Pre-University Summer School

Game Theory (part 2)



Strategies and Equilibrium

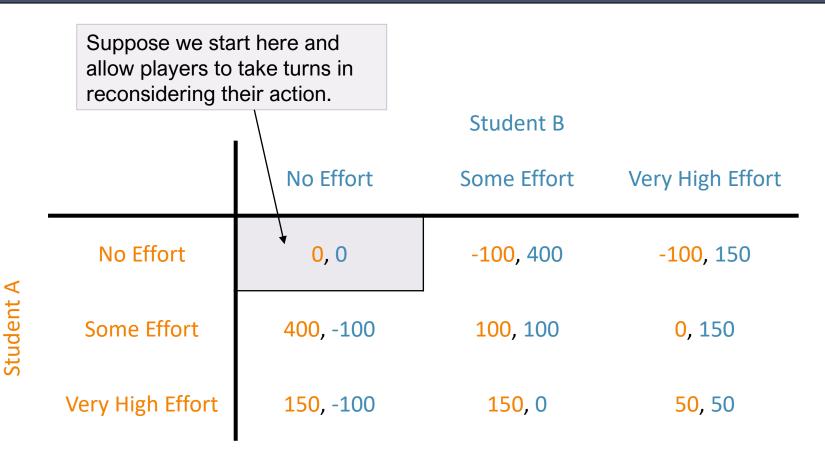
'Dominant strategies' are stable strategies.

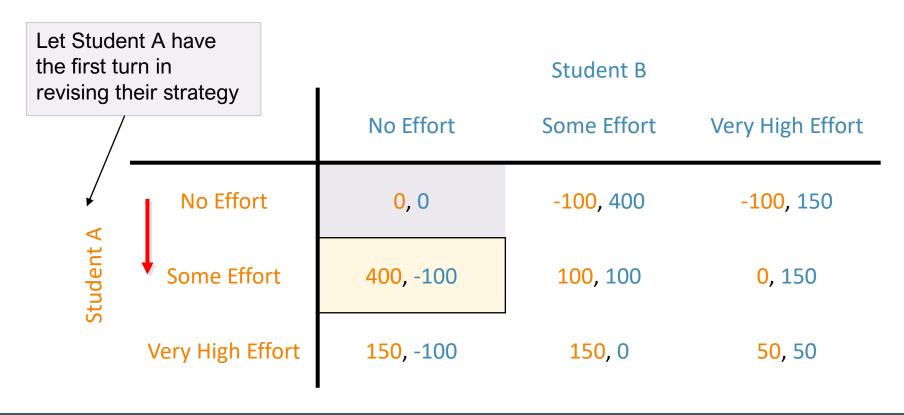
My optimal action does not change, no matter what you will do.

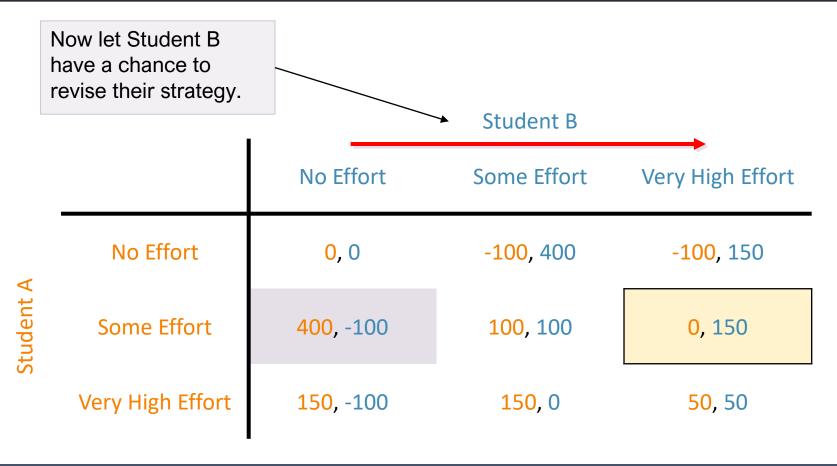
However, 'dominant strategies' do not always exist, so they cannot be used to predict the outcome in every game.

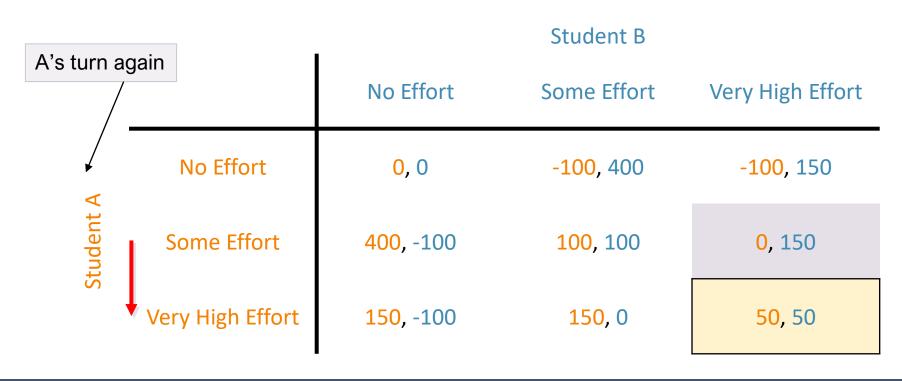
We must look beyond stable strategies and focus on stable outcomes.

