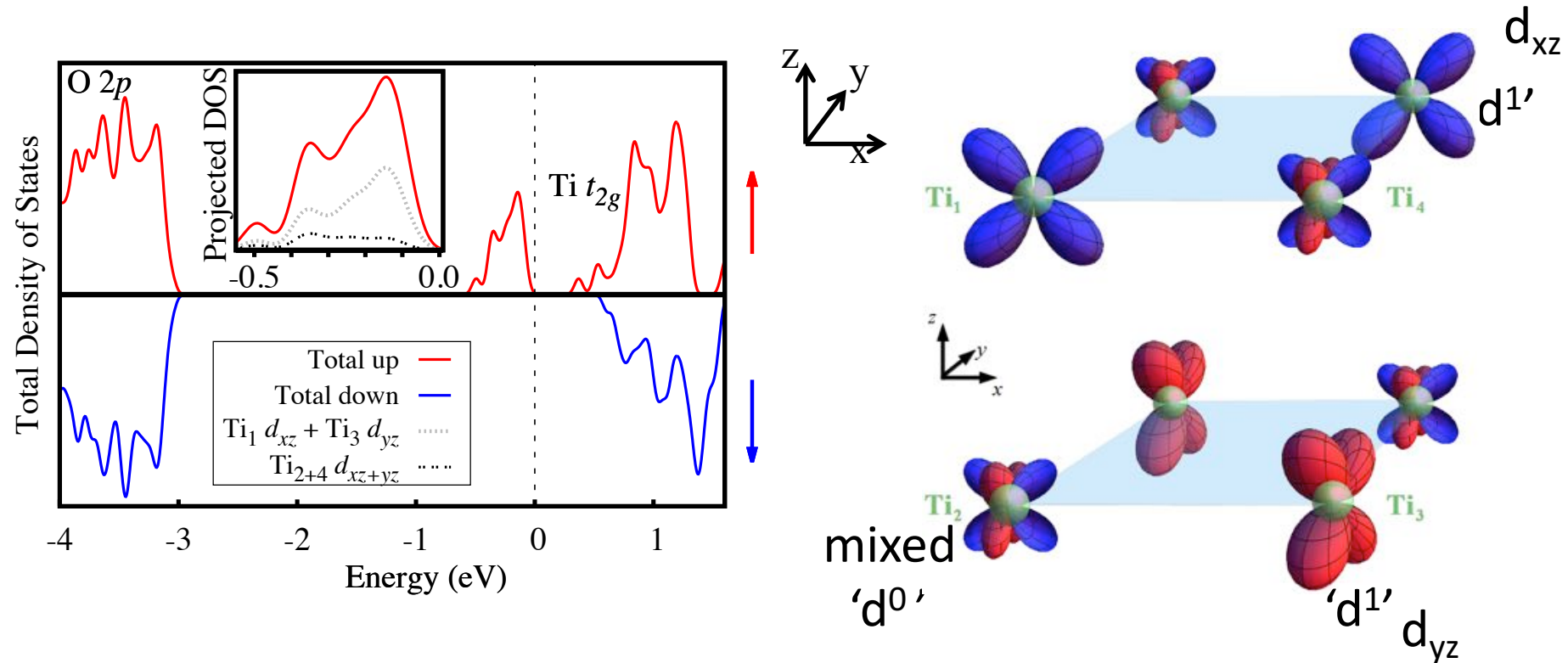
Lifts the degeneracy between neighboring Ti sites

Charge order reported in similar systems:

R. Pentcheva and W.E. Pickett, Phys. Rev. Lett. **99**, 016802 (2007)

A.C. Komarek *et al.*, arXiv:1109.0234 (2012)

# Electronic structure – charge+ orbital ordering



- Spin-polarized split-off  $d^1$  band
- Not the ideal  $d^1-d^0$  occupancy
- $d^1$  site : orbital ordering  $d_{xz} - d_{yz}$
- $d^0$  site : orbital mixing



# Origin of orbital ordering

---

$M_{JT}$  distortion allowed by symmetry  
(equivalent to the coupling in  $Pnma$ )

