

# Unemployment and Mismatch in the UK

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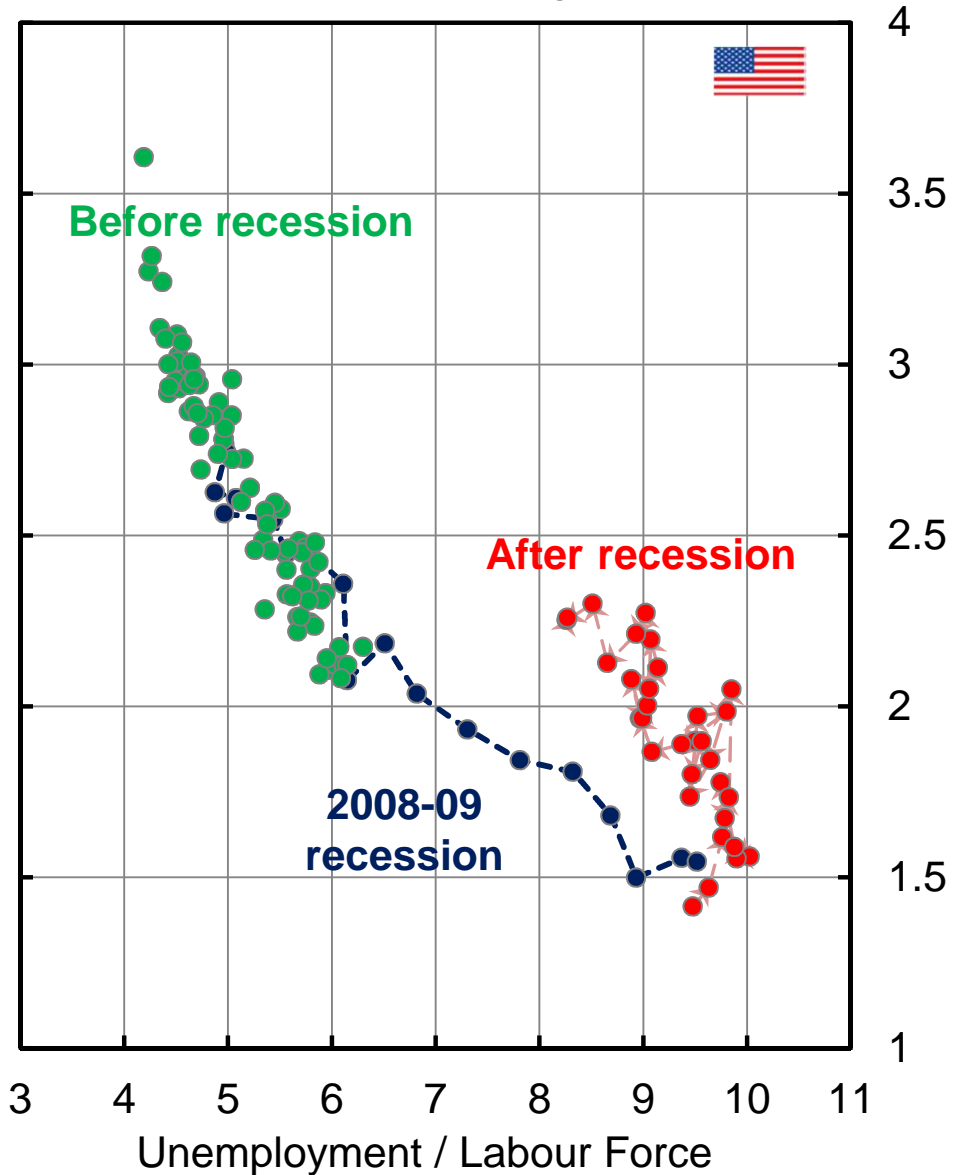
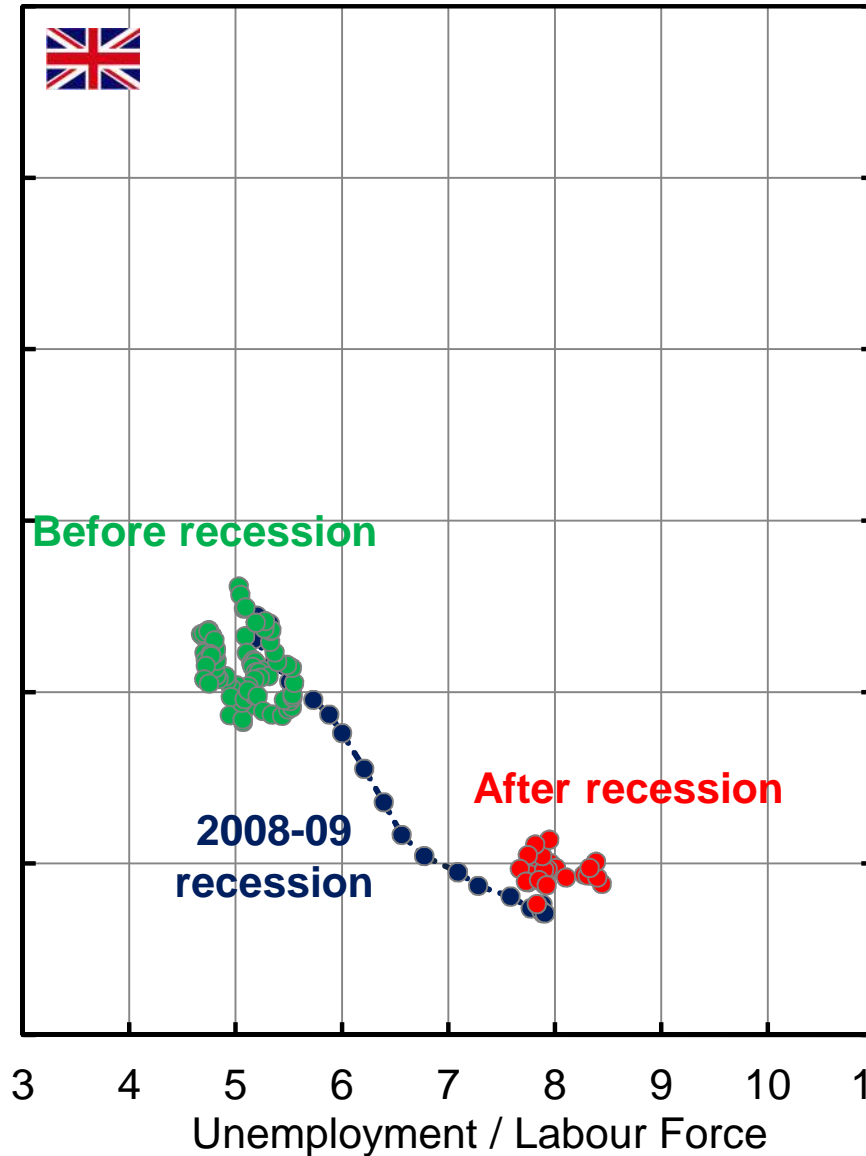


BoE/LSE Conference on Macroeconomics and Monetary Policy:  
“Unemployment, productivity and potential output: the aftermath of the crisis”  
Bank of England, 11-12 October 2012

