

Week 2 - Chi-square/SPSS handout

Chi-square (χ^2) statistic = (Amount of) evidence of a relationship

		<u>Conclusion</u>
Large chi-square (χ^2) statistic	\Rightarrow	\surd relationship
Small chi-square (χ^2) statistic	\Rightarrow	\times relationship

What kind of sizes (values) of the χ^2 statistic occur just as a consequence of sampling error (i.e. if there is no relationship)?

What value is only exceeded by one in twenty, or 5% ($p=0.05$), of χ^2 statistics if there is no relationship?

The **critical value** of χ^2_3 (at the 5% level) is 7.815

The SPSS syntax file CHISQ.SPS and the corresponding data file CHISQ.SAV can be used to generate samples (and hence χ^2 statistics) corresponding to two populations: (i) a 'real' population where there is a relationship between class and the presence/absence of teeth and (ii) a 'hypothetical' population where there is no relationship between class and the presence/absence of teeth.

[Download the data file *chisq.sav* from the following webpage:

<http://go.warwick.ac.uk/so201/schedule/week2>

Open the syntax file *chisq.sps* from the same page].

\times : $P \geq 0.05$
 \surd : $P < 0.05$

TABLE	SAMPLES FROM 'HYPOTHETICAL' POPULATION			SAMPLES FROM 'REAL' POPULATION		
	χ^2	SIGNIFICANCE	(p)	χ^2	SIGNIFICANCE	(p)
1	1.552	0.670	X	14.629	0.002	\surd
2	4.244	0.236	X	14.640	0.002	\surd
3	2.187	0.535	X	16.724	0.001	\surd
4	0.748	0.862	X	6.681	0.083	X
5	3.003	0.391	X	15.965	0.001	\surd
6	1.220	0.748	X	4.867	0.182	X
7	3.920	0.270	X	7.322	0.062	X
8	3.677	0.299	X	16.179	0.001	\surd
9	3.651	0.302	X	7.905	0.048	\surd
10	0.348	0.951	X	18.924	0.000	\surd

\rightarrow TOTAL 24.550 (V: 0/10) TOTAL 123.836 (V: 7/10)
 If there is a relationship in the population, the size of the chi-square statistic depends on: (i) the strength of the relationship; (ii) the shape of the table; (iii) sample size.
 MEAN \approx 2.5 \leftarrow SAMPLING ERROR MEAN \approx 12.4
UNDERLYING PATTERN + SAMPLING ERROR