$$\mathcal{F} \propto P_{xy} \phi_z^+ \phi_{xy}^- + P_{xy} M_{JT} \phi_{xy}^-$$

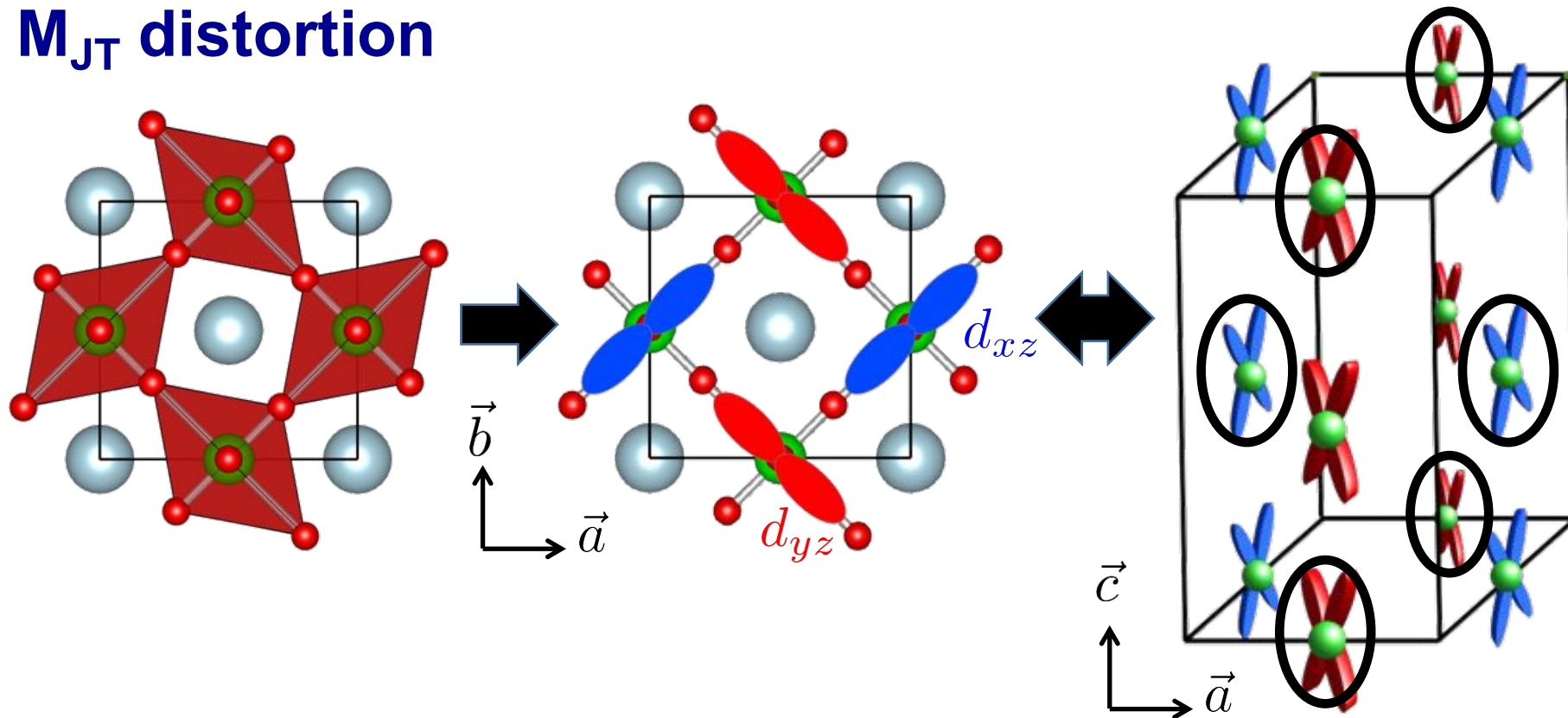
R, A	Q		P	$\Delta$	$\Delta E$			
	$\Phi_z^+$	$\Phi_{xy}^-$						
Sm, Sr	0.96	1.19	0.56	0.10	0.04	14.9	0.46	20.1
Y, Sr	1.10	1.30	0.66	0.11	0.04	16.7	0.57	18.0
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Sm, Ba	0.75	0.96	0.48	0.13	0.07	18.6	0.50	18.5
Y, Ba	0.95	1.08	0.59	0.14	0.07	21.2	0.60	13.9
Tm, Ba	1.05	1.16	0.65	0.16	0.07	23.4	0.66	10.5

# Origin of orbital ordering

$M_{JT}$  distortions produces the C-type orbital ordering

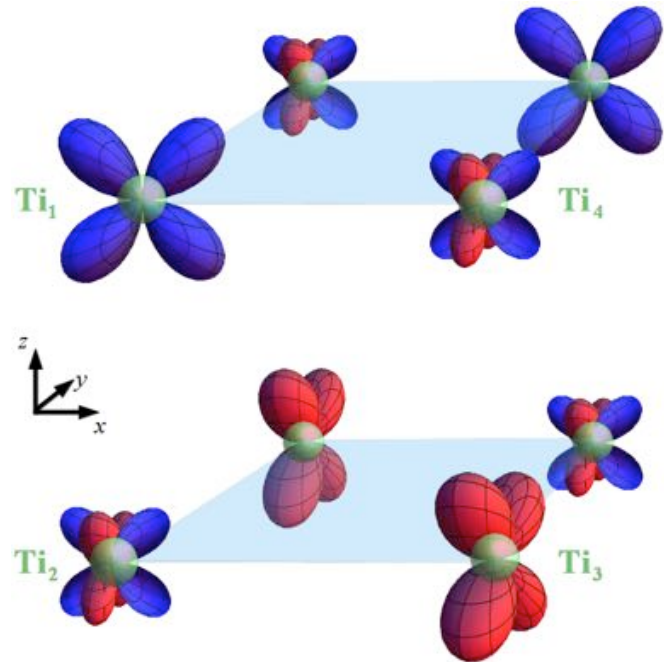
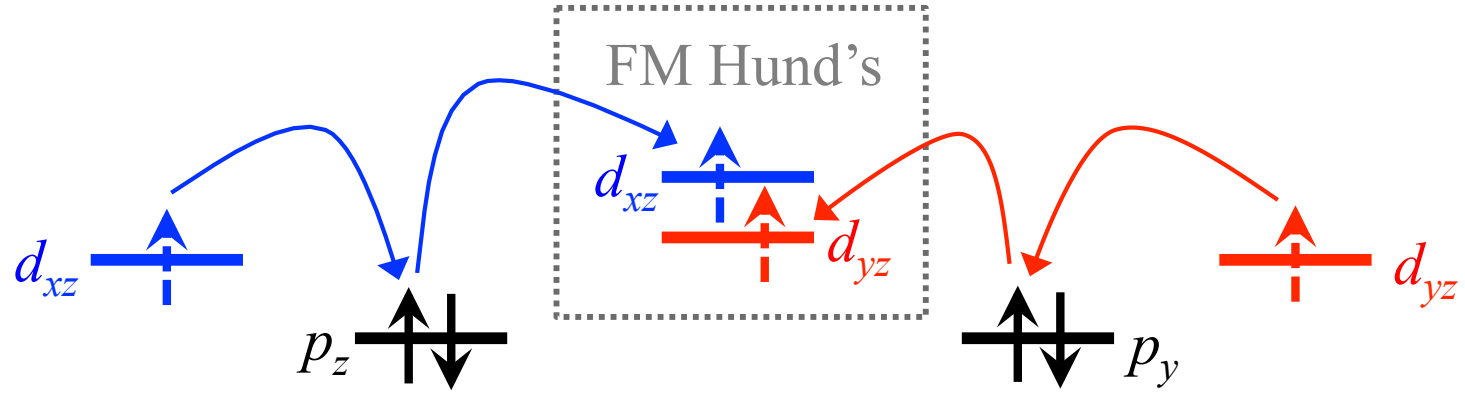
$$\mathcal{F} \propto P_{xy} \phi_z^+ \phi_{xy}^- + P_{xy} M_{JT} \phi_{xy}^-$$