# Beveridge Curves: UK and US

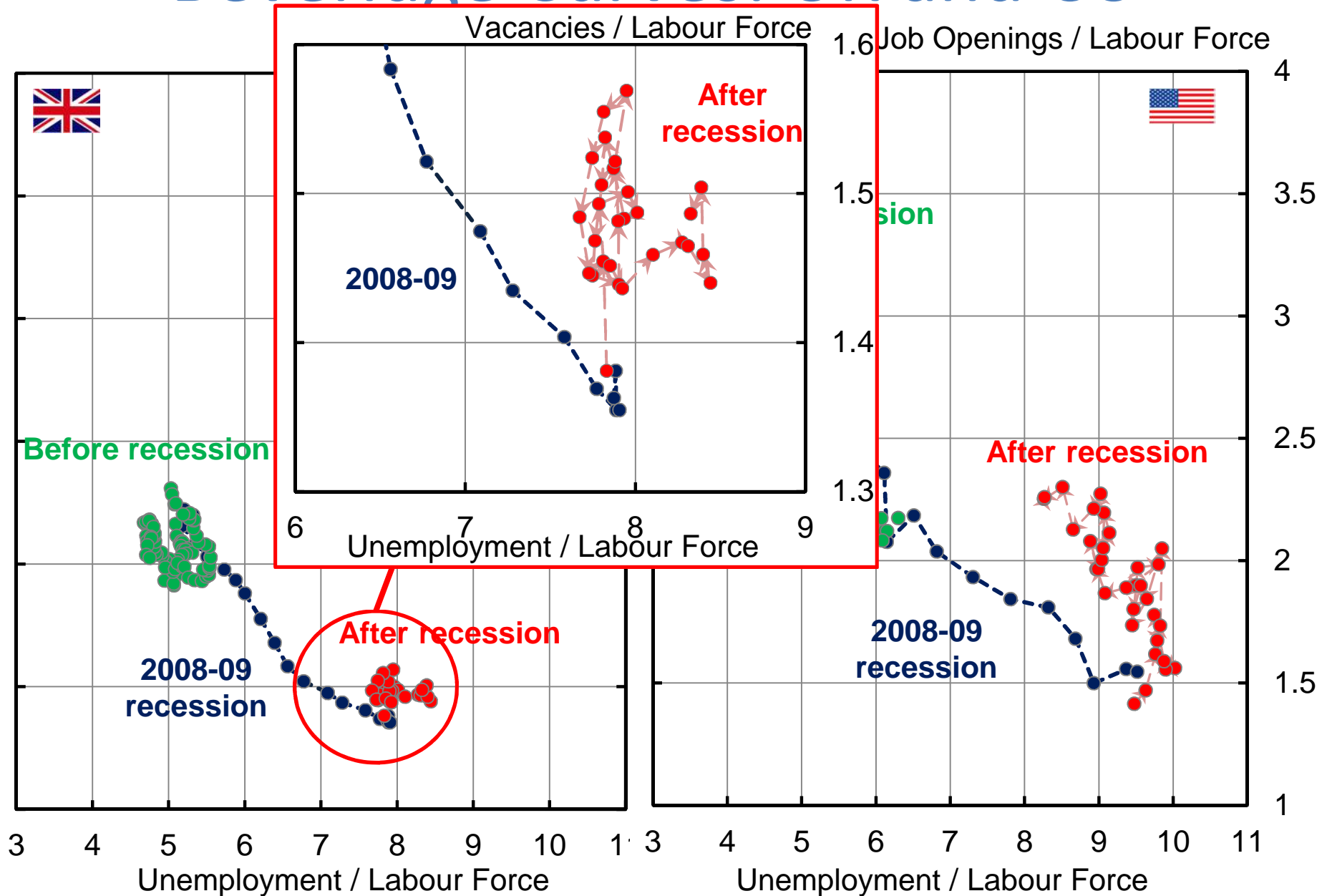
Vacancies / Labour Force

Job Openings / Labour Force



Sources: Author's calculations using ONS Vacancy Survey and ONS LFS and BLS JOLTS and CPS.

# Beveridge Curves: UK and US



Sources: Author's calculations using ONS Vacancy Survey and ONS LFS and BLS JOLTS and CPS.

# Unemployment and Mismatch

## *Methodological contribution*

Develop a method of measuring the contribution of mismatch to unemployment dynamics.

- An extension of previous work
  - Smith (2011); Elsby, Hobijn and Sahin (forthcoming); Elsby, Michaels and Solon (2009); Fujita and Ramey (2009).
- Based on decompositions of unemployment dynamics (steady state or actual).
  - Previously used to examine the influence of inflows and outflows on unemployment.

# Unemployment and Mismatch

## *Methodological contribution*

Develop method of measuring the contribution of mismatch to unemployment dynamics.

- Mismatch affects the unemployment outflow rate:
  - makes it harder for searchers to match with available vacancies.
- If we could measure the extent to which mismatch lowers the job finding rate, we could use decomposition methods estimate the impact of mismatch on unemployment dynamics.
  - It turns out that mismatch also contributes to unemployment dynamics via the separation rate, and this impact can also be estimated.

# Unemployment and Mismatch

- Herz and van Rens (2011)
  - Focus on dynamics: Mismatch unemployment as cyclical as overall unemployment.
  - Path involves wage setting, not worker or job mobility.
- Sahin, Song, Topa and Violante (2012)
  - Mismatch ‘hump’ in Great Recession.
  - Mismatch accounts for at most 1/3 overall unemployment increase.
- Barnichon and Figura (2011)
  - Changes in matching efficiency can explain a part of unemployment dynamics – around 1.5 pp during the Great Recession.

# A Starting Point

The steady state unemployment rate does not capture all the dynamics of interest, especially for a country like the UK where flow transition rates are relatively low.

But it's a useful place to start...

# Unemployment Dynamics and Labour Market Flows

- *Law of Motion for Unemployment:*

$$\Delta U_{t+1} = s_t E_t - f_t U_t$$

Change in unemployment = inflows – outflows.

- Write in terms of unemployment *rate*:

$$\Delta u_{t+1} = s_t (1 - u_t) - f_t u_t$$

- In steady state,

$$\bar{u}_t = \frac{s_t}{f_t + s_t}$$



# Mismatch and Dynamics of the Steady State Unemployment Rate

$$\bar{u}_t = \frac{s_t}{f_t + s_t}$$

Greater mismatch raises  $\bar{u}_t$  directly

- by reducing  $f_t$ .

# Mismatch and Dynamics of the Steady State Unemployment Rate

$$\bar{u}_t = \frac{s_t}{f_t + s_t}$$

Greater mismatch also has an indirect effect on  $\bar{u}_t$

- working through  $s_t$ :
  - $\uparrow$  mismatch  $\rightarrow \downarrow f_t \rightarrow \uparrow U_t$  shrinking the denominator of  $s_t = EU_t / (1 - U_{t-1})$ , thus raising  $s_t$  for given  $EU_t$ .
  - $\frac{\partial^2 \bar{u}_t}{\partial s_t \partial f_t} = \frac{s_t - f_t}{(f_t + s_t)^3} < 0$  since  $f_t \gg s_t$

# Mismatch and Dynamics of the Steady State Unemployment Rate

- Aim:  
Decompose changes in the log unemployment rate, based on a recursive model involving steady state unemployment, into parts:

$$\Delta \ln \bar{u}_t \approx \bar{C}_t^M + \bar{C}_t^{NM}$$

$$\Delta \ln \bar{u}_t \approx \bar{C}_t^{fM} + \bar{C}_t^{fNM} + \bar{C}_t^{sM} + \bar{C}_t^{sNM}$$

# Mismatch and Dynamics of the Steady State Unemployment Rate

Imagine we have:

- an estimate of the **counterfactual unemployment rate** in the absence of mismatch  $u^*$
- and an estimate of the **no-mismatch job finding rate**  $f^*$ .

These estimates can be obtained, under various assumptions,

- using data on hires, unemployment and vacancies
- and estimated matching functions.

I use UK micro QLFS and Vacancy Survey data at industry (18-sector) level.