This is the essence of the concept of *equilibrium*.









Does either player wish to change their action?

This kind of stable outcome is called a *Nash equilibrium*.

	,	•	Student B	
		No Effort	Some Effort	Very High Effort
Student A	No Effort	0, 0	-100, 400	-100, 150
	Some Effort	400, -100	100, 100	<mark>0, 150</mark>
	Very High Effort	150, - 100	150, 0	50, 50

Other Examples of Nash Equilibrium

		Prisoner B			
_		Confess	Stay Quiet		
Prisoner A	Confess	-5 , -5	<mark>0</mark> , -10		
Priso	Stay Quiet	-10, 0	-1 , -1		
	,	Player B			
		Split	Steal		
Player A	Split	500, 500	<mark>0</mark> , 1000		
Play	Steal	1000, 0	0, 0		

Applying Nash Equilibrium

When is the Nash equilibrium of a game likely to be a useful prediction?

To illustrate some problems, we will study and play two games:

- 1. Keynes' beauty contest game
- 2. Schelling's mass coordination game



Rules

- 1. You will pick an integer number between 1 and 100.
- 2. I will take the average of these submissions.
- 3. The guess which is closest to 2/3^{rds} of the average wins.

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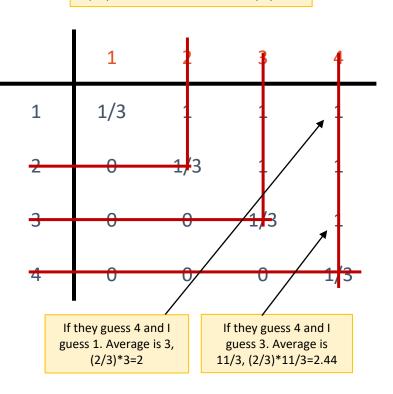




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A Simplified Version (3 total players, guess 1-4)

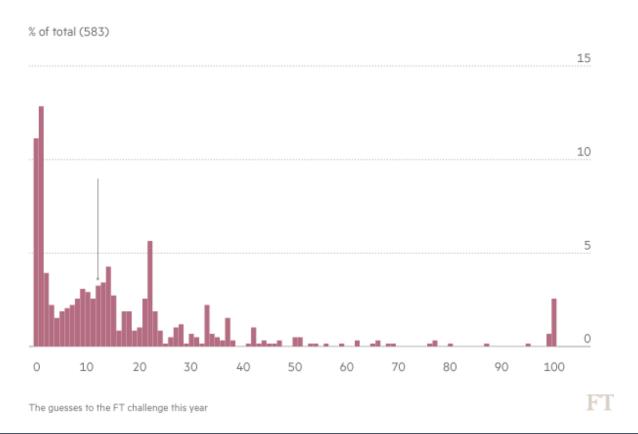
Red number is the guess of the other players. Blue is our choice/our payoff.



Solving by eliminating step by step:

- 4 can never be optimal, even if everyone else picks 4 (it is dominated by 3,2,1).
- 2. If 4 is never played then 3 can never be optimal (dominated by 2,1)
- 3. If 3 is never played then 2 can never be optimal (dominated by 1)
- 4. '1' is left. This is the Nash equilibrium

Results from FT



Implications of 'The Beauty Contest'

This illustrates three problems for players in a game:

- Understanding the game.
- 2. Forming expectations about what the other players will do.
- 3. Finding the best response to what you anticipate them doing.

Is the game theoretic solution to the beauty contest useful?

- Does it provide a good prediction of how people <u>actually</u> play?
- Does it provide good advice about how you would optimally play?



The economist Thomas Schelling devised a version of the following game:

- You and a random person from the population are chosen to play a game.
- You both have the chance to win £10m.
- ➤ You must meet under Big Ben tomorrow but you don't know which time.
- You must decide on the same time to meet, but you cannot communicate.

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	10:00	11:00	12:00	1:00	2:00
10:00	10,10	0,0	0,0	0,0	0,0
11:00	0,0	10,10	0,0	0,0	0,0
12:00	0,0	0,0	10,10	0,0	0,0
1:00	0,0	0,0	0,0	10,10	0,0
2:00	0,0	0,0	0,0	0,0	10,10

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Analysis

	10:00	11:00	12:00	1:00	2:00
10:00	10,10	0,0	0,0	0,0	0,0
11:00	0,0	10,10	0,0	0,0	0,0
12:00	0,0	0,0	10,10	0,0	0,0
1:00	0,0	0,0	0,0	10,10	0,0
2:00	0,0	0,0	0,0	0,0	10,10

Focal Points

Thomas Schelling's theory of *focal points* give us some insight in to how we might select one of multiple Nash equilibria.

In short: Certain NE are culturally more salient (or focal) than others.

Important feature is that focal points are common knowledge.

Examples of similar games:

- Both players have to name a mountain.
- ▶ Both players have to name a famous musician.
- Both players have to name a well-known dish.

Focal points work by being common knowledge, so culture dependent.

Game Theory (Part 2) - Summary

A Nash equilibrium is a prediction about what is likely to happen in a game.

Nash equilibrium makes most sense when players have a chance to revise and adapt their strategy over time.

Two important practical issues when applying Nash equilibrium:

- A Nash equilibrium strategy is not always optimal for an individual to play (others may be acting irrationally!)