$M_{JT}$  distortion



# FM due to intrasite Hund's

---



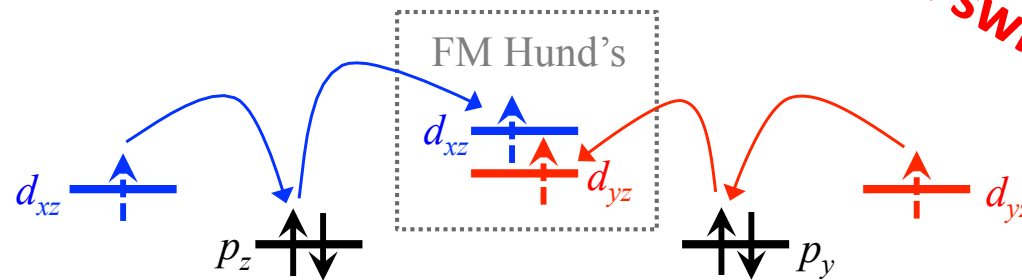
# $M_{JT}$ crucial for FM

If we artificially suppress AFD motions and hence  $M_{JT}$

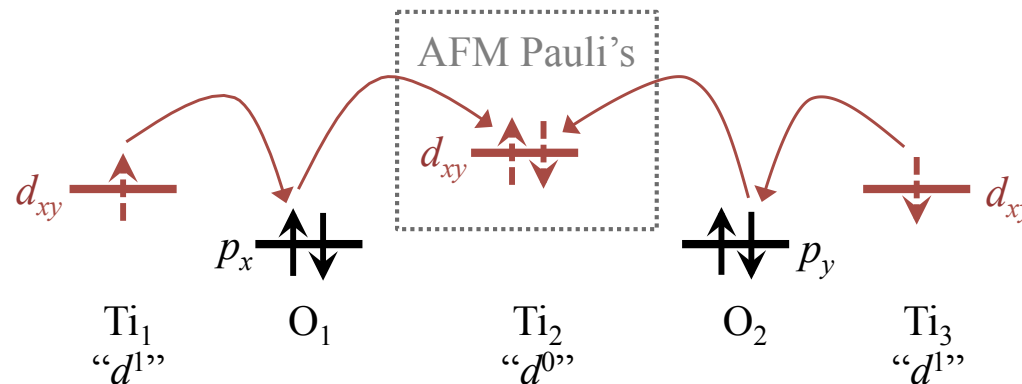
$$E \propto \lambda M_{JT} \phi_{xy}^- P_{xy}$$

- No orbital ordering:  $d_{xy}$  occupancy everywhere
- AFM GS
- Pauli's exclusion principle

With  $M_{JT}$  motions:



Without  $M_{JT}$  motions:



# Highlight three P-JT couplings

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Symmetry analysis supported by first principles calculations (PBEsol+U and/or B1WC)

1) Superlattices ( $d^1-d^0$ )  
Titanates:  $\text{ATiO}_3$ - $\text{RTiO}_3$

$$E \propto \lambda M_{JT} \phi_{xy}^- P_{xy}$$

Bristowe, Varignon, Fontaine, Bousquet & Ghosez,  
Nat. Commun. **6**, 6677 (2015)

2) Superlattices ( $d^2-d^2$ )  
Vanadates:  $\text{RVO}_3$ - $\text{R}'\text{VO}_3$

$$E \propto \lambda M_{JT} P_z R_{JT}$$

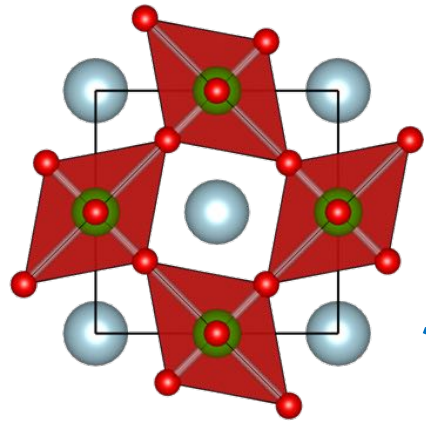
Varignon, Bristowe, Bousquet & Ghosez,  
Sci Reports **5**, 15364 (2015)

3) Epitaxial bulk (all d fillings)  
ferrites, titanates, manganites ...

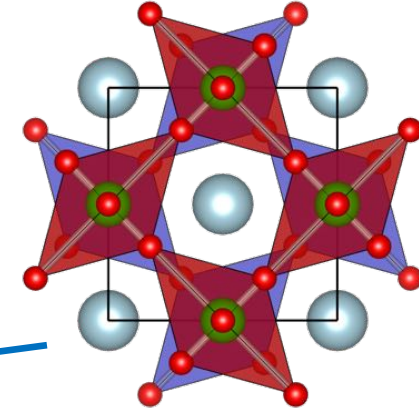
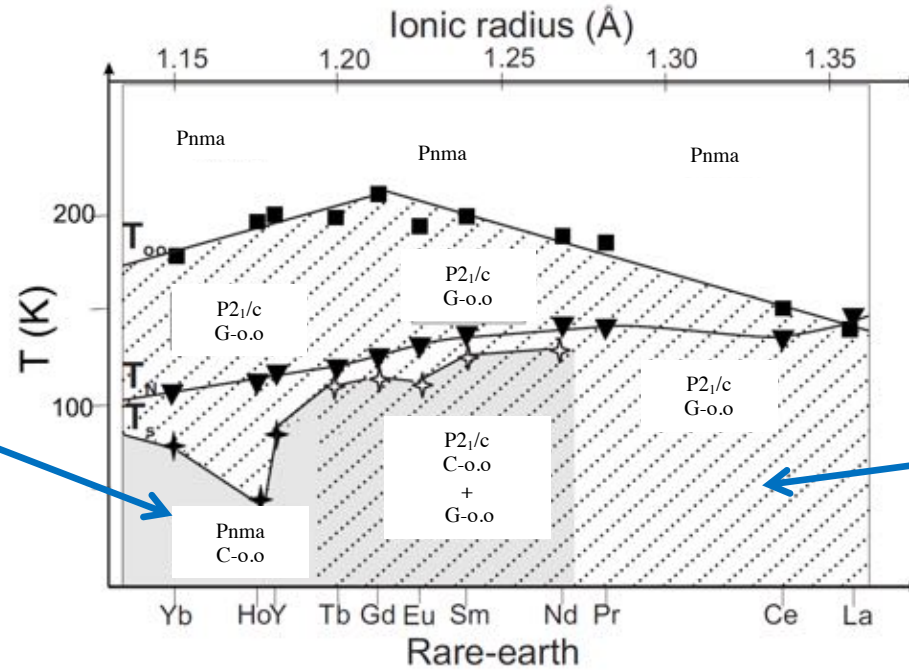
$$E \propto \lambda M_{JT} P_{xy} A_{xy}$$