# Mismatch and Dynamics of the Steady State Unemployment Rate

Simple fact: The steady state unemployment rate can be decomposed into a **part reflecting mismatch**, and a **part reflecting non-mismatch shocks**.

$$\bar{u}_t = \left( \bar{u}_t - \bar{u}_t^* \right) + \bar{u}_t^*$$

Take log differences:

$$\Delta \ln \bar{u}_t \approx \frac{\left( \bar{u}_t - \bar{u}_t^* \right)}{\bar{u}_t} \Delta \ln \left( \bar{u}_t - \bar{u}_t^* \right) + \frac{\bar{u}_t^*}{\bar{u}_t} \Delta \ln \bar{u}_t^*$$

$$\Delta \ln \bar{u}_t \approx \bar{C}_t^M + \bar{C}_t^{NM}$$

# Mismatch and Dynamics of the Steady State Unemployment Rate

Can dig deeper to distinguish the roles of inflow and outflow rates:

$$\Delta \ln \bar{u}_t \approx \bar{C}_t^{fM} + \bar{C}_t^{fNM} + \bar{C}_t^{sM} + \bar{C}_t^{sNM}$$

# Mismatch and Dynamics of the Steady State Unemployment Rate

Can dig deeper to distinguish the roles of inflow and outflow rates:

Consider first the influence of mismatch on unemployment working via the outflow rate.

The overall outflow rate can be written

$$f_t = (f_t - f_t^*) + f_t^*.$$

where:

$(f_t - f_t^*)$  is the effect of **mismatch** on the outflow rate (which is negative).

$f_t^*$  is the outflow rate in the **absence** of mismatch.

# Mismatch and Dynamics of the Steady State Unemployment Rate

$$f_t = (f_t - f_t^*) + f_t^*$$

The steady state unemployment rate can be written:

$$\bar{u}_t = \frac{s_t}{f_t + s_t} = \frac{s_t}{\left( [f_t - f_t^*] + f_t^* \right) + s_t}$$

Decomposition of steady state unemployment (Elsby, Michaels and Solon, 2009):

$$\Delta \ln \bar{u}_t \approx (1 - \bar{u}_t) \{ \Delta \ln s_t - \Delta \ln f_t \}$$



# Mismatch and Dynamics of the Steady State Unemployment Rate

$$f_t = (f_t - f_t^*) + f_t^*$$

The steady state unemployment rate can be written:

$$\bar{u}_t = \frac{s_t}{f_t + s_t} = \frac{s_t}{\left( [f_t - f_t^*] + f_t^* \right) + s_t}$$

So the formula breaking down steady state unemployment dynamics into inflow and outflow influences is:

$$\Delta \ln \bar{u}_t \approx (1 - \bar{u}_t) \left\{ \Delta \ln s_t - \Delta \ln \left( [f_t - f_t^*] + f_t^* \right) \right\}$$

# Mismatch and Dynamics of the Steady State Unemployment Rate

$$\Delta \ln \bar{u}_t \approx (1 - \bar{u}_t) \left\{ \Delta \ln s_t - \Delta \ln \left( \left[ f_t - f_t^* \right] + f_t^* \right) \right\}$$

- To estimate, rearrange final outflow rate term:

$$\Delta \ln \left( \left[ f_t - f_t^* \right] + f_t^* \right) \approx \frac{(f_t - f_t^*)}{f_t} \left[ \frac{f_t}{(f_t - f_t^*)} \Delta \ln f_t - \frac{f_t^*}{(f_t - f_t^*)} \Delta \ln f_t^* \right] + \frac{f_t^*}{f_t} \Delta \ln f_t^*$$

# Mismatch and Dynamics of the Steady State Unemployment Rate

- Changes in the steady state unemployment rate can then be decomposed into 4 parts:

$$\Delta \ln \bar{u}_t \approx \bar{C}_t^{fM} + \bar{C}_t^{fNM} + \bar{C}_t^{sM} + \bar{C}_t^{sNM}$$

$$\bar{C}_t^{fM} = - (1 - \bar{u}_t) \frac{(f_t - f_t^*)}{f_t} \left[ \frac{f_t}{(f_t - f_t^*)} \Delta \ln f_t - \frac{f_t^*}{(f_t - f_t^*)} \Delta \ln f_t^* \right]$$

# Mismatch and Dynamics of the Steady State Unemployment Rate

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$$\Delta \ln \bar{u}_t \approx \bar{C}_t^{fM} + \bar{C}_t^{fNM} + \bar{C}_t^{sM} + \bar{C}_t^{sNM}$$

$$\bar{C}_t^{fNM} = -(1 - \bar{u}_t) \left( \frac{f_t^*}{f_t} \right) \Delta \ln f_t^*$$

# Mismatch and Dynamics of the Steady State Unemployment Rate

- Changes in the steady state unemployment rate can then be decomposed into 4 parts:

$$\Delta \ln \bar{u}_t \approx \bar{C}_t^{fM} + \bar{C}_t^{fNM} + \bar{C}_t^{sM} + \bar{C}_t^{sNM}$$

$$\bar{C}_t^s \equiv \bar{C}_t^{sM} + \bar{C}_t^{sNM} = (1 - \bar{u}_t) \Delta \ln s_t$$

- $\bar{C}_t^M$ ,  $\bar{C}_t^{NM}$ ,  $\bar{C}_t^s$ ,  $\bar{C}_t^{fM}$  and  $\bar{C}_t^{fNM}$  can be directly estimated.
- How can  $\bar{C}_t^s$  be split into  $\bar{C}_t^{sM}$  and  $\bar{C}_t^{sNM}$ ?

$$\bar{C}_t^{sM} = \bar{C}_t^M - \bar{C}_t^{fM}$$

# Mismatch and Dynamics of the Steady State Unemployment Rate

- Changes in the steady state unemployment rate can then be decomposed into 4 parts:

$$\Delta \ln \bar{u}_t \approx \bar{C}_t^{fM} + \bar{C}_t^{fNM} + \bar{C}_t^{sM} + \bar{C}_t^{sNM}$$

- Then either analyse the relative contributions period- by-period, graphically,
- Or calculate 'beta' variance contributions:

$$\beta^{fM} = \frac{\text{cov}(\bar{C}_t^{fM}, \Delta \ln \bar{u}_t)}{\text{var}(\Delta \ln \bar{u}_t)}$$

# Mismatch

## *Measuring mismatch*

I use an index of mismatch

– developed by Sahin, Song, Topa and Violante (2012)

based on a very intuitive idea:

- The *efficient* distribution of unemployed searchers across sectors should vary in proportion to the sectoral distribution of job openings.
  - And if there is *heterogeneity* in matching efficiency across sectors, there should be more unemployed searchers in sectors with higher matching efficiency (“generalised Jackman-Roper condition”).

# Mismatch

## *Measuring mismatch*

I use an index of mismatch

– developed by Sahin, Song, Topa and Violante (2011)

based on a very intuitive idea:

- The *efficient* distribution of unemployed searchers across sectors should vary in proportion to the sectoral distribution of job openings.
- The mismatch index calculates the extent to which hires are lowered by deviation of the actual distribution of unemployment and vacancies across sectors deviates from the efficient distribution.



# An Index of Mismatch

- Index of mismatch  $\mathcal{M}_t$   
captures the proportion by which  
actual hires  $h_t$  fall below the efficient level  $h_t^*$ .

$$\mathcal{M}_t = \frac{h_t^* - h_t}{h_t^*}$$

# An Index of Mismatch

- Assume a Cobb-Douglas CRS matching function in each sector  $i$ :

$$h_{it} = \Phi_t \phi_i v_{it}^\alpha u_{it}^{1-\alpha}$$

where  $h_{it}$ ,  $v_{it}$ , and  $u_{it}$  are hires, vacancies and unemployment, respectively, in sector  $i$  at time  $t$ .

