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Economics in the Real World for Pre-University Students

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Session #2: Intertemporal Cooperation and Coordination

Repeated Interaction as an alternative to the State

- Repeated Interaction. No State present, like in International context.
- Main aim: Explore when and if players (*countries*) can cooperate for mutually benefit *across time* - *intertemporal cooperation*.
- Central Idea: *"Carrots and Sticks"* - Attempt to cooperate (the "carrot") with deviations (cheating) by others from that met with punishment (the "stick").
- Dealing with the problem of *short-run temptation to cheat*.
- Key Trade-off: Benefit from cheating *today* versus costs from doing so, which come from the loss of the benefits from *future cooperation*.

Repeated PD Game

- **Key Feature:** Each time they play the PD game, they **know the history of past plays** (except the first time they play as there is no history).
- Objective for each player – UK and EU: To maximise the present discounted value of their payoffs.
- Let each player **discount future payoffs** at some rate, which we denote by δ , which is a number between 0 and 1. **So £1 secured tomorrow is worth δ today – which is less than 1.**
- The more a player cares about **future** payoffs the **higher** is the value of δ .

Repeated PD – Sustaining Cooperation

The Grim-Trigger Strategy

- India adopts the “*grim-trigger*” strategy:

First time they play the PD game, UK chooses **C** (to cooperate).

Thereafter, UK plays as follows: Play **C** *if* both players (UK and USA) played **C** throughout the past. Otherwise, play **D**.

- USA also adopts the same grim-trigger strategy.
- **Note therefore that the outcome each time they play will be that both of them will cooperate, choose C, and thus each obtains a payoff of 5 each time they play.**

Repeated PD – Sustaining Cooperation

Costs and Benefits of Cheating.

- Benefit from cheating “today” – the temptation: Getting an 8 rather than a 5. **Hence the “short-run” benefit from cheating is: $8 - 5 = 3$.**
- Cost from cheating “today” are the losses from “tomorrow” onwards of benefits from cooperation. **Hence the “long-run” cost from cheating is: loss of $5 - 1 = 4$ each period from tomorrow onwards.**
- The **present discounted value** of these losses are:

$$4\delta + 4\delta^2 + 4\delta^3 + 4\delta^4 + 4\delta^5 + \dots = \frac{4\delta}{1-\delta}$$

- **Notice that when $\delta = 0$, these losses are also zero. Indeed, when δ is small, these losses will be small and close to zero - and so well below 3, which is the temptation from cheating.**

Repeated PD – Sustaining Cooperation

Incentive-Compatibility Condition for Not Cheating:

The Future needs to matter sufficiently

- Each player will **not** cheat provided the benefit from cheating is **less than or equal to** the cost from cheating. That is the following holds:

$$3 \leq \frac{4\delta}{1-\delta}$$

- This will not hold if the discount factor is sufficiently small. **This means that when a player does not care much about future payoffs then s/he will cheat and thus cooperation will not be sustained.**
- But if the discount factor is sufficiently large, then the above inequality will hold. **This means that when both players care sufficiently about their respective future payoffs, then neither of them has as an incentive to cheat and thus cooperation is sustained.**

Coordination Problems with Conflict of Interest

The Battle of Sexes game

C = Colosseum

B = Ballet

Romeo:

Juliet:

	<i>C</i>	<i>B</i>
<i>C</i>	2, 3	0, 0
<i>B</i>	0, 0	3, 2

Nash Demand Game: coordination with conflict

- **Two Players:** A and B.
- **Strategies:** Each player chooses – or *demands* - how much of the £100 she wants – so states a number between £0 and £100.
- **Choices** are made “simultaneously” - no communication
- **Payoffs:** If the sum of the two demands exceeds £100, each player gets nothing. But if the sum of the demands is less than or equal to £100, then each gets what they respectively demanded.
- **What demand will you choose?**