Varignon, Bristowe & Ghosez,  
Phys. Rev. Lett **116**, 057602 (2016)

# RVO<sub>3</sub>



**G-type AFM**



**C-type AFM**

Rare-earth vanadates *Pnma* at room T, and with decreasing T appearance of:

- C and G type orbital orderings
- G and C type AFM orderings
- Structural phase transition to *P2<sub>1</sub>/c* for C-AFM

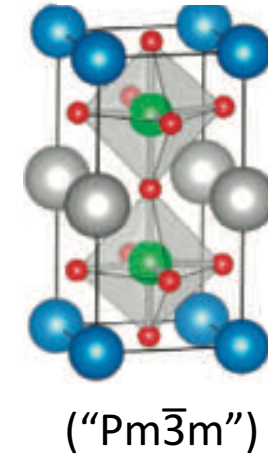
# RVO<sub>3</sub>-R'VO<sub>3</sub> Superlattices

- Ground state:

	AFMG $Pb2_1m$	AFMC $Pb$
YVO/LaVO	0 meV	+7.76 meV
PrVO/YVO	0 meV	-0.87 meV
PrVO/LaVO	0 meV	-3.72 meV

("Pnma")                      ("P2<sub>1</sub>/c")

P4/mmm ref



- Symmetry mode analysis of ground states (Å)

		$\Phi_{xy}^-$	$\Phi_z^+$	$\Phi_z^-$	$R_{JT}$	$M_{JT}$	$P_z$	$P_{xy}$
YVO/LaVO	$Pb2_1m$ AFMG	1.58	1.14			0.12		0.77
PrVO/YVO	$Pb$ AFMC	1.61	1.16	0.01	0.10	0.04	0.01	0.81
PrVO/LaVO	$Pb$ AFMC	1.36	0.94	0.01	0.10	0.01	0.00(4)	0.59

( $a^-a^0c^0$ ) ( $a^0a^0c^+$ )

"Pnma"-like tilt pattern

**$Pb$  phases have additional  $P_z$  component, and combination of both Jahn-Tellers**

# R'VO<sub>3</sub>-RVO<sub>3</sub> couplings

---

## (RVO<sub>3</sub>)<sub>1</sub>/(R'VO<sub>3</sub>)<sub>1</sub> superlattice expansion

$$\Phi_{xy}^- \Phi_z^+ \Phi_z^- \mathbf{P}_{xy} \mathbf{P}_z M_{jt} R_{jt}$$

$$\mathcal{F} \propto \begin{matrix} [2] \\ \mathbf{P}_{xy} \Phi_z^+ \Phi_{xy}^- + \mathbf{P}_{xy} M_{jt} \Phi_{xy}^- \\ + \mathbf{P}_z \Phi_z^+ \Phi_z^- + \boxed{\mathbf{P}_z M_{jt} R_{jt}} \\ [1] \end{matrix}$$

- *Pb2<sub>1</sub>m* (*Pnma* in bulk)
- *Pb* (*P2<sub>1</sub>/c* in bulk)

New trilinear coupling identified

**Out-of-plane polarization coupled to Jahn-Teller !**

[1] Bousquet *et al*, Nature **452** (2008)

[2] Fukushima *et al*, Phys. Chem. Chem. Phys **13** (2011); Rondinelli *et al*, Adv. Materials **24** (2012)



# Magnetolectric application?

---

## Electric field driven magnetic transition ?

$$\text{YVO/LaVO: } \Delta E(\text{AFMG-AFMC}) = -7.76 \text{ meV}$$

Ground-state:  $Pb2_1m$  ("Pnma") – AFMG phase:

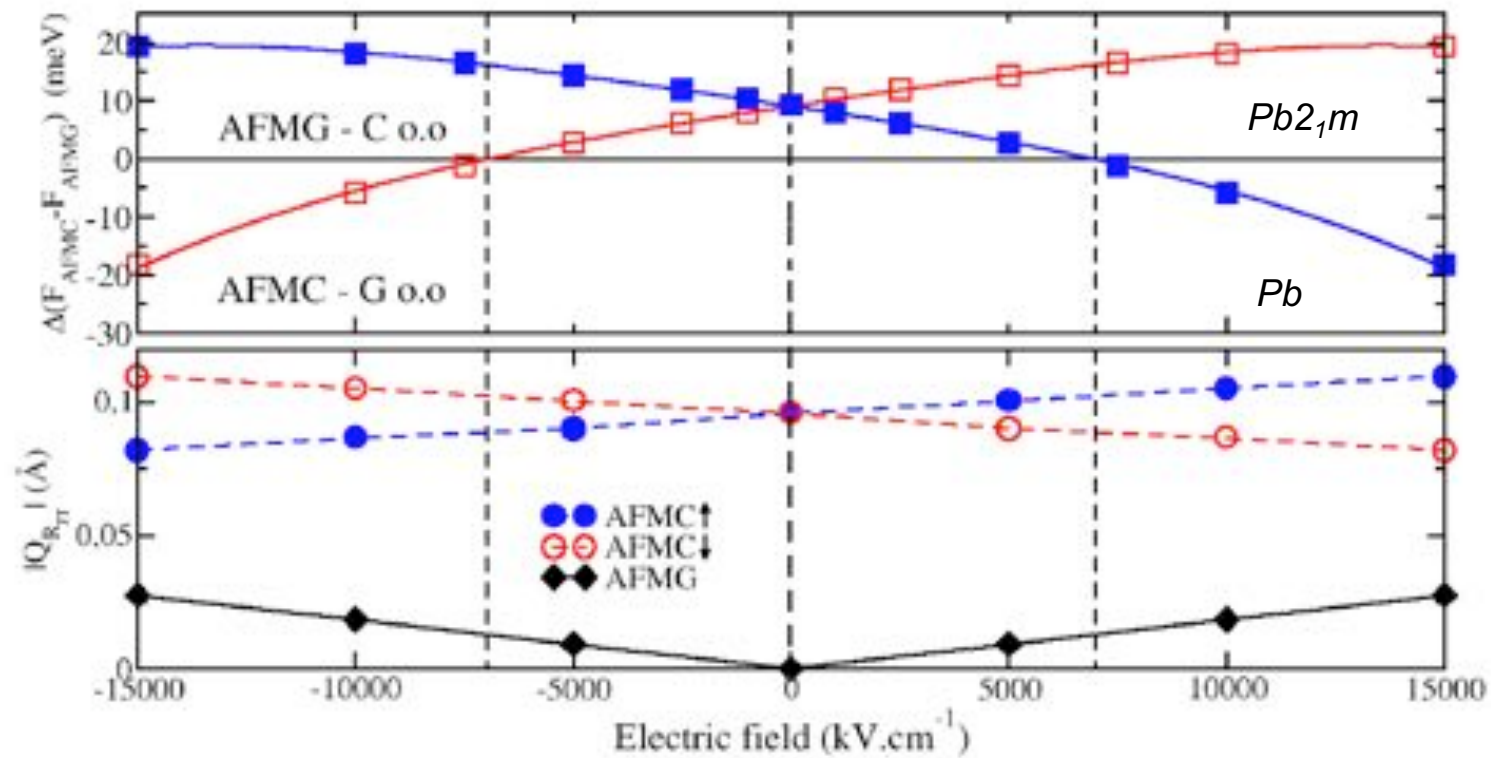
$$\mathcal{F} \propto P_{xy}M_{jt}\Phi_{xy}^- + P_{xy}\Phi_z^+\Phi_{xy}^- \\ + P_zM_{jt}R_{jt} + P_z\Phi_z^+\Phi_z^-$$

$\vec{E} \parallel z$

*Change of orbital and  
AFM orderings !*

# Electric field driven magnetic transition

Finite electric field method (transition at 0.55 V / bilayer)



E-field directly controls  $R_{JT}$  distortion amplitude!  
In turn, this induces M transition

# Highlight three P-JT couplings

---

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$$E \propto \lambda M_{JT} \phi_{xy}^- P_{xy}$$

Bristowe, Varignon, Fontaine, Bousquet & Ghosez,  
Nat. Commun. **6**, 6677 (2015)

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Varignon, Bristowe, Bousquet & Ghosez,  
Sci Reports **5**, 15364 (2015)

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ferrites, titanates, manganites ...

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Varignon, Bristowe & Ghosez,  
Phys. Rev. Lett **116**, 057602 (2016)

# Can couplings appear in general bulk $\text{ABO}_3$ ?

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Strain engineering?

# Can couplings appear in general bulk $\text{ABO}_3$ ?

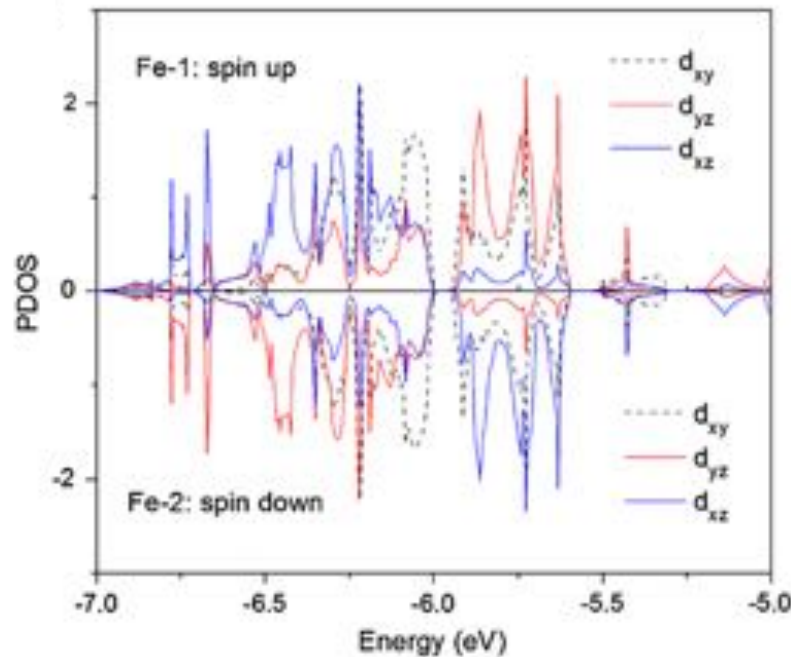
## Strain engineering?

Unusual  $Pmc2_1$  phase (equivalently  $Pb2_1m$ ) under tensile strain:

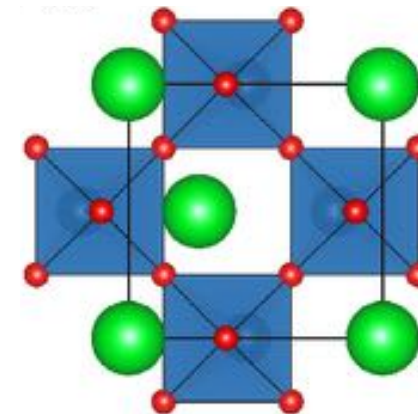
Ground state for  $\text{BiFeO}_3$ ,  $\text{PbTiO}_3$ ,  $\text{BaMnO}_3$ ,  $\text{EuTiO}_3$ ,  $\text{CaTiO}_3$  (+?) at about 5% [1]

“Orbital ordering” observed for  $\text{BiFeO}_3$  [1]  
(though no Jahn-Teller distortion mentioned)

Tri-linear coupling found [2]:  
(but not involving Jahn-Teller?)



$$E \propto \lambda A_{xy} \phi_z^+ P_{xy}$$



$$A_{xy} \\ (M_5^+)$$

[1] Yang *et al.*, Phys. Rev. Lett. **109** 057602 (2012)

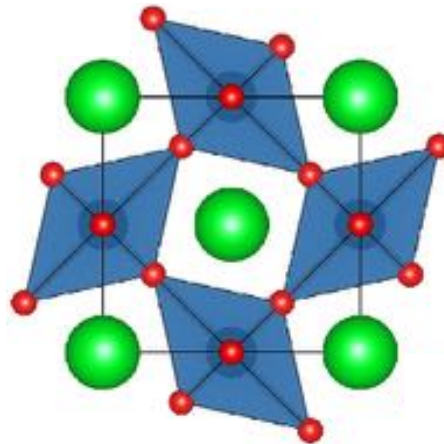
[2] Yang *et al.*, Phys. Rev. Lett. **112** 057202 (2014)

# Reinvestigate $Pmc21$ phase

Truly general? Test on a range of d-fillings

		$d^0$	$d^3$	$d^5$	$d^4$
		SrTiO <sub>3</sub>	BaMnO <sub>3</sub>	BiFeO <sub>3</sub> *	YMnO <sub>3</sub> *
Strain	(%)	+7.35 [61]	+6.1 [61]	+5.8 [61]	+4.0 [61]
Magnetism		NM	FM	AFMG	AFMG
$P$ ( $\Gamma_5^-$ )	(Å)	0.615	0.421	0.346	0.753
	( $\mu\text{C cm}^{-2}$ )	76	45	29	7 [62]
$M_{JT}$ ( $M_3^+$ )	(Å)	0.232	0.190	0.644	0.737
$A$ ( $M_5^+$ )	(Å)	0.558	0.217	1.072	0.940
$\phi_z^+$ ( $M_2^+$ )	(Å)	0.640	0.059	1.668	1.733
Gap	(eV)	3.02	0.28	1.88	1.88

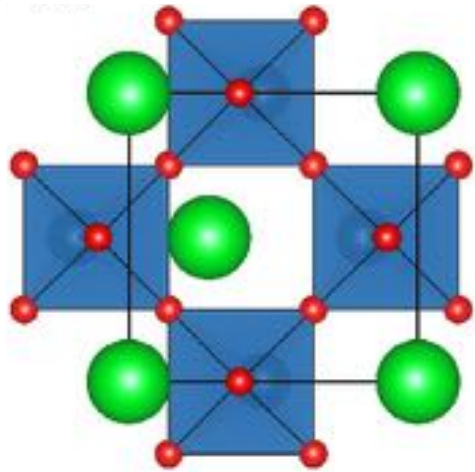
4<sup>th</sup> mode found:  $M_{JT}$   
Very large!



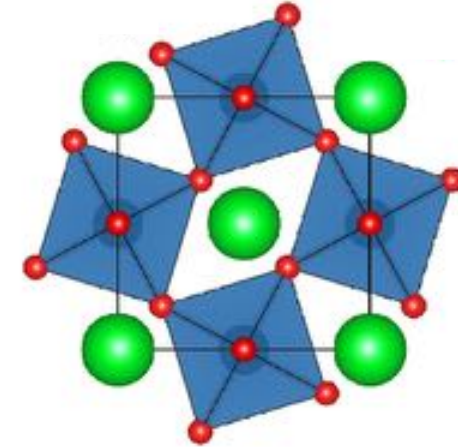
\* Also develop  $\Phi_{xy}^-$

# Invariants analysis

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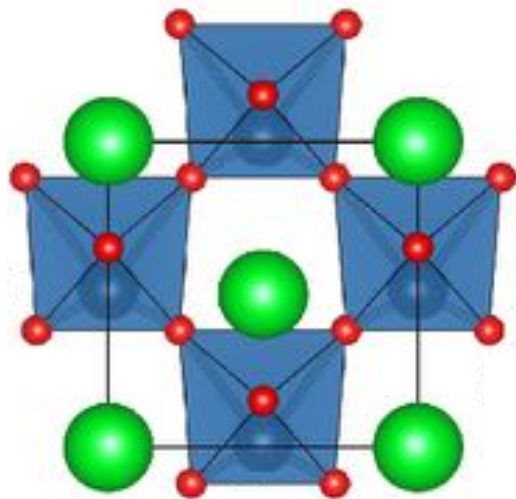


$A_{xy}$   
( $M_5^+$ )

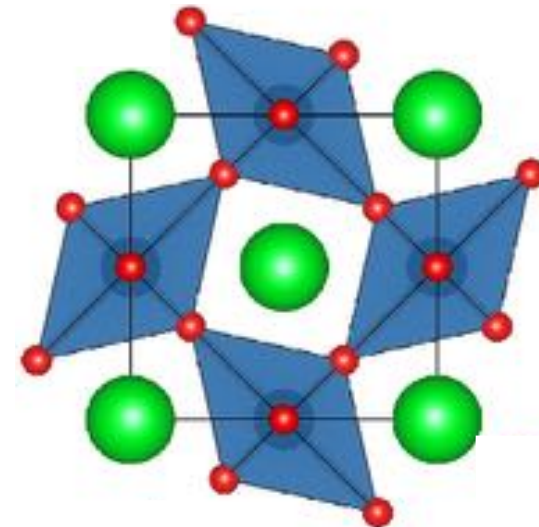


$\Phi_z^+$   
( $M_2^+$ )