$\Phi_t$  captures changes in matching efficiency common to all sectors.

$\phi_i$  represent sector-specific matching efficiencies.

$\alpha$  is the vacancy share.

# An Index of Mismatch

Constrained-optimal hires:  $h_t^* = \Phi_t \bar{\phi} v_t^\alpha u_t^{1-\alpha}$

Actual hires:  $h_t = \Phi_t v_t^\alpha u_t^{1-\alpha} \left[ \sum_{i=1}^I \phi_i \left( \frac{v_{it}}{v_t} \right)^\alpha \left( \frac{u_{it}}{u_t} \right)^{1-\alpha} \right]$

- Planner allocates unemployed across sectors in proportion to exogenous vacancies and sectoral matching efficiency.

$\bar{\phi} = \left[ \sum_{i=1}^I \phi_i^{\frac{1}{\alpha}} \left( \frac{v_{it}}{v_t} \right) \right]^\alpha$  is a CES aggregator of sector matching efficiencies, weighted by their vacancy shares

# An Index of Mismatch

Constrained-optimal hires:  $h_t^* = \Phi_t \bar{\phi} v_t^\alpha u_t^{1-\alpha}$

Actual hires:  $h_t = \Phi_t v_t^\alpha u_t^{1-\alpha} \left[ \sum_{i=1}^I \phi_i \left( \frac{v_{it}}{v_t} \right)^\alpha \left( \frac{u_{it}}{u_t} \right)^{1-\alpha} \right]$

- In reality, unemployment will not be efficiently allocated, so hires will be lower than optimal.

# An Index of Mismatch

Constrained-optimal hires:  $h_t^* = \Phi_t \bar{\phi} v_t^\alpha u_t^{1-\alpha}$

Actual hires:  $h_t = \Phi_t v_t^\alpha u_t^{1-\alpha} \left[ \sum_{i=1}^I \phi_i \left( \frac{v_{it}}{v_t} \right)^\alpha \left( \frac{u_{it}}{u_t} \right)^{1-\alpha} \right]$

- Measure of mismatch:

$$\mathcal{M}_t = \frac{h_t^* - h_t}{h_t^*} = 1 - \sum_{i=1}^I \left( \frac{\phi_i}{\bar{\phi}} \right) \left( \frac{v_{it}}{v_t} \right)^\alpha \left( \frac{u_{it}}{u_t} \right)^{1-\alpha}$$

# The Job Finding Rate in the Absence of Mismatch

- The aggregate job finding rate is defined as

$$f_t = \frac{h_t}{u_t}$$

- The counterfactual job finding rate in the absence of mismatch would be

$$f_t^* = \frac{h_t^*}{u_t^*} = f_t \frac{1}{1 - \mathcal{M}_t} \left( \frac{u_t}{u_t^*} \right)^\alpha$$

# The Unemployment Rate in the Absence of Mismatch

- The counterfactual job finding rate in the absence of mismatch would be

$$f_t^* = \frac{h_t^*}{u_t^*} = f_t \frac{1}{1 - \mathcal{M}_t} \left( \frac{u_t}{u_t^*} \right)^\alpha$$

- $f_t^*$  and  $u_t^*$  can be calculated simultaneously, using the Law of Motion for  $u_t^*$  and assuming initial condition  $u_0^* = \bar{u}_0^*$ .

$$u_{t+1}^* = s_t + \left( 1 - s_t - f_t^* \right) u_t^*$$

# Estimating Mismatch

- To calculate the mismatch index:

$$\mathcal{M}_t = 1 - \sum_{i=1}^I \left( \frac{\phi_i}{\bar{\phi}} \right) \left( \frac{v_{it}}{v_t} \right)^\alpha \left( \frac{u_{it}}{u_t} \right)^{1-\alpha}$$

requires estimates of vacancy share  $\alpha$  and industry-specific match efficiencies  $\phi_i$ .

- To obtain these, estimate a matching function:

$$\ln \left( \frac{h_{it}}{u_{it}} \right) = \ln \Phi_t + \ln \phi_i + \alpha \ln \left( \frac{v_{it}}{u_{it}} \right) + \varepsilon_{it}$$



# Estimates of Vacancy Share $\alpha$

	(1)
$\alpha$	0.632*** (0.0251)
Fixed effects	yes
Quadratic time trend	yes
Seasonal dummies	yes
$R^2$	0.720
Observations	756
Industries	18
Sample period	2001q3-20011q4

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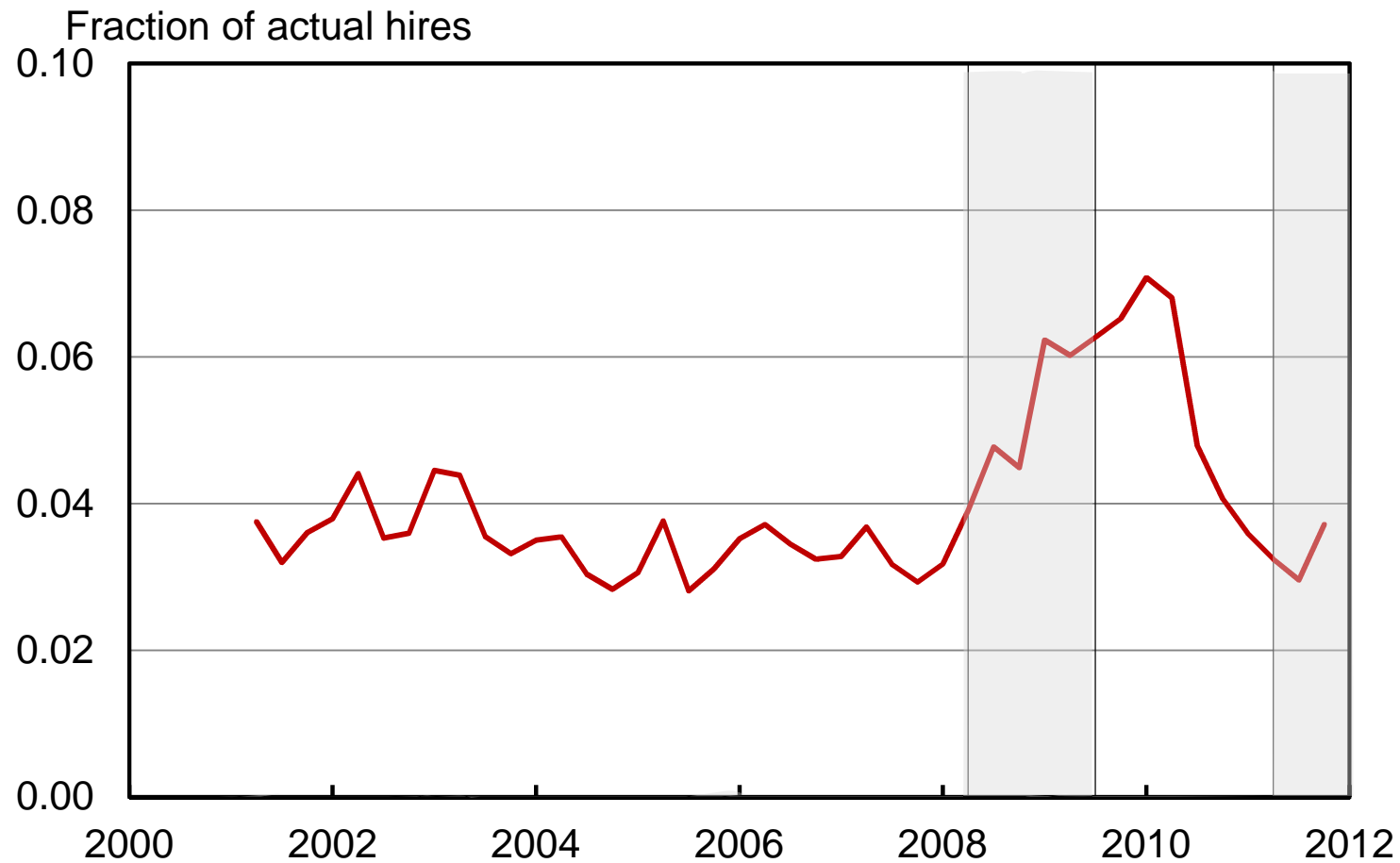
# Estimates of Vacancy Share $\alpha$

