International Business and Finance Seminar 3

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Road Map

- ▶ In the first two seminars, we've mainly covered
 - ▶ Bank essentials: balance sheet; how banks make money; measurements of banks' performance
 - ▶ Bond essentials: interest rate; compounding; present value and future value

► Today's seminar will be a bridge between the first two seminars and Friday's seminar, when we will talk extensively about derivatives

More on Future Value and Present Value

Formal way of defining intra-year compounding

$$FV = PV \left(1 + \frac{r}{m}\right)^{m.t}$$

And if
$$m \to +\infty$$
, using $\lim_{m \to \infty} \left(1 + \frac{1}{m}\right)^m = e$, then $FV = PV.e^{r.t}$

► The present value of a multiple cash inflows

If an investment project has a series of expected cash flows C_1, C_2, \dots, C_t extending over t years and if we also assume that the interest (or discount) rate r has no significant change in this period, the present value of all expected returns will be calculated by :

$$PV = \frac{C_1}{(1+r)} + \frac{C_2}{(1+r)^2} + \dots + \frac{C_t}{(1+r)^t} = \sum_{i=1}^t \frac{C_i}{(1+r)^i}$$

Net Present Value

- ► Net present value, is a measure of "is it a good deal?"
 - NPV is essentially all your future earnings discounted to today, minus all costs discounted to today
 - Positive NPV usually indicates good investment, because well, why not?

$$NPV = \sum_{i=1}^{t} \frac{C_i}{(1+r)^i} - I_0 > 0$$

$$NPV = \sum_{i=1}^{t} \frac{C_i}{(1+r)^i} - \sum_{j=0}^{m} \frac{I_j}{(1+r)^j} > 0 \quad (m \le t)$$

Some Very Important Algebra

$$a_n = a_1 + (n-1)d$$

$$S_n = \frac{n}{2} [2a_1 + (n-1)d]$$

$$= \frac{n}{2} [a_1 + a_n]$$

$$d = a_n - a_{n-1}$$

where,

→
$$a_n$$
 = n^{th} term
→ a_1 = 1^{st} term
→ n = number of terms
→ S_n = Sum of n terms
→ a_{n-1} = n - 1^{th} term

nth term of a geometric sequence a, ar, ar2,..... is,

$$a_n = ar^{n-1}$$

Sum of n term of a finite geometric sequence is,

$$a + ar^{2} + ar^{3} + + ar^{n-1}$$

$$= \underbrace{a(1 - r^{n})}_{1 - r^{n}}, \text{ when } r \neq 1$$

Sum of infinite geometric sequence is,

$$a + ar^2 + ar^3 + = \frac{a}{1-r}$$
, when r < 1

When Sequences Meet Infinity

$$\lim_{n o \infty} \sum_{k=1}^n a * r^k = \lim_{n o \infty} a * rac{r(1-r^n)}{1-r} = a * rac{r}{1-r} = rac{a}{rac{1}{r}-1}$$

The PV of a perpetuity:

$$PV = \frac{C}{(1+r)} + \frac{C}{(1+r)^2} + \frac{C}{(1+r)^3} + \dots = \sum_{t=1}^{\infty} \frac{C}{(1+r)^t}$$

So, $\frac{PV}{r} = \frac{c}{r}$ and the rate of return for a perpetuity can be obtained as: $r = \frac{c}{PV}$

Present Value of Bond

$$PV = \frac{C}{(1+r)} + \frac{C}{(1+r)^2} + \dots + \frac{C}{(1+r)^t} + \frac{Face\ Value}{(1+r)^t} = \sum_{i=1}^t \frac{C}{(1+r)^i} + \frac{C}{(1+r)^t} = \sum_{i=1}^t \frac{C}{(1+r)^i} + \frac{C}{(1+r)^t} = \sum_{i=1}^t \frac{C}{(1+r)^i} + \frac{C}{(1+r)^t} = \sum_{i=1}^t \frac{C}{(1+r)^i} + \frac{C}{(1+r)^i} = \sum$$

$$PV = \frac{C}{(1+r)} + \frac{C}{(1+r)^2} + \dots = \sum_{i=1}^{\infty} \frac{C}{(1+r)^i} = \frac{C}{r}$$

Growing Perpetuity

Growing Perpetuity:

Let's consider the situation that the stream of a cash flow growing at a constant rate g, so, the PV for growing perpetuity can be written as follows:

$$PV = \frac{C_1}{(1+r)} + \frac{C_2}{(1+r)^2} + \frac{C_3}{(1+r)^3} + \cdots$$

$$= \frac{C_1}{(1+r)} + \frac{C_1(1+g)}{(1+r)^2} + \frac{C_1(1+g)^2}{(1+r)^3} + \cdots$$

$$= \sum_{i=1}^{\infty} \frac{C_1(1+g)^{i-1}}{(1+r)^i} = \frac{C_1}{r-g}$$

The Present Value of Equity: Valuation of Common Stocks

The Present Value of Equity:

There are two sources of payoff for the shareowners (if they stay with their shares for a year): a) cash dividends and b) capital gain or loss.

If P_0 , P_1 are the current and expected price (after a year) of a share, respectively, and Div_1 is the expected dividend at the end of a year; the expected rate of return r at the end of the year is:

$$r = \frac{Div_1 + (P_1 - P_0)}{P_0}$$

If dividends grow at a constant rate g each year (like growing perpetuity), the current share price can be calculated by:

$$P_0 = \frac{Div_1}{r - g} \quad (if \ r > g)$$

We can re-write the formula to show r (expected return) as the subject. In this case;

$$r = \frac{Div_1}{P_0} + g$$

Question 6: In 2019, Daimler Chrysler had just paid a dividend of €2 per share on its equity. The dividends are expected to grow at a constant rate of 5% per year indefinitely. If investors require an 11% return on the company's equity:

- a. What is the current price?
- b. What will be the price in 2022?
- c. What will be the price in 2034?

Question 6:

a. Current price at a constant growth of 5 per cent per year indefinitely

- b. Price in 3 years: $P = P_0(1+g)^3 = \text{€}35(1.05)^3 = \text{€}40.52$
- c. Price in 15 years: $P = P_0(1+g)^{15} = \text{€}35(1.05)^{15} = \text{€}72.76$

Exercises on NPV

- You can decide today to invest in a machine that costs £1600, paid regardless of the state of nature at the end of a year
- At the end of year, the machine produces one unit of product, which is worth £300 or £100, with 50-50 probability
- The weighted average cost of capital (WACC) is 10%
- What is the NPV today if the machine can be only used for one period?
- What is the NPV today if the machine continues to produce forever and the price level stays the same forever?

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NPV(one period) =
$$\frac{(-1600 + 0.5^*300 + 0.5^*100)}{1.1} = -1272.7$$

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$$egin{aligned} NPV_1 &= -1,600 + [0.5(300) + 0.5(100)] + \sum_{t=1}^{\infty} rac{0.5(300) + 0.5(100)}{(1+0.1)^t} \ &= -1,600 + 200 + rac{200}{0.1} = 600 \ NPV_0 &= 600/1.1 = 545.5. \end{aligned}$$