$$E \propto \lambda A_{xy} \phi_z^+ P_{xy} + \lambda A_{xy} M_{JT} P_{xy}$$



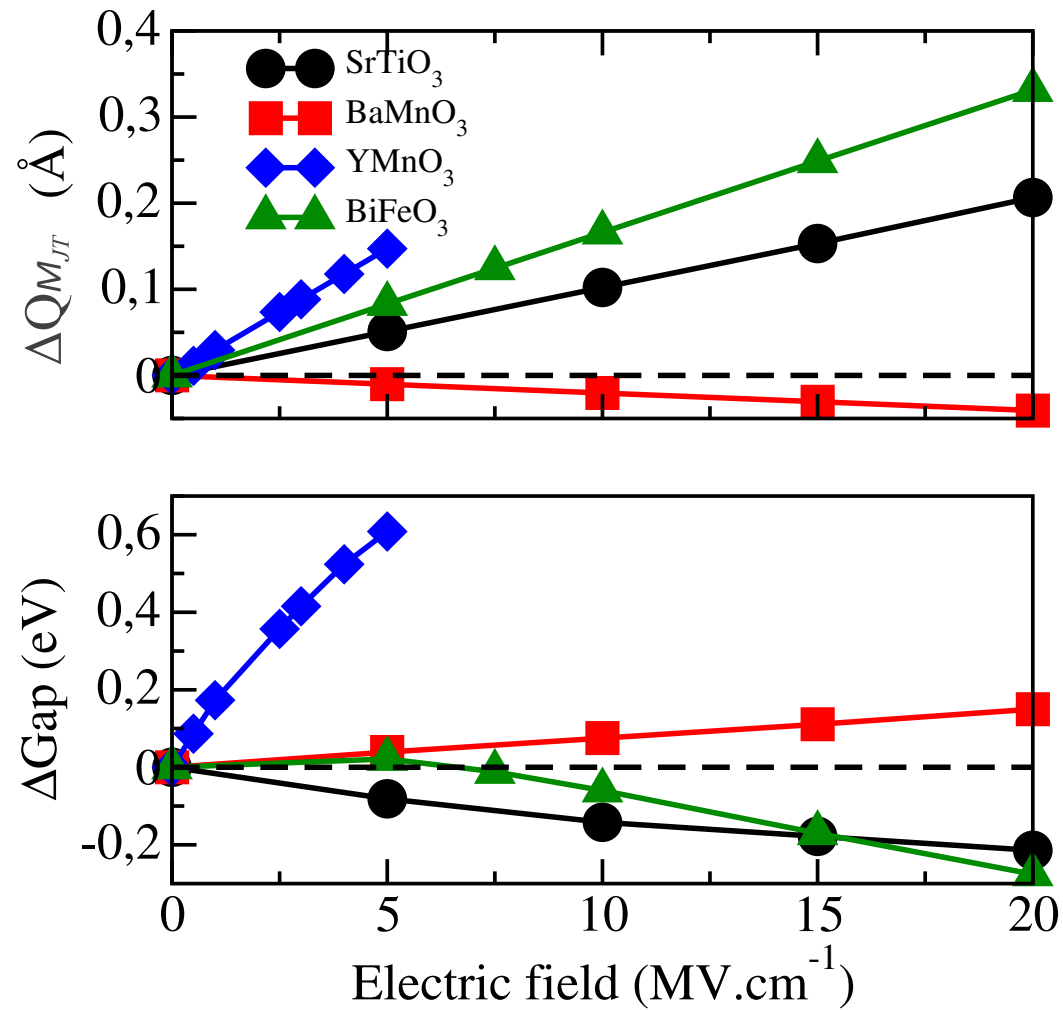
$P_{xy}$   
( $GM_5^-$ )



$M_{JT}$   
( $M_3^+$ )

# E-field control of gap via JT

YMnO<sub>3</sub> largest effect since it is JT active

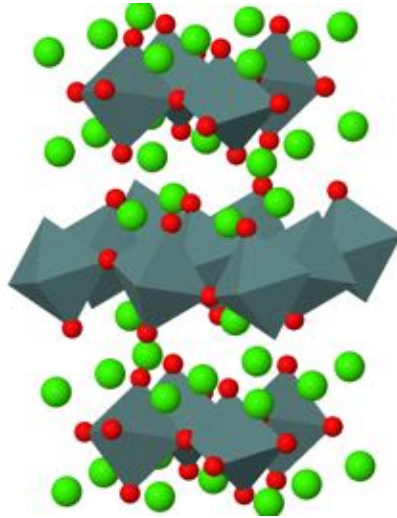




# On-going/Future research in my group

## Emergent phenomena at perovskite interfaces:

Negative thermal expansion  
In naturally layered perovskites



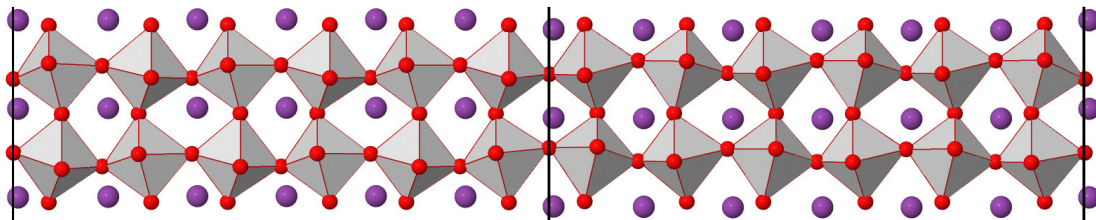
Chris Ablitt

Andrew Warwick



$$\gamma_i = - \left( \frac{\partial \ln(\omega_i)}{\partial \ln(V)} \right)$$

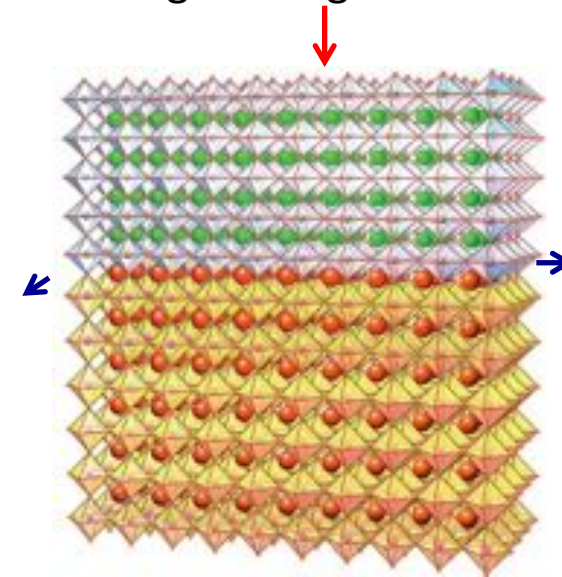
Emergent ferroic orders at domain walls



Khang Le



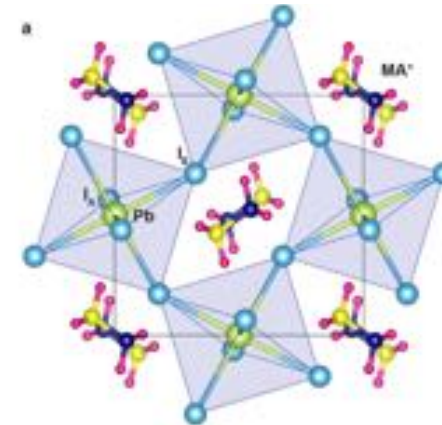
Strain engineering structural phases



Jordan Cowell



Photoferroicity in layered hybrid perovskites



# Methodology

“Effective potential” for lattice dynamics

Wojdel *et al.*, *JPCM* **25** 305401 (2013)