	(1)	(2) No time trend	(3) Pre-2008q2	(4) OLS
$\alpha$	0.632*** (0.0251)	0.800*** (0.0213)	0.750*** (0.0371)	0.522*** (0.0181)
Fixed effects	yes	yes	yes	no
Quadratic time trend	yes	no	yes	yes
Seasonal dummies	yes	yes	yes	yes
$R^2$	0.720	0.762	0.752	0.686
Observations	756	756	486	756
Industries	18	18	18	18
Sample period	2001q3-20011q4	2001q3-20011q4	2001q3-2008q1	2001q3-20011q4

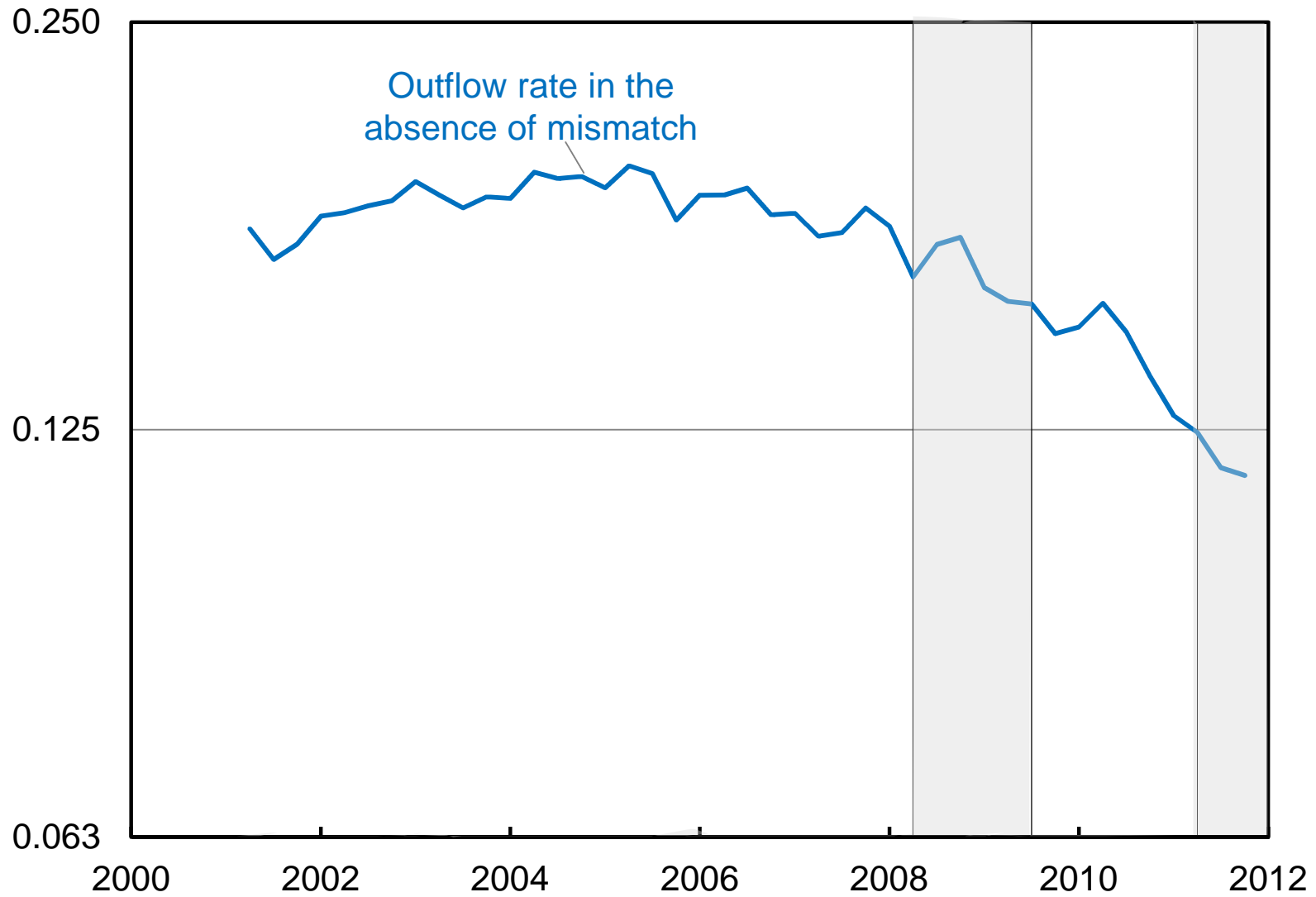
# The Mismatch Index

Proportionate increase in  
actual hires that would occur  
if mismatch were eliminated:

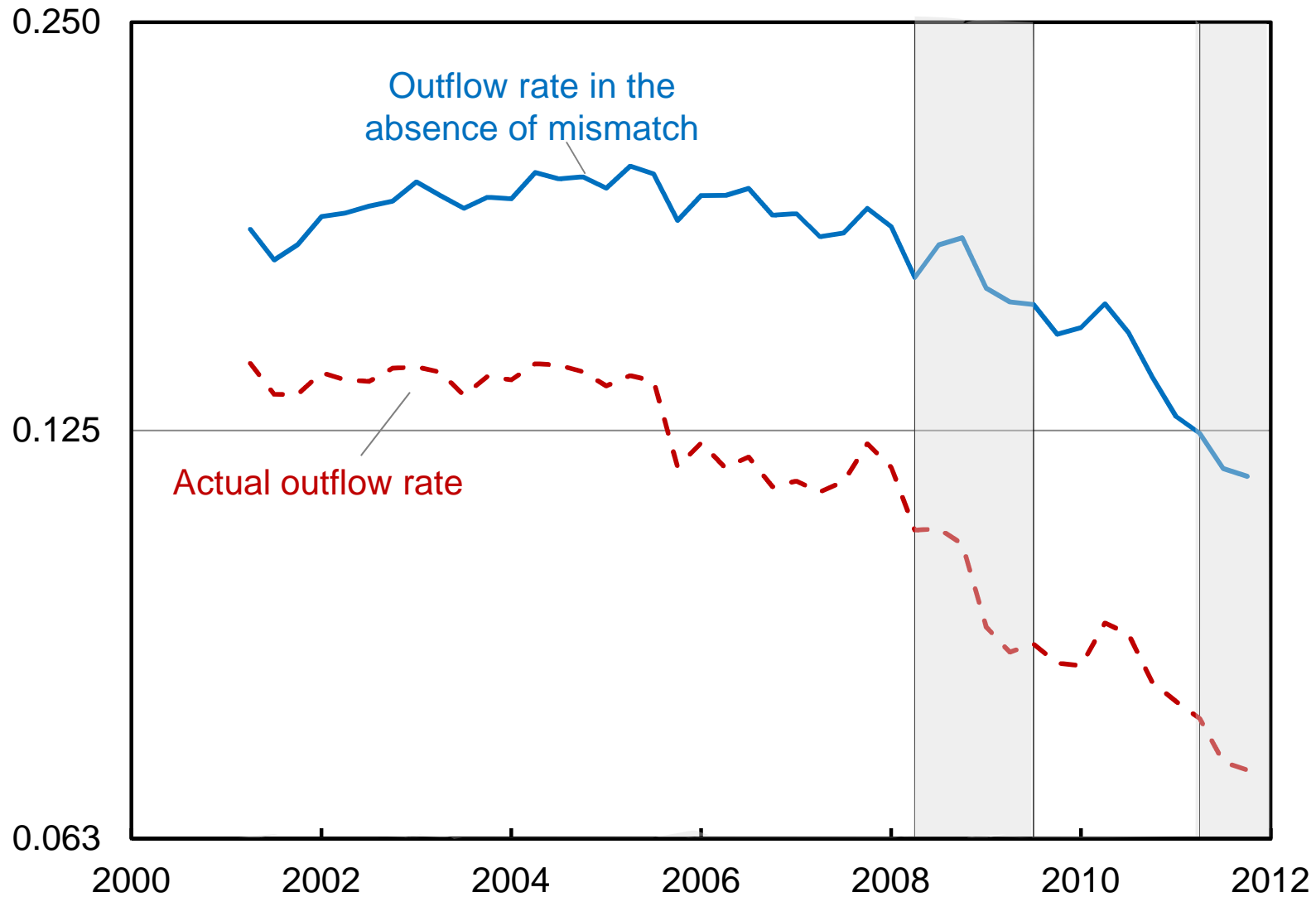
$$\frac{M_t}{1 - M_t}$$



# The Impact of Mismatch on the Outflow Rate

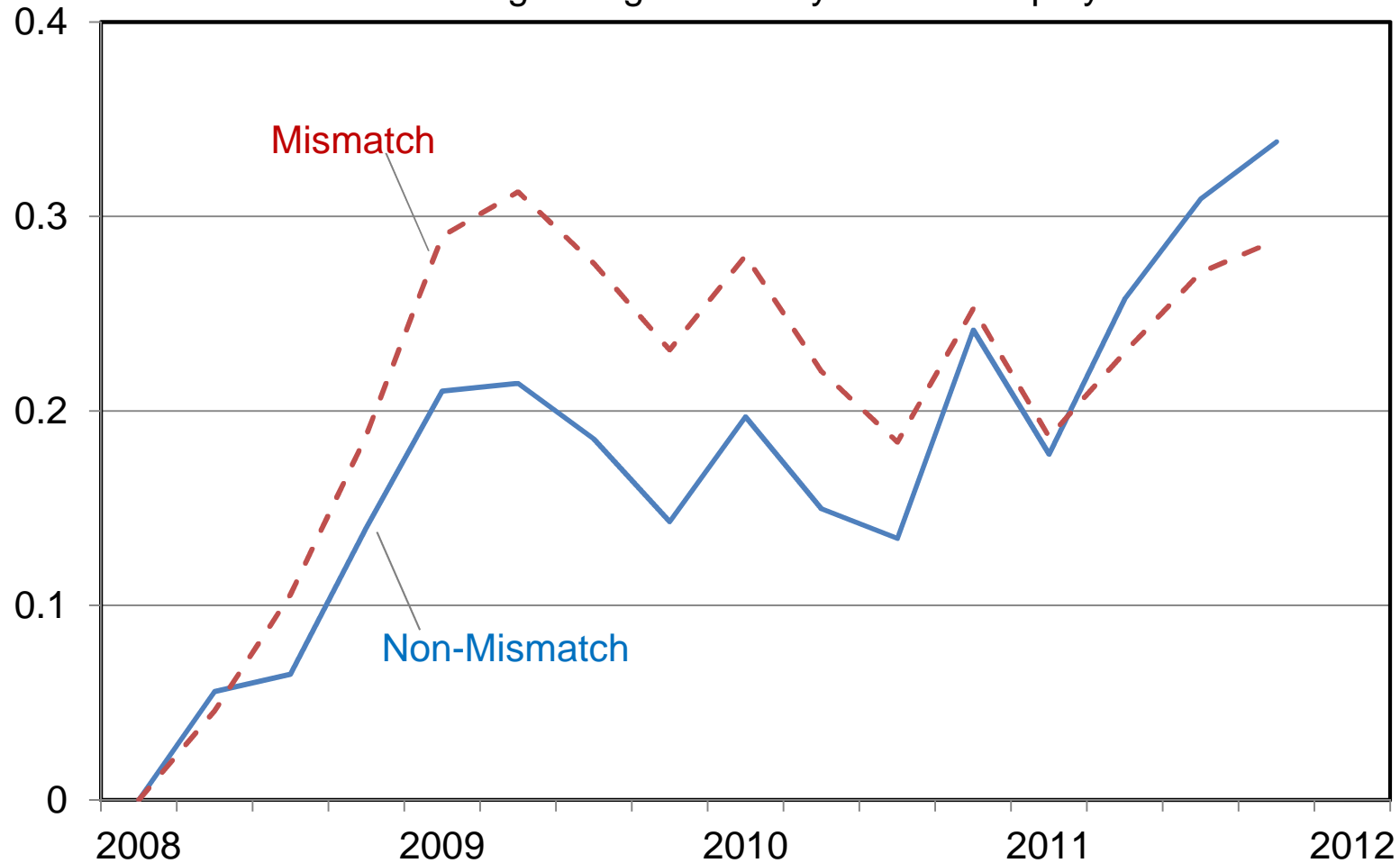


# The Impact of Mismatch on the Outflow Rate



# Mismatch Contribution to Steady State Unemployment Dynamics

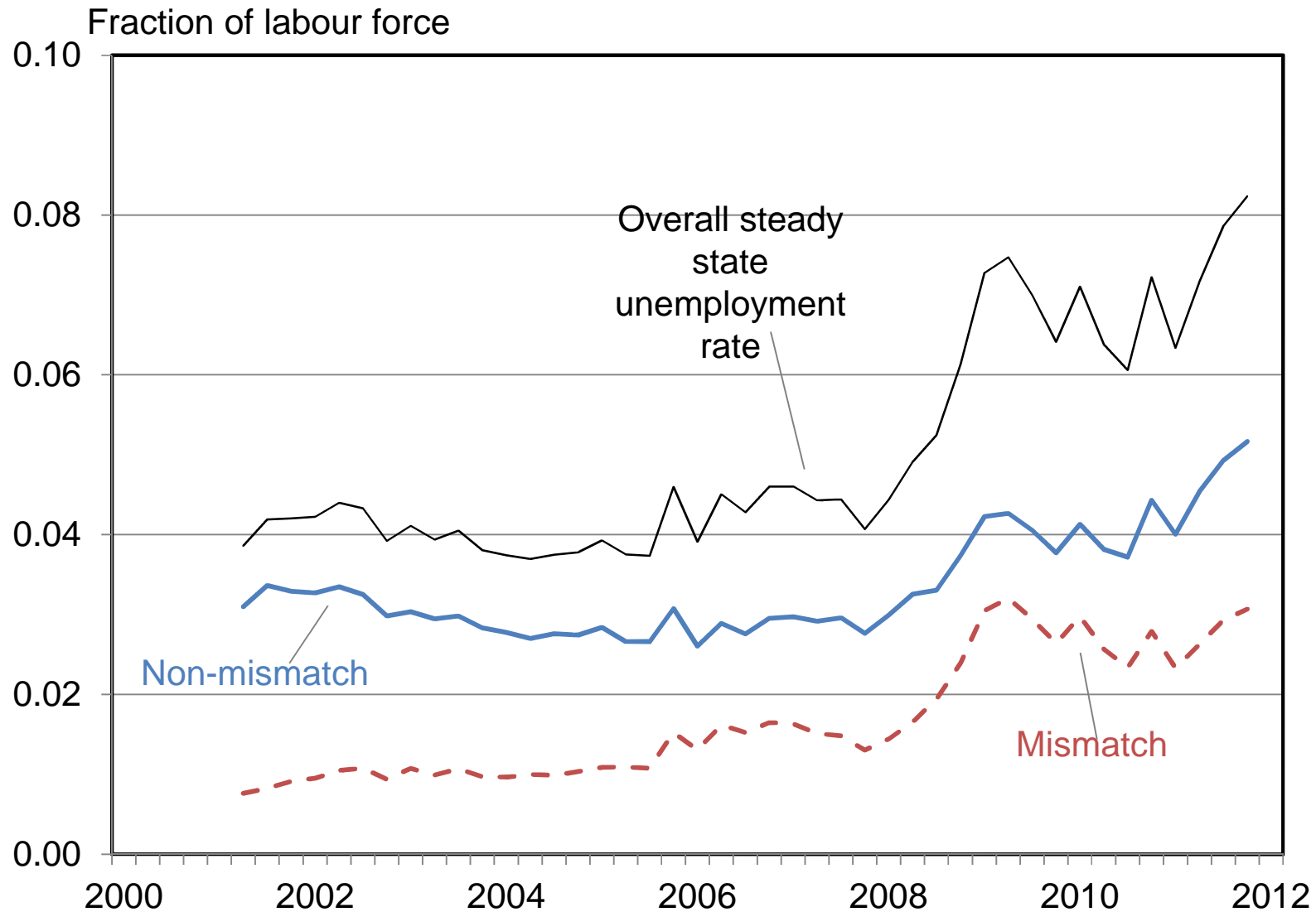
Cumulative contribution to log change in steady state unemployment