**Energy changes around reference structure due to distortions:**

$$E_{\text{eff}}(\{\mathbf{u}_i\}, \boldsymbol{\eta}) = E_{\text{p}}(\{\mathbf{u}_i\}) + E_{\text{s}}(\boldsymbol{\eta}) + E_{\text{sp}}(\{\mathbf{u}_i\}, \boldsymbol{\eta})$$

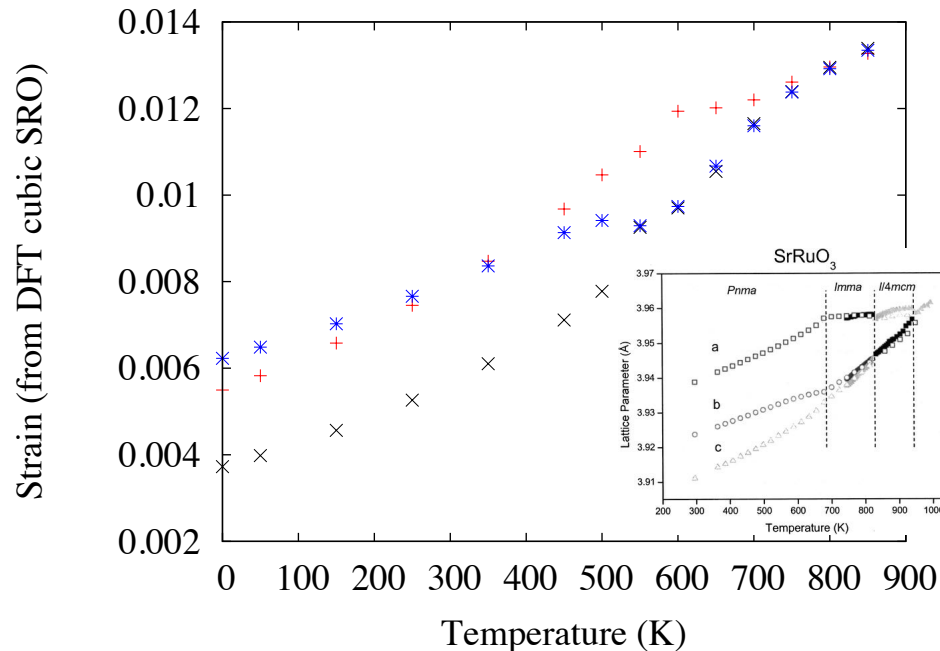
(1) Energy change from atomic displacements (p: phonons), with:

$$E_{\text{p}}(\{\mathbf{u}_i\}) = E_{\text{har}}(\{\mathbf{u}_i\}) + E_{\text{anh}}(\{\mathbf{u}_i\})$$

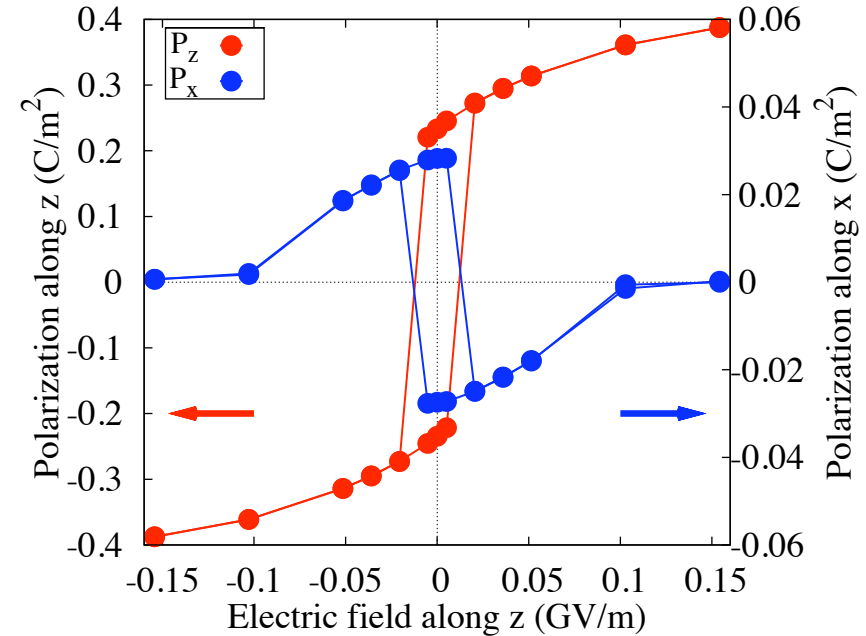
(2) Energy change due to strain only

(3) Strain-phonon coupling term

Finite T: SrRuO<sub>3</sub>



Finite E: PbTiO<sub>3</sub>-SrTiO<sub>3</sub>

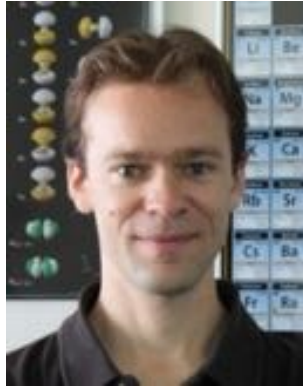


# Thanks for your attention

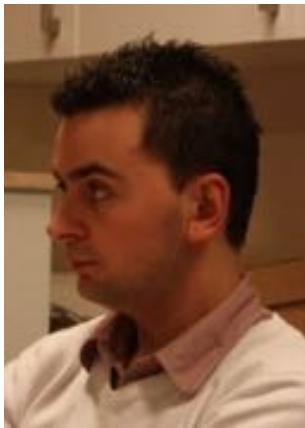
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Philippe Ghosez



Eric Bousquet



Julien Varignon



Denis Fontaine