# Mismatch Contribution to Steady State Unemployment Dynamics

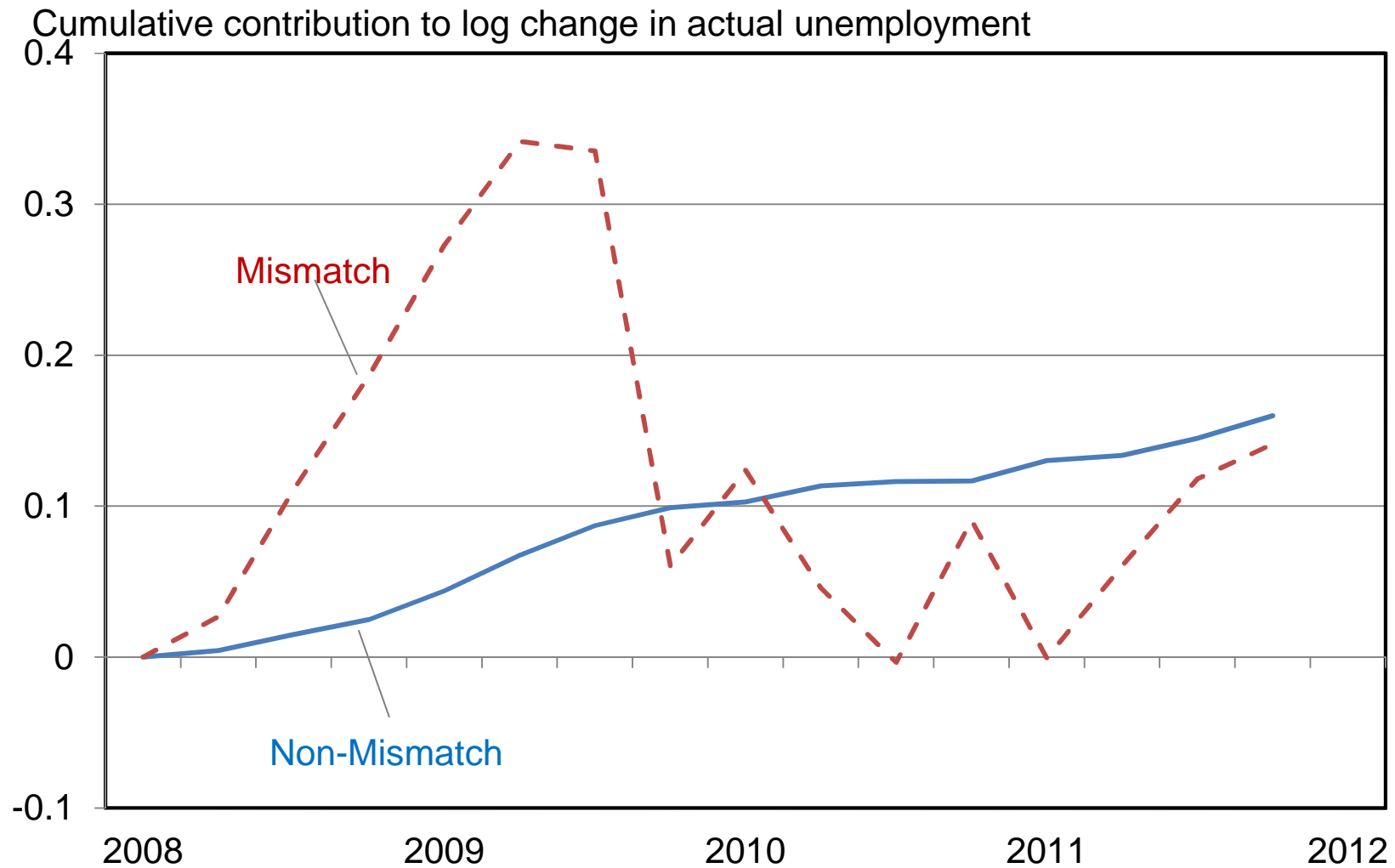
		Mismatch	Non-mismatch
<b>Pre-recession</b>	2001q3- 2008q1	0.44	0.57
<b>Recession</b>	2008q2- 2009q3	<b>0.54</b>	<b>0.46</b>
<b>Post-recession</b>	2009q4- 2011q4	0.46	0.54
<b>Full sample</b>	2001q3- 2011q4	0.47	0.54

# Steady State Unemployment Due to Mismatch and Other Influences

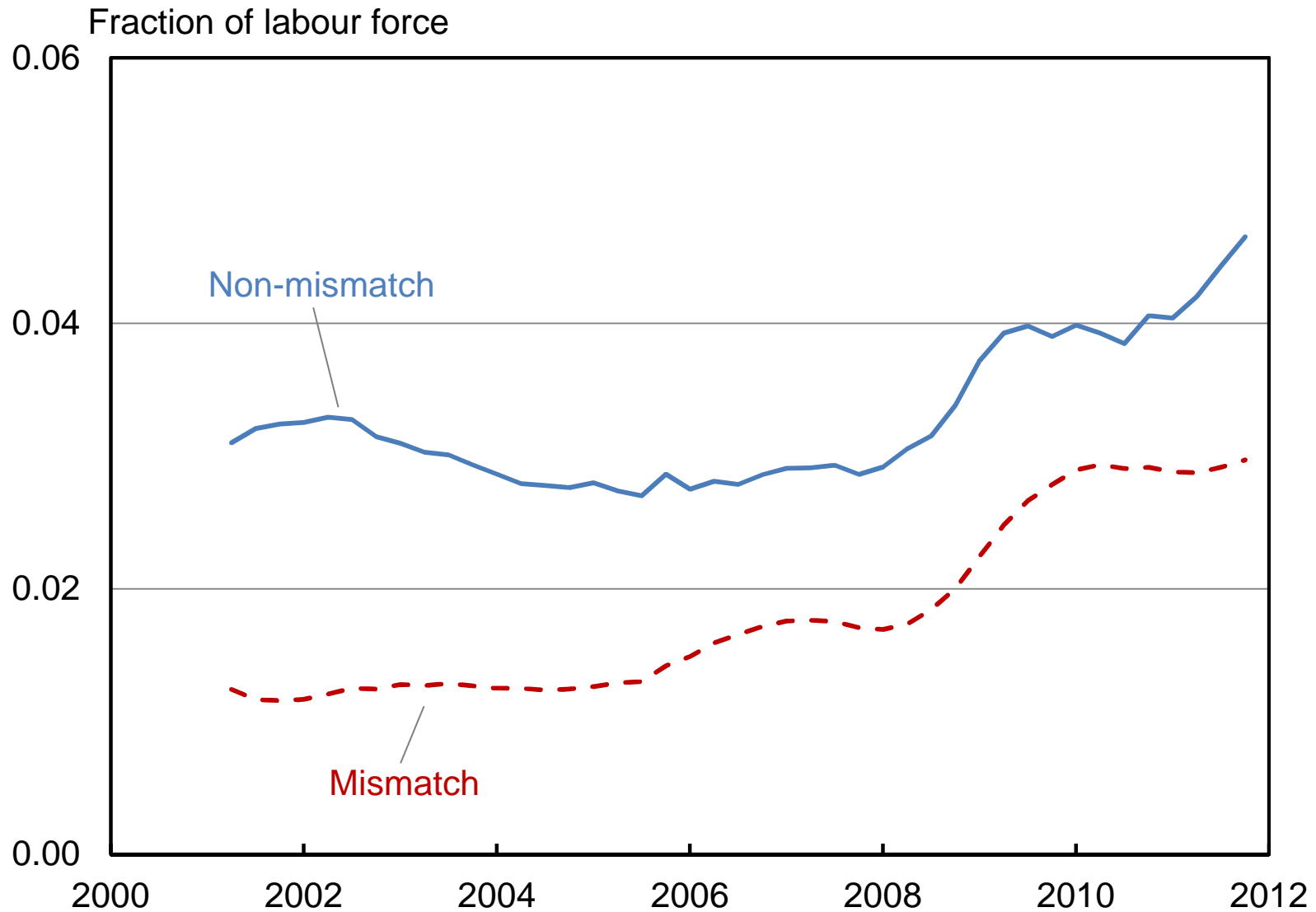




# Mismatch Contribution to Actual Unemployment Dynamics



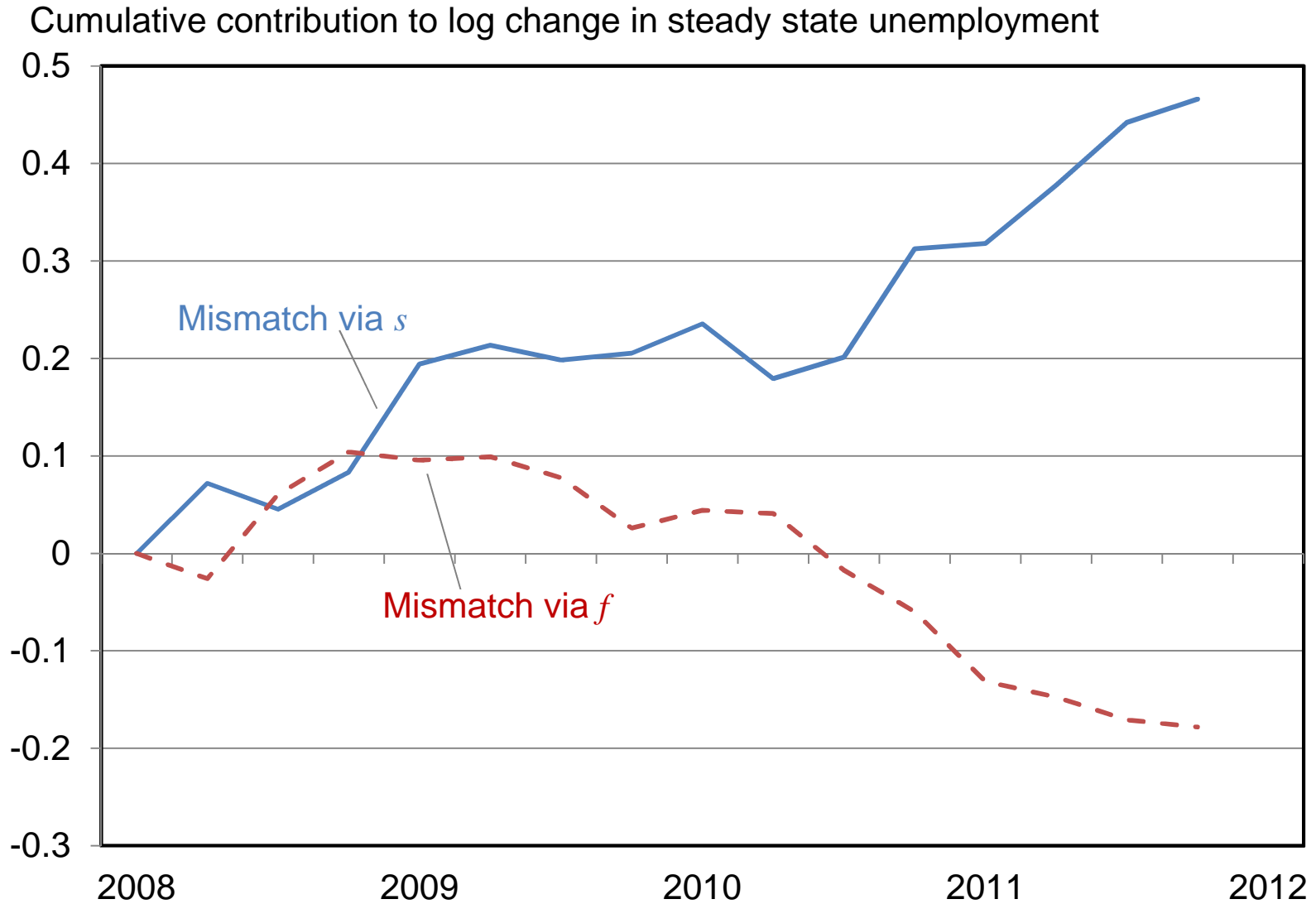
# Actual Unemployment Due to Mismatch and Other Influences



# Flow Transition Rate Contributions to Steady State Unemployment Dynamics

Beta		Overall <i>f</i>	Overall <i>s</i>
Pre-recession	2001q3- 2008q1	44%	56%
Recession	2008q2- 2009q3	44%	57%
Post-recession	2009q4- 2011q4	20%	80%
Full sample	2001q3- 2011q4	37%	63%

# Mismatch Paths



# Mismatch Paths

Beta		Mismatch		Non-mismatch	
		<i>f</i>	<i>s</i>	<i>f</i>	<i>s</i>
Pre-recession	2001q3-2008q1	6%	39%	38%	17%
Recession	2008q2-2009q3	11%	44%	33%	13%
Post-recession	2009q4-2011q4	12%	35%	8%	46%
Full sample	2001q3-2011q4	8%	38%	29%	25%

# Conclusions

- Mismatch does appear to have played a role in UK unemployment dynamics.
- The indirect effect of mismatch, which raises the impact of inflow rate increases, seems to play